

鉄系高温超伝導体

銅酸化物、重い電子系との比較

超伝導ギャップ構造

量子臨界点



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量子臨界点



High- T_c cuprates

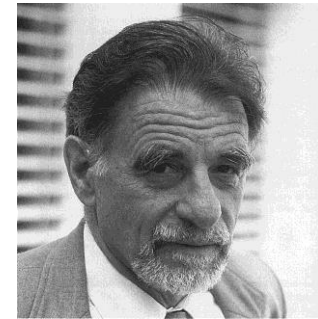
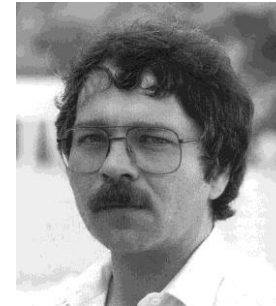
Possible High T_c Superconductivity in the Ba – La – Cu – O System

J.G. Bednorz and K.A. Müller

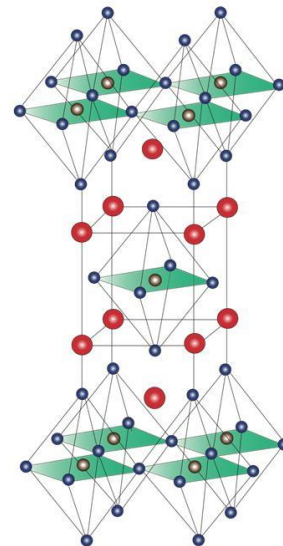
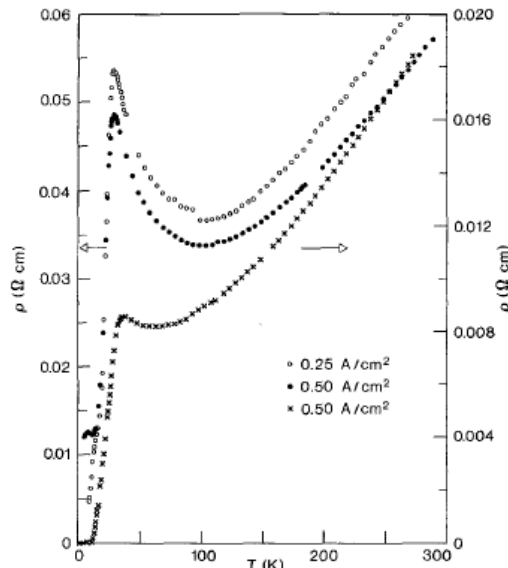
IBM Zürich Research Laboratory, Rüschlikon, Switzerland

Received April 17, 1986

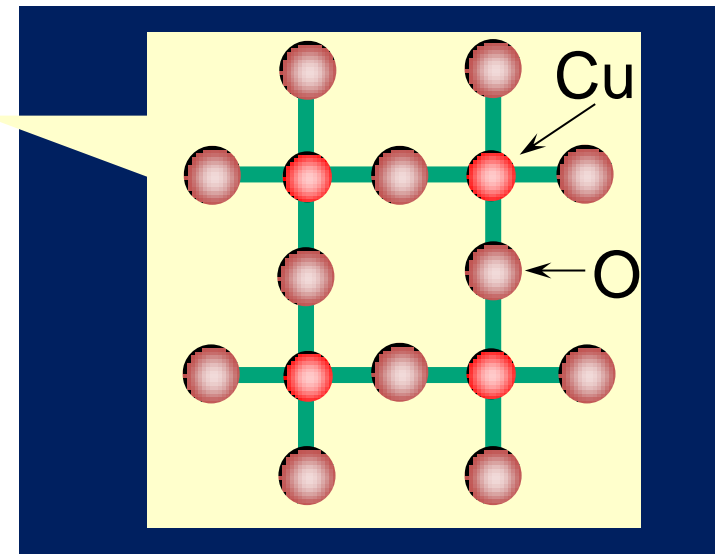
Metallic, oxygen-deficient compounds in the Ba – La – Cu – O system, with the composition $\text{Ba}_x\text{La}_{5-x}\text{Cu}_5\text{O}_{5(3-y)}$ have been prepared in polycrystalline form. Samples with $x=1$ and 0.75 , $y>0$, annealed below 900°C under reducing conditions, consist of three phases, one of them a perovskite-like mixed-valent copper compound. Upon cooling, the samples show a linear decrease in resistivity, then an approximately logarithmic increase, interpreted as a beginning of localization. Finally an abrupt decrease by up to three orders of magnitude occurs, reminiscent of the onset of percolative superconductivity. The highest onset temperature is observed in the 30 K range. It is markedly reduced by high current densities. Thus, it results partially from the percolative nature, but possibly also from 2D superconducting fluctuations of double perovskite layers of one of the phases present.



Superconductivity in CuO_2 planes

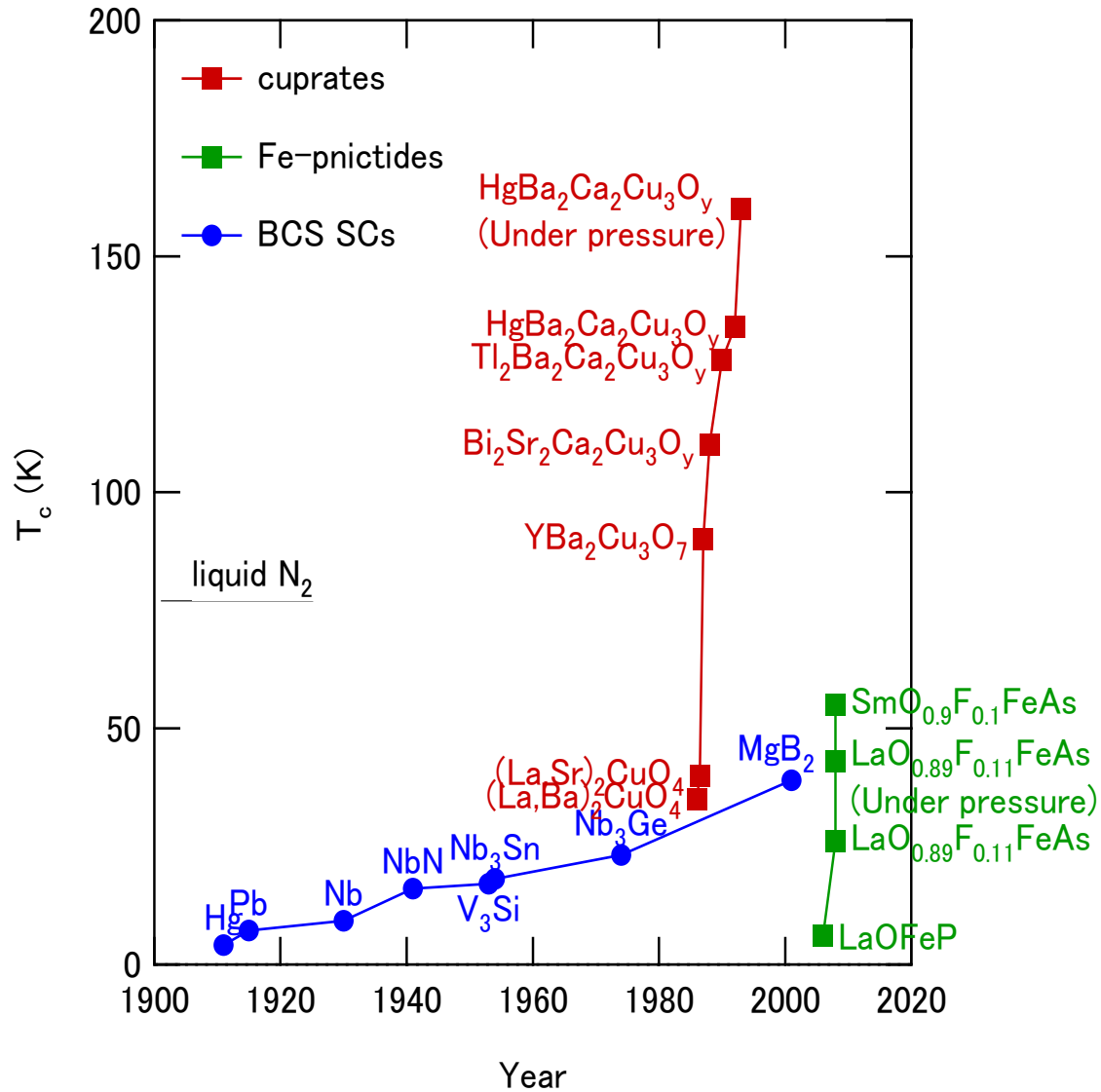


● La/Sr ● Cu ● O



J. G. Bednorz and K.A. Müller, Zeitschrift für Physik B **64**, 189 (1986).

Fe-based high- T_c superconductors



Superconductivity in Fe-Pnictides — Discovery

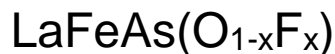
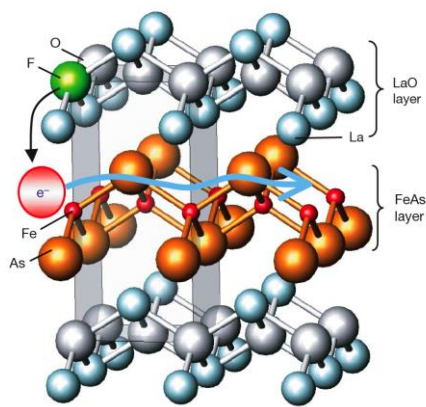
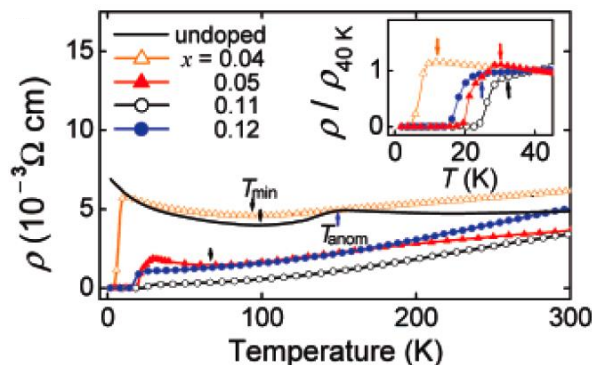
J|A|C|S
COMMUNICATIONS

Published on Web 02/23/2008

Iron-Based Layered Superconductor $\text{La}[\text{O}_{1-x}\text{F}_x]\text{FeAs}$ ($x = 0.05\text{--}0.12$) with $T_c = 26\text{ K}$

Yoichi Kamihara,^{*,†} Takumi Watanabe,[‡] Masahiro Hirano,^{†,§} and Hideo Hosono^{†,‡,§}

ERATO-SORST, JST, Frontier Research Center, Tokyo Institute of Technology, Mail Box S2-13, Materials and Structures Laboratory, Tokyo Institute of Technology, Mail Box R3-1, and Frontier Research Center, Tokyo Institute of Technology, Mail Box S2-13, 4259 Nagatsuta, Midori-ku, Yokohama 226-8503, Japan



Y. Kamihara *et al.*, JACS, **130**, 3296 (2008).

High- T_c superconductors

Hosono's group was not looking for superconductor, but trying to create new kind of transparent semiconductors for flat-panel display.

LaFePO $T_c=4$ K

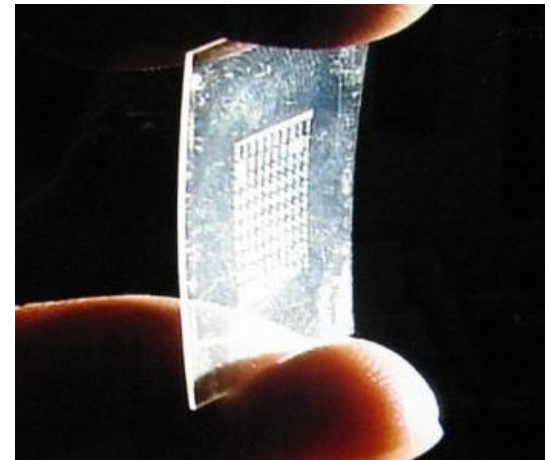
LaFeP(O,F) $T_c=7$ K

LaFeAs(O,F) $T_c=26$ K

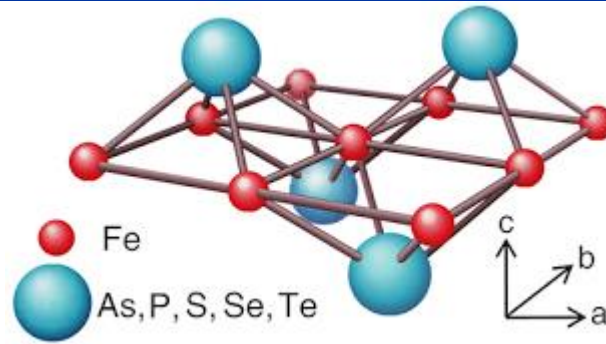
SmFeAs(O,F) $T_c=56$ K



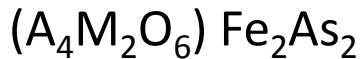
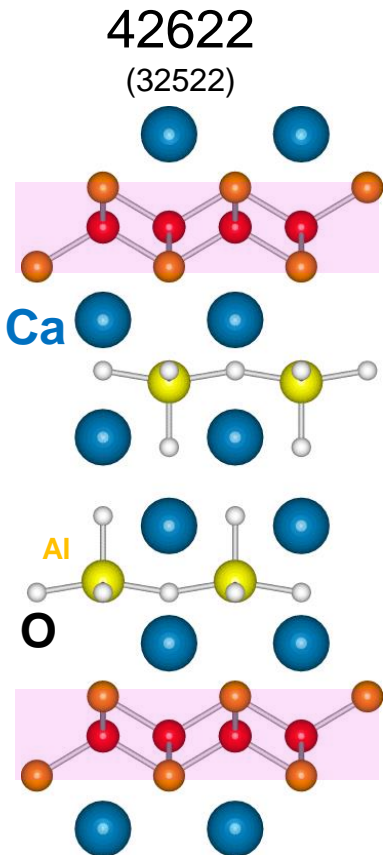
Only two months!



Fe-based high- T_c superconductors

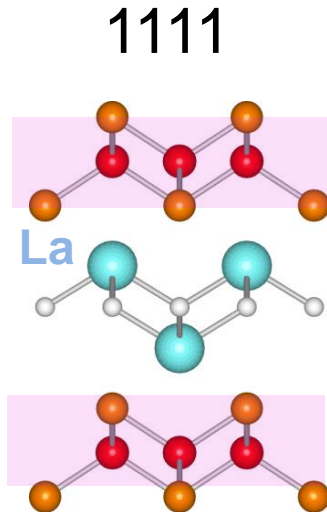


2D square lattice of Fe



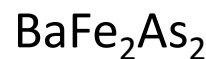
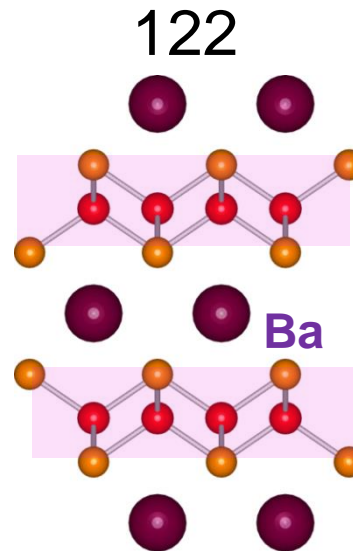
$T_c(\text{max})=47\text{K}$

Zhu et al.(2009)
Ogino et al. (2009)



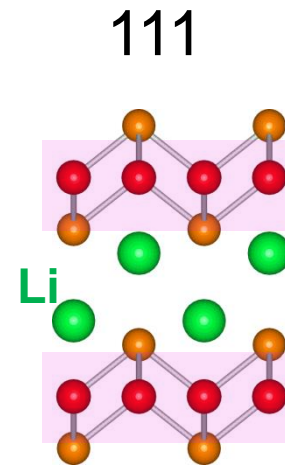
$T_c(\text{max})=55\text{K}$

Y. Kamihara et al.(2008)



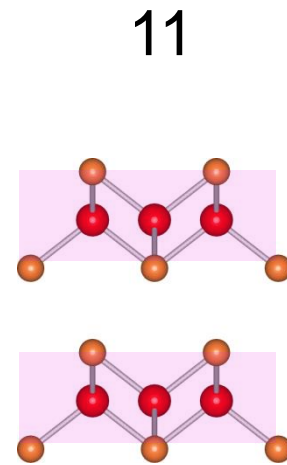
$T_c(\text{max})=38\text{K}$

M. Rotter et al.(2008)



$T_c=18\text{K}$

X.C.Wang et al.(2008)



$T_c=8\text{K}$

F.C.Hsu et al.(2008)

Fe-based high- T_c superconductors

Are iron-pnictides an Electron-Phonon Superconductor?

$$T_c \sim \omega_D e^{-\frac{1}{\lambda}}$$

$$\omega_D \sim 200 \text{ K}$$

ω_D Debye frequency

$$\lambda \sim 0.2$$

λ Electron-phonon coupling Comparable to the conventional metals

$$\Rightarrow T_c \sim 1 \text{ K}$$

Electron-phonon coupling is not sufficient to explain superconductivity in the whole family of Fe-As based superconductors

Why are Fe-based HTSC important?

1. A new class of high temperature superconductors

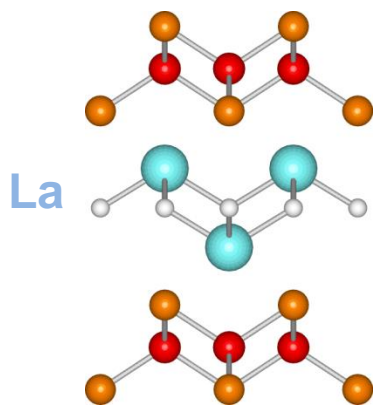
They knocked the cuprates off their pedestal as a unique class of high temperature superconductors.

2. A new family of unconventional superconductors

A possible new mechanism of high- T_c superconductivity

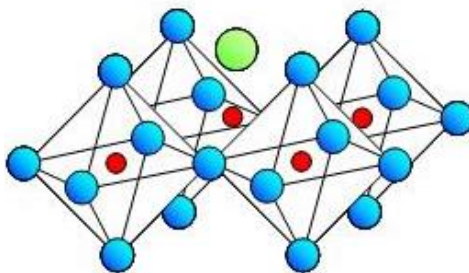
Three families of unconventional superconductor

Iron pnictide (Fe)



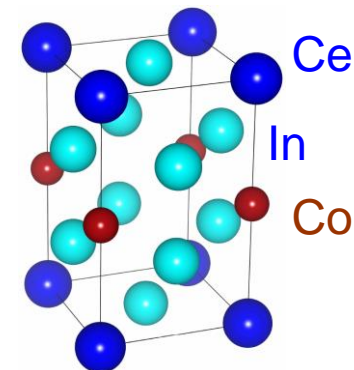
Weakly localized
3*d*-electrons

Cuprate (Cu)



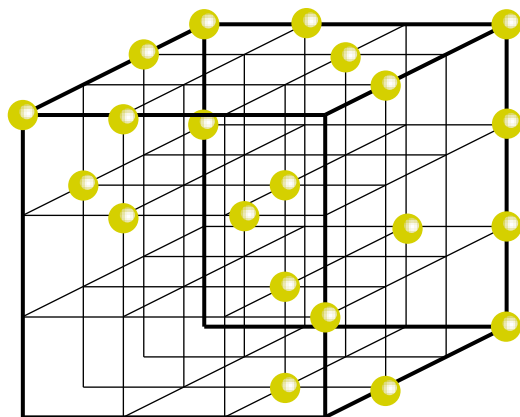
Strongly localized
3*d*-electrons

Heavy fermion compound
(Ce, U)

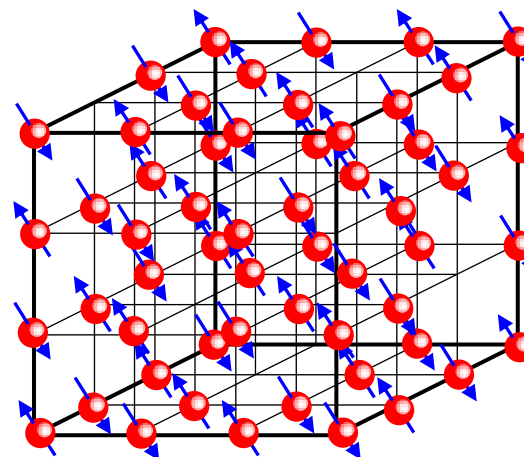


Very strongly localized
4*f*, 5*f* electrons

Weak correlation

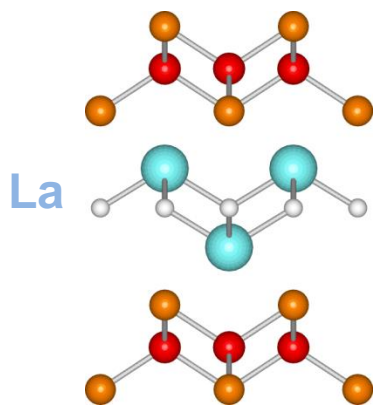


Strong correlation

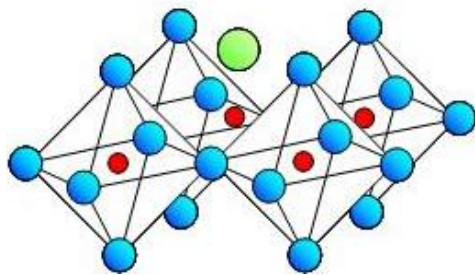


Three classes of unconventional superconductor

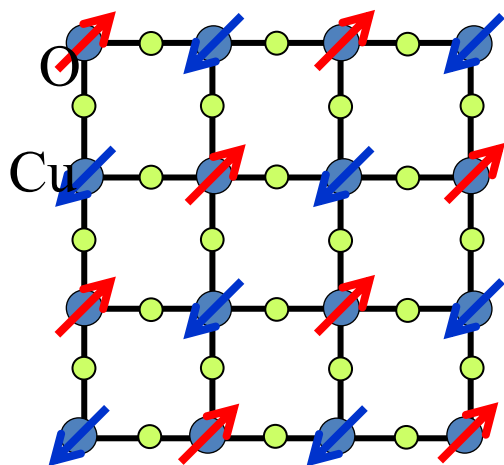
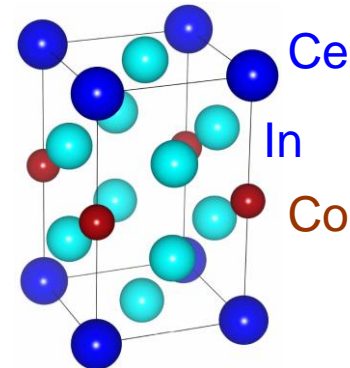
Iron pnictide (Fe)



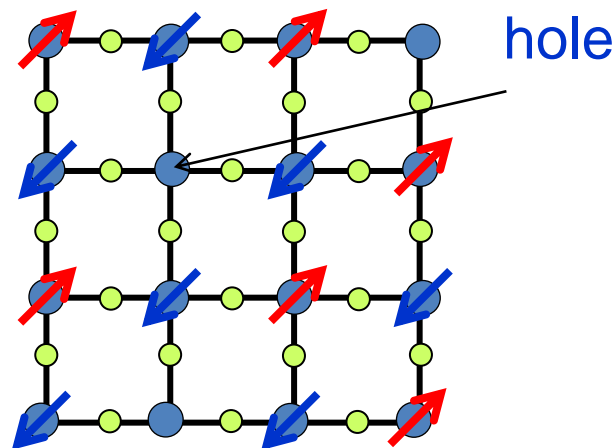
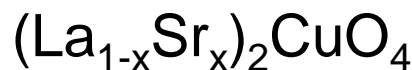
Cuprate (Cu)



Heavy fermion compound (Ce, U)



Mott insulator

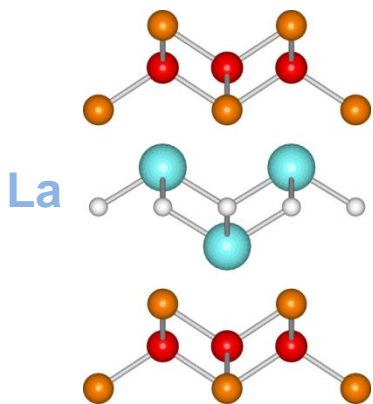


High- T_c superconductor

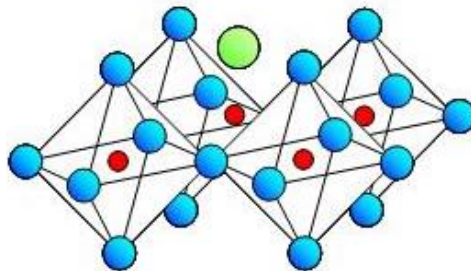
Carrier doping

Three families of unconventional superconductor

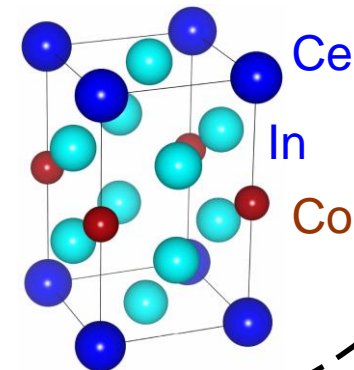
Iron pnictide (Fe)



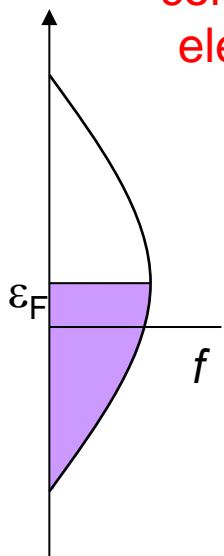
Cuprate (Cu)



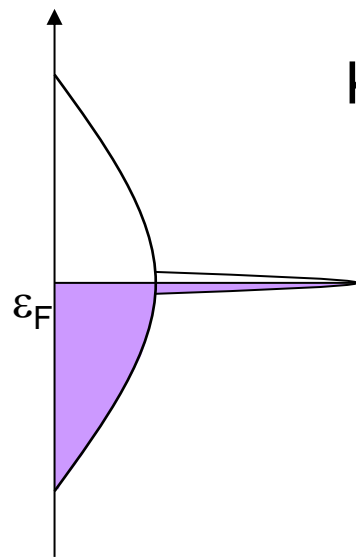
Heavy fermion compound (Ce, U)



Hybridization with conduction electrons

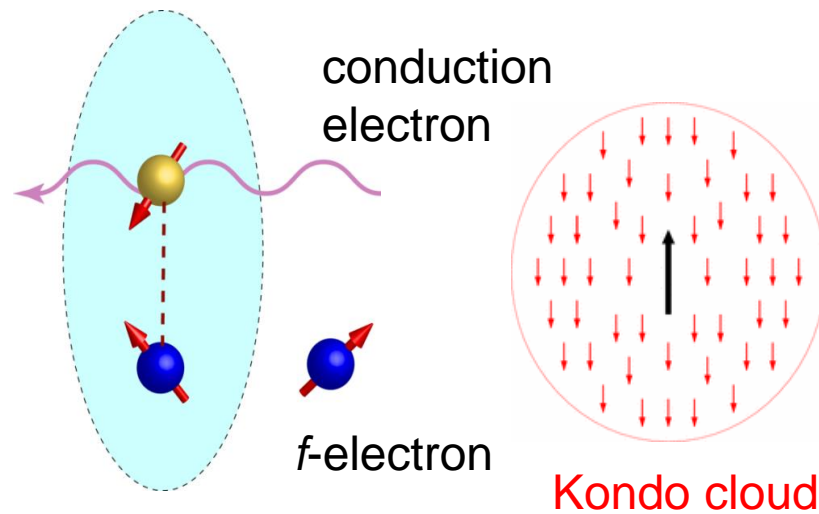


High temperature



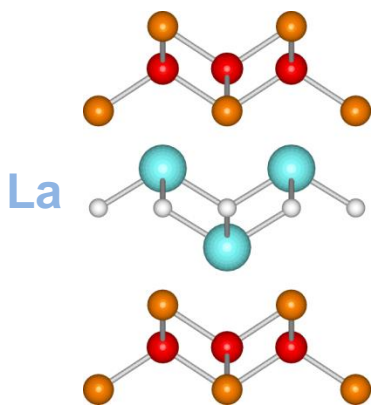
Low temperature

Kondo effect

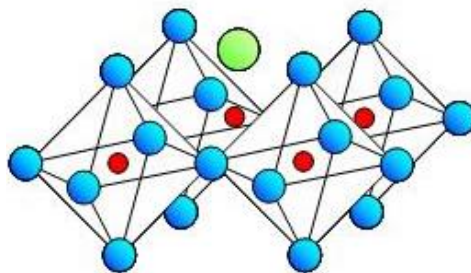


Three families of unconventional superconductor

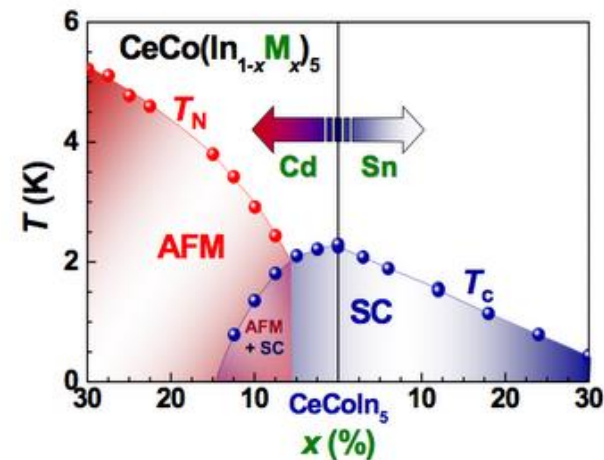
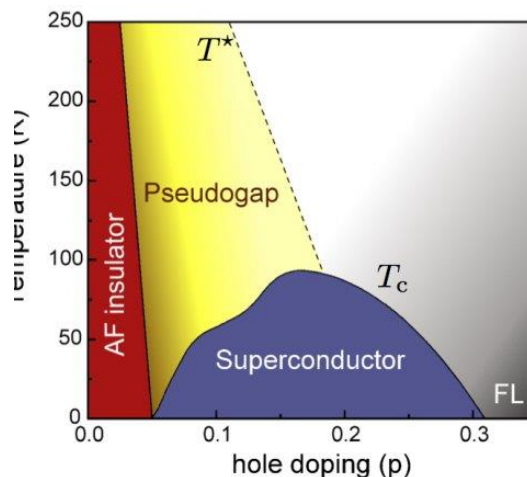
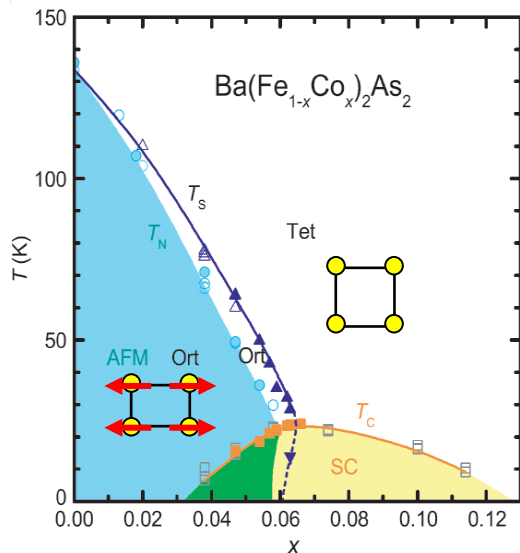
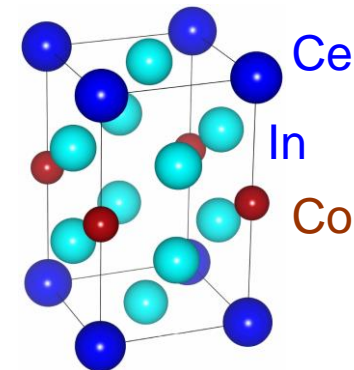
Iron pnictide (Fe)



Cuprate (Cu)



Heavy fermion compound (Ce, U)

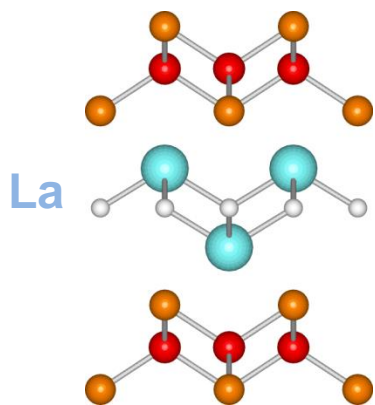


Superconductivity is induced by suppressing a magnetically ordered phase

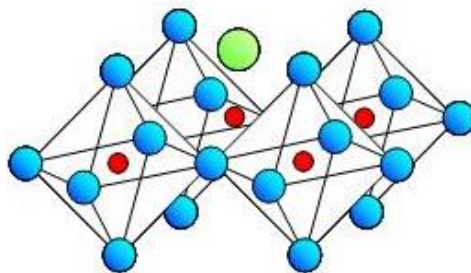
Magnetic fluctuations may bind the Cooper pairs

Three families of unconventional superconductor

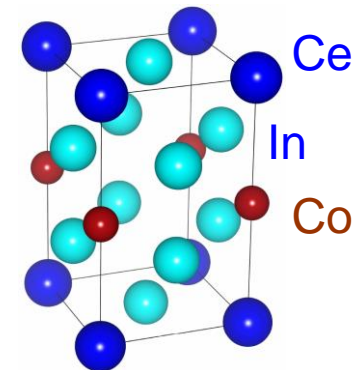
Iron pnictide (Fe)



Cuprate (Cu)

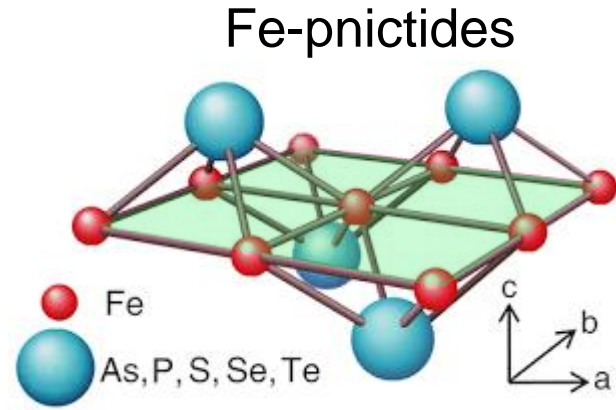
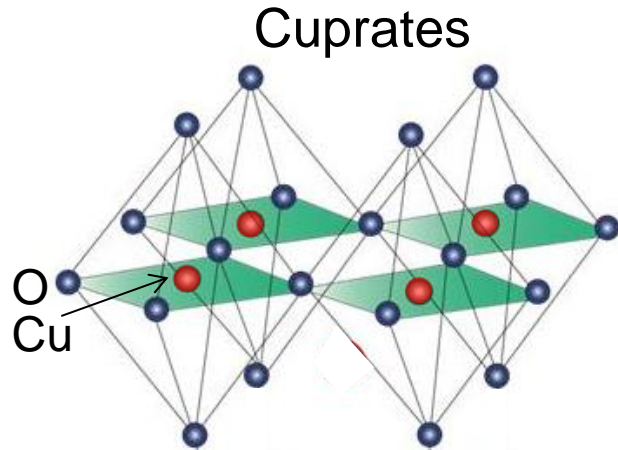


Heavy fermion compound (Ce, U)

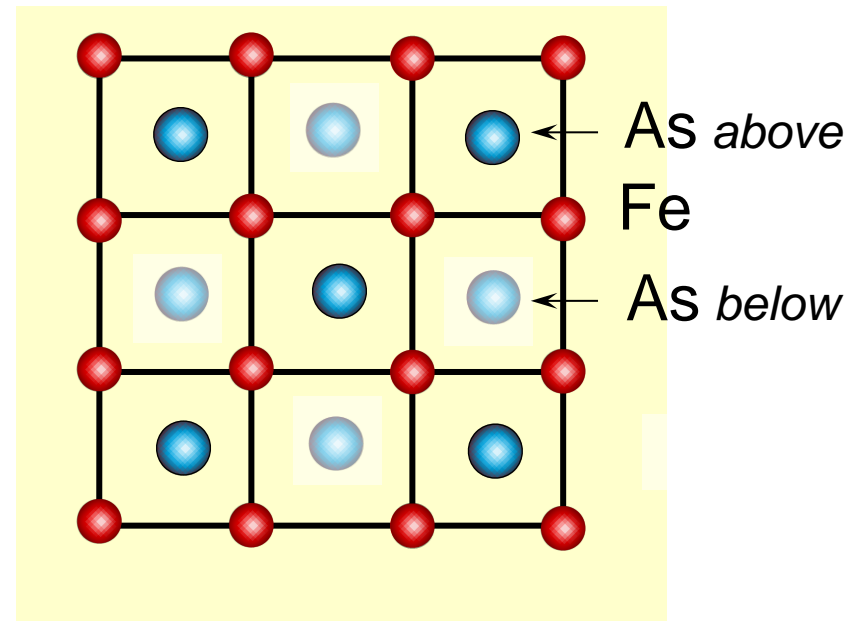
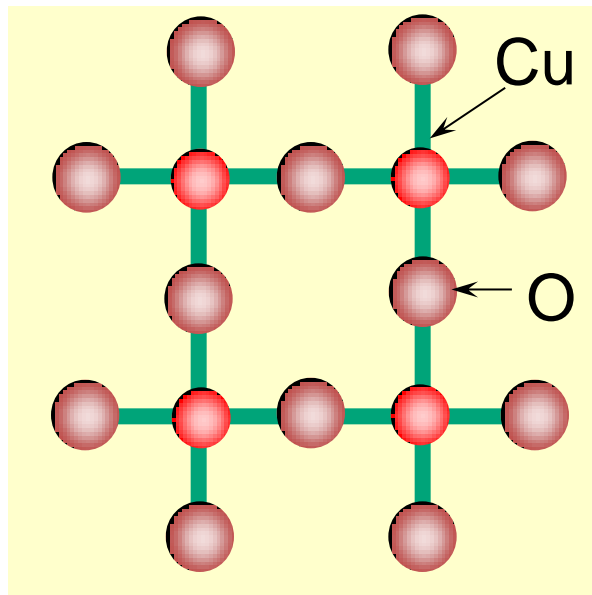


	Pnictide		Cuprate		Heavy Fermion
Electron correlation	strong	<	strong	<	very strong
Fermi surface	simple 2D		Very simple 2D		Complicated 3D
Magnetic structure	simple		simple		complicated
Physics	Multi-orbital		Mott		Kondo

Similarities and differences between cuprates and pnictides

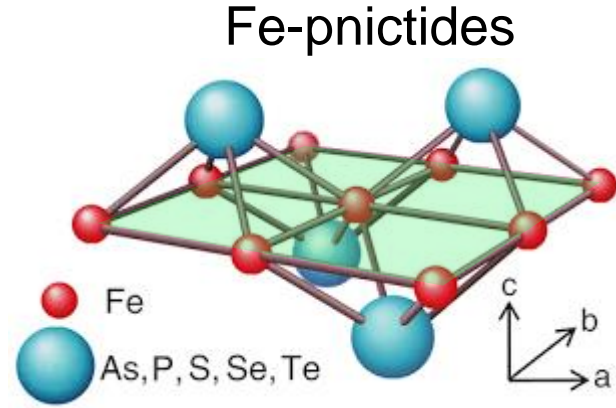
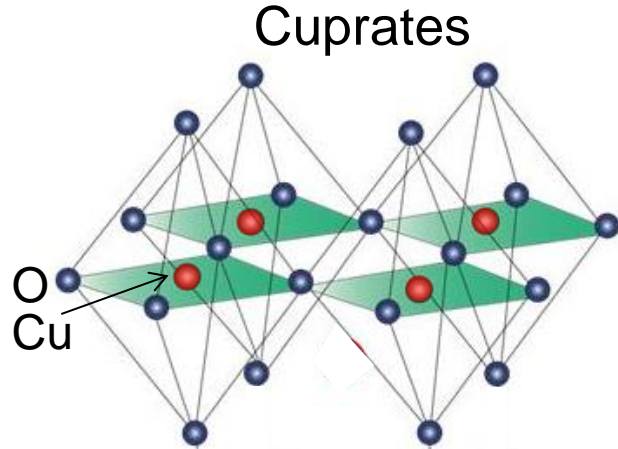


Superconductivity in 2D planes



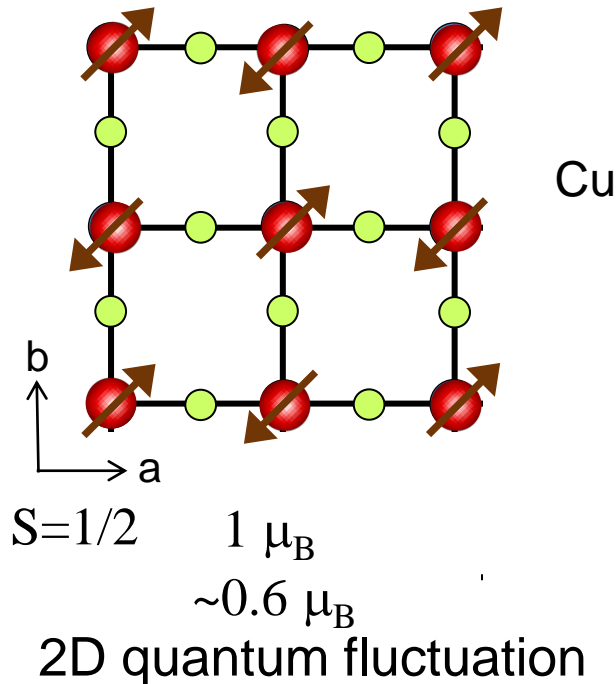
Enhanced fluctuations → suppression of magnetic order

Similarities and differences between cuprates and pnictides

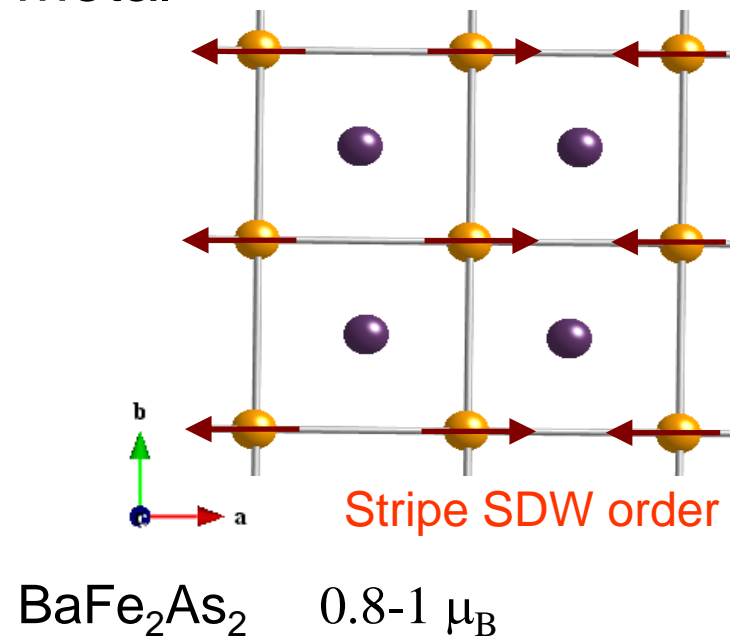


Parent compound

AFM insulator

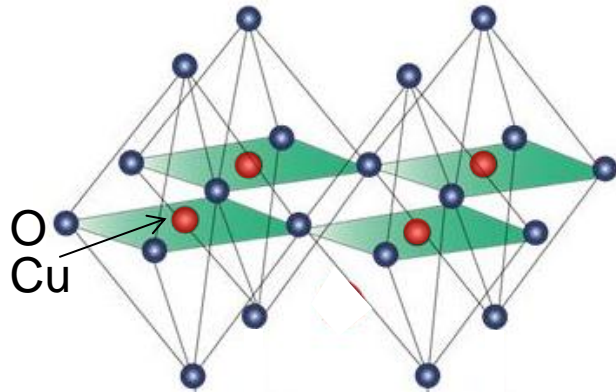


SDW metal

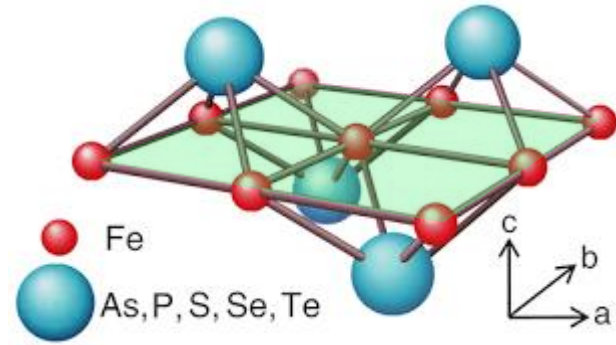


Similarities and differences between cuprates and pnictides

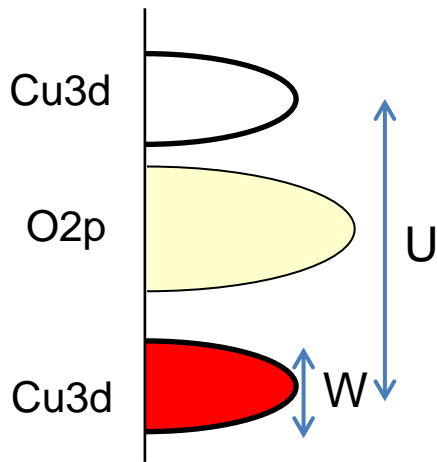
Cuprates



Fe-pnictides



Parent compound

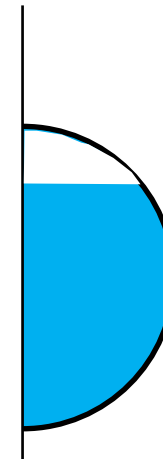


U : Coulomb $\sim 8\text{eV}$

W : Band width $\sim 3\text{eV}$

Strong electron-electron correlation

Mott insulator



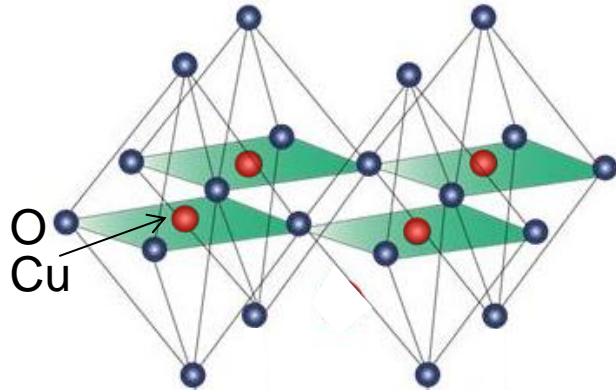
$U \sim W \sim 2\text{-}3\text{ eV}$

Intermediate correlation

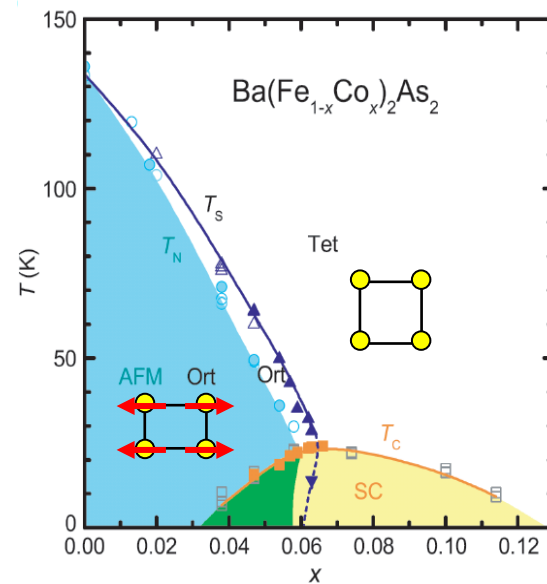
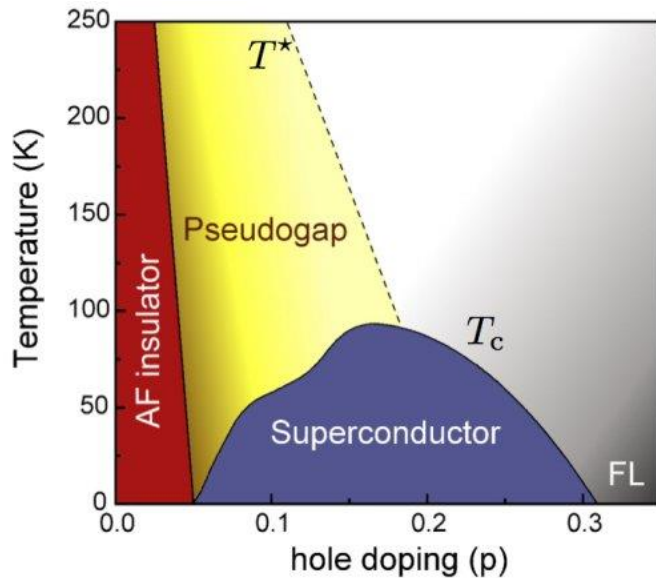
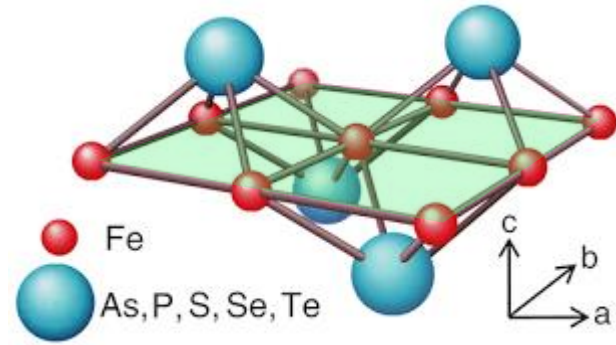
Spin density wave (SDW) metal

Similarities and differences between cuprates and pnictides

Cuprates



Fe-pnictides

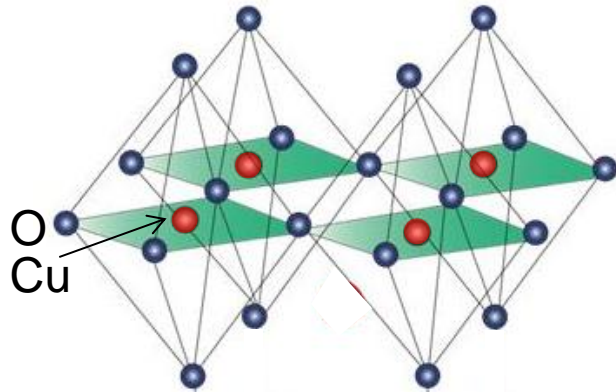


Superconductivity occurs in the vicinity of magnetic order

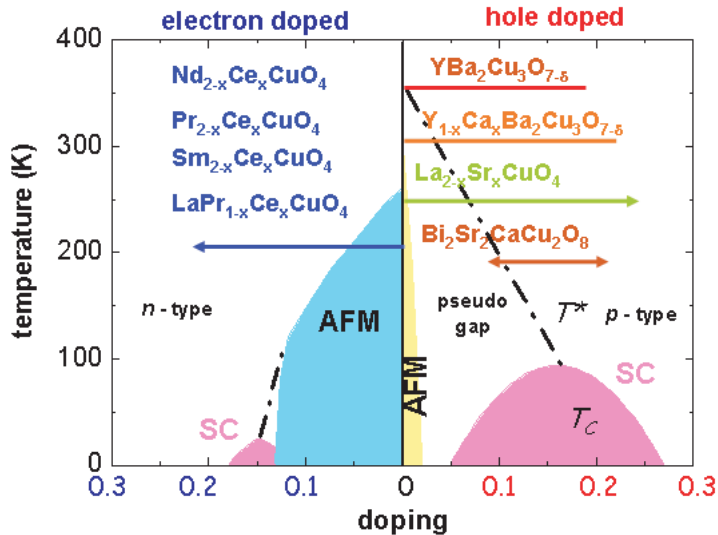
In Fe-pnictides, structural (T_s) and AFM transition (T_N) lines follow closely each other

Similarities and differences between cuprates and pnictides

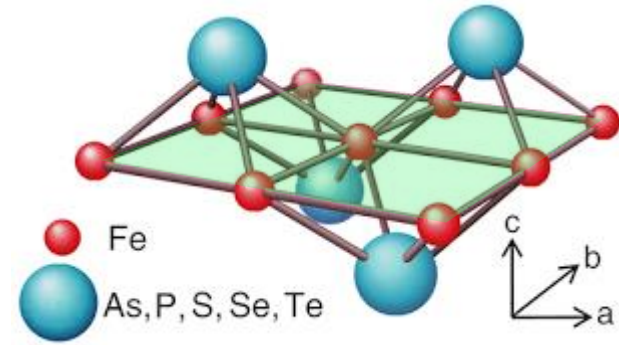
Cuprates



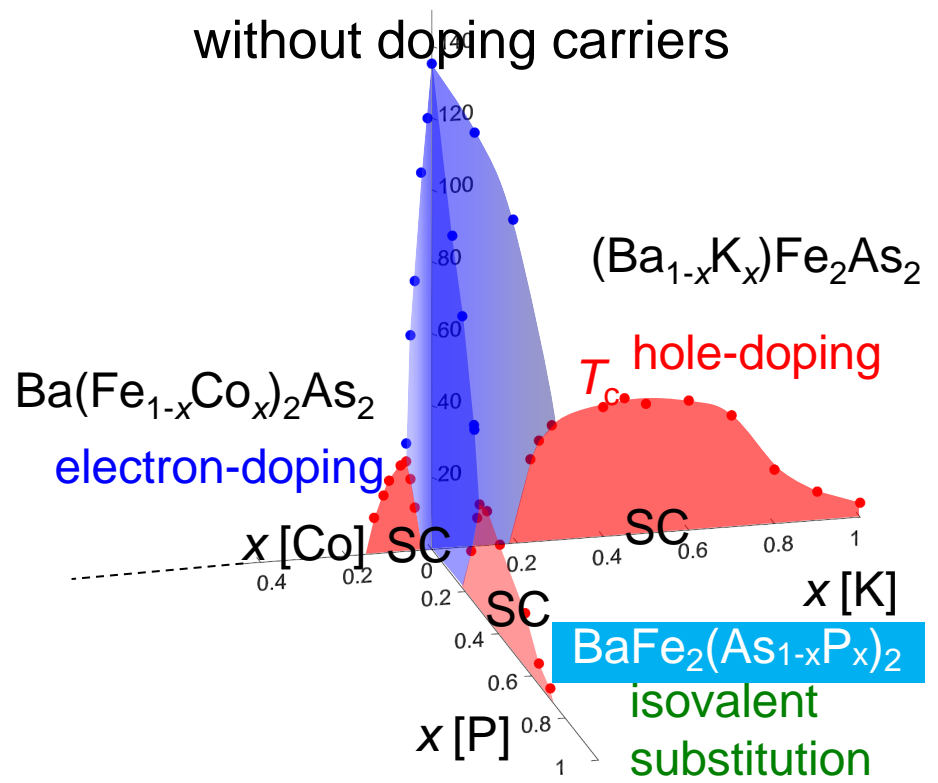
Superconductivity induced by doping holes or electrons



Fe-pnictides

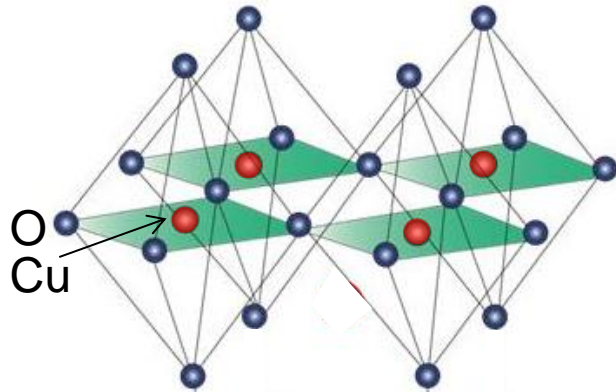


Ground state can be tuned without doping carriers

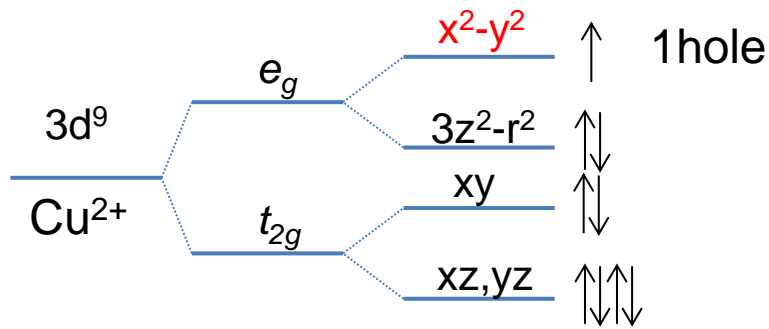
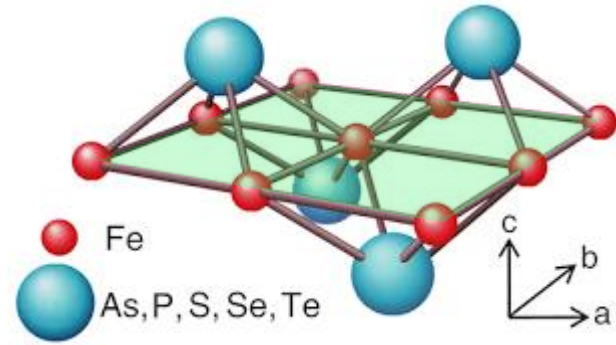


Similarities and differences between cuprates and pnictides

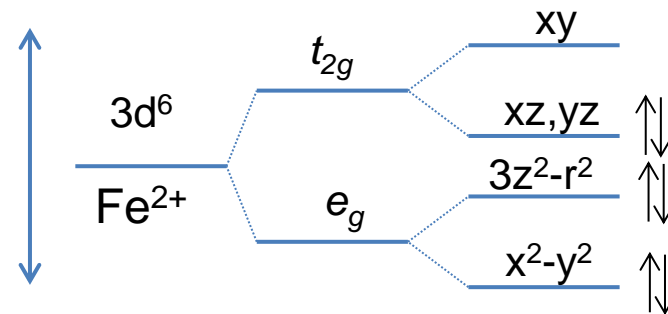
Cuprates



Fe-pnictides



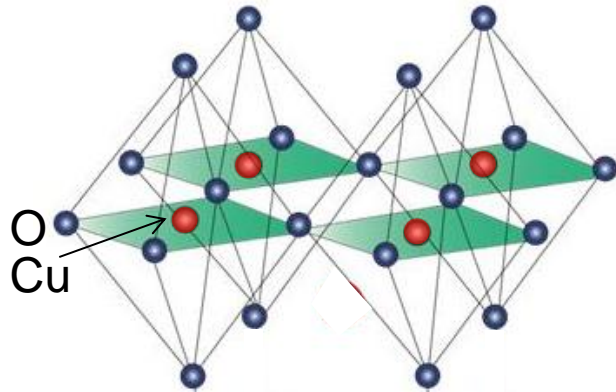
Large crystal field $\sim 2-3$ eV



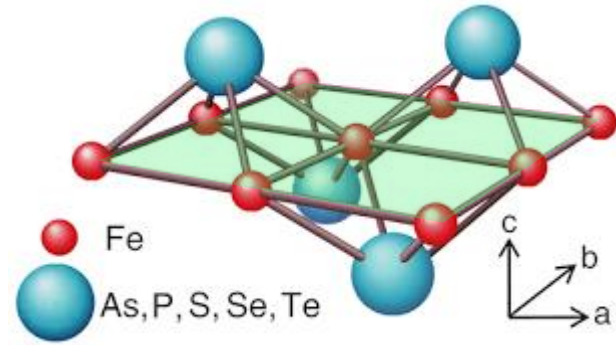
Small crystal field (~ 500 meV)

Similarities and differences between cuprates and pnictides

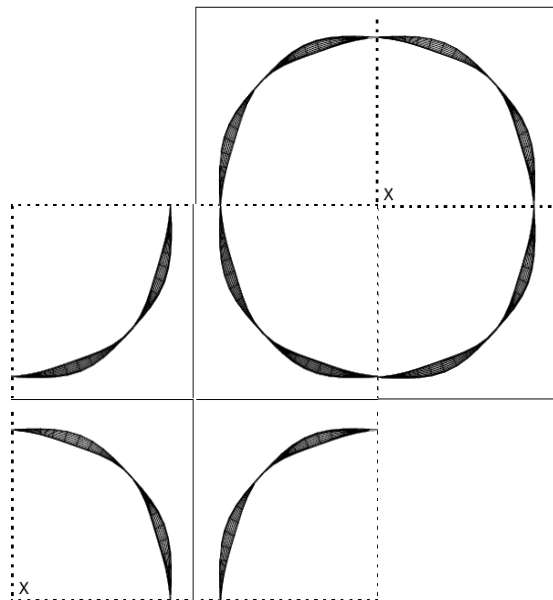
Cuprates



Fe-pnictides

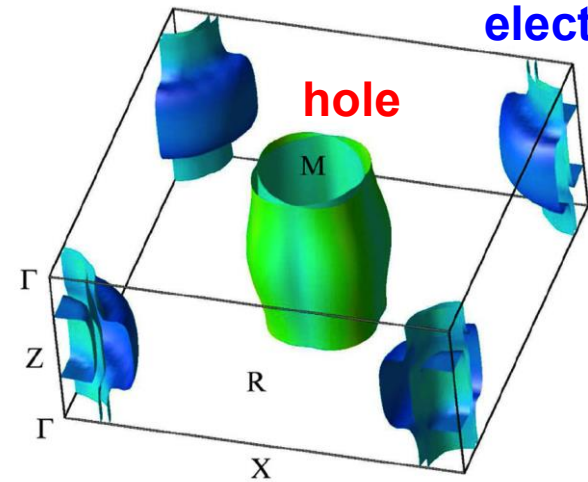


hole



Only hole band

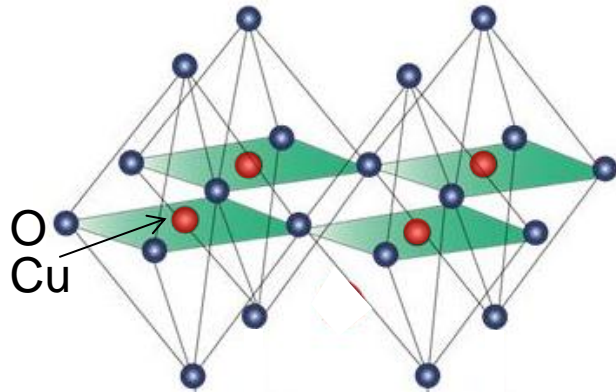
electron



Well separated hole and electron bands

Similarities and differences between cuprates and pnictides

Cuprates

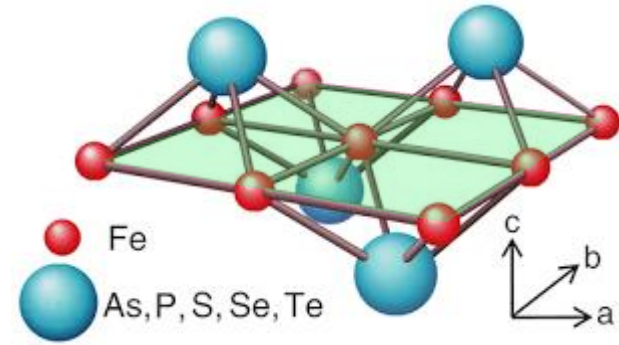


One orbital

$$x^2-y^2$$

Mainly three orbitals

Fe-pnictides



$$xz+yz$$

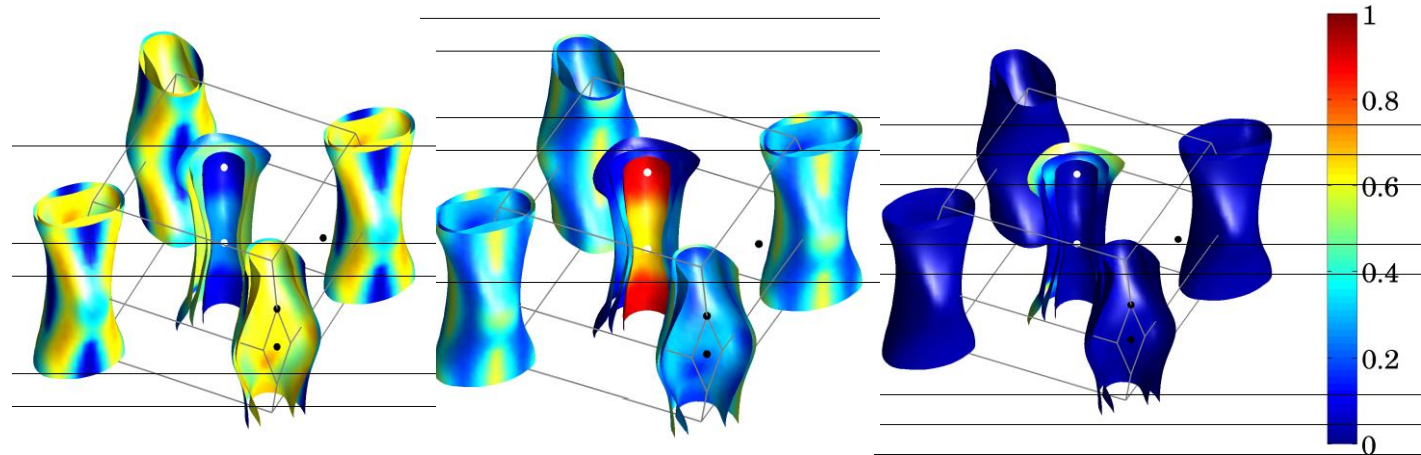
$$xy$$

$$3z^2-r^2$$



$Tl_2Ba_2CuO_{6+\delta}$

N. E. Hussey *et al.*,
Nature (2003).



$BaFe_2As_2$

鉄系高温超伝導体

銅酸化物、重い電子系との比較

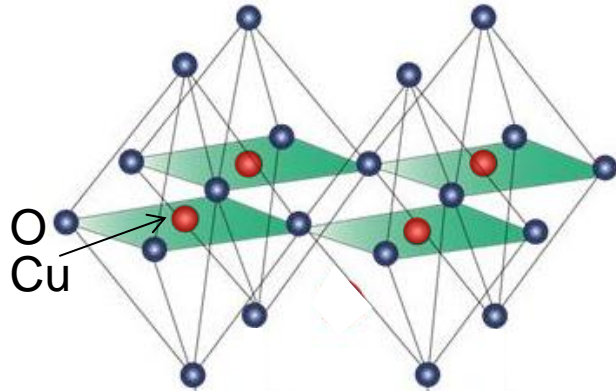
超伝導ギャップ構造

量子臨界点

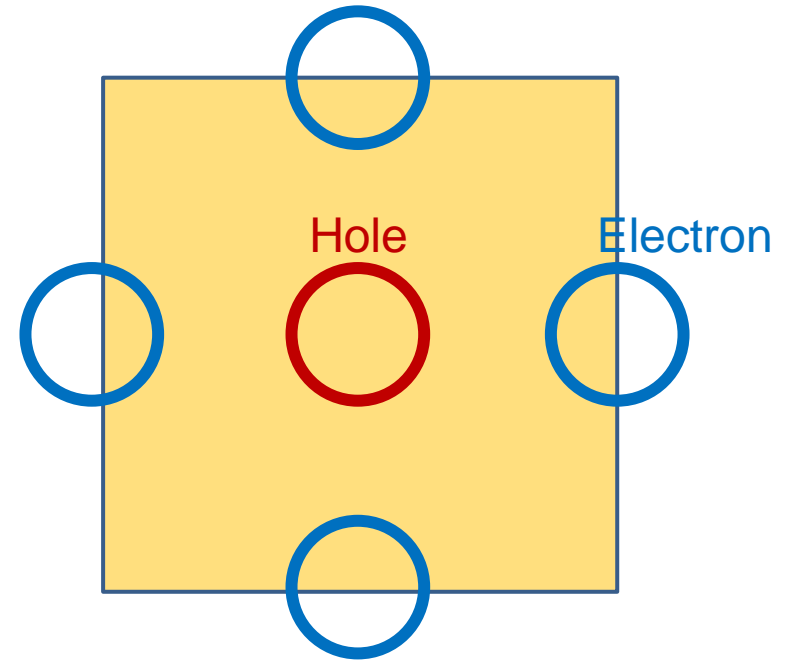
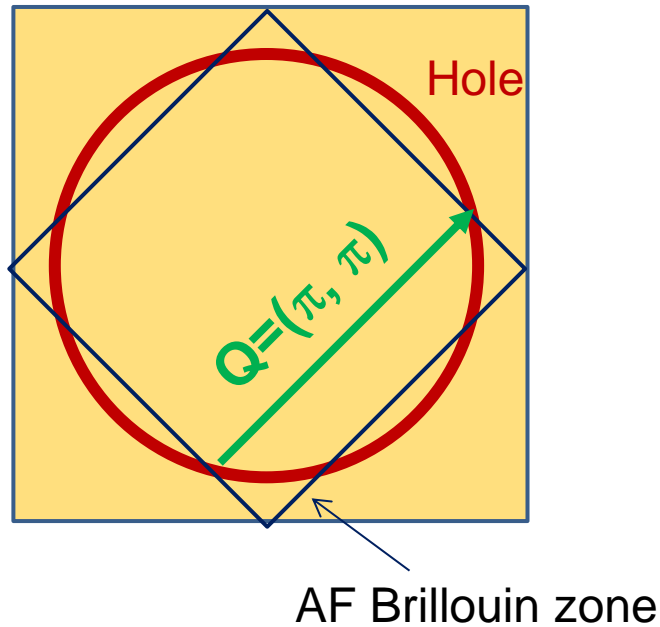
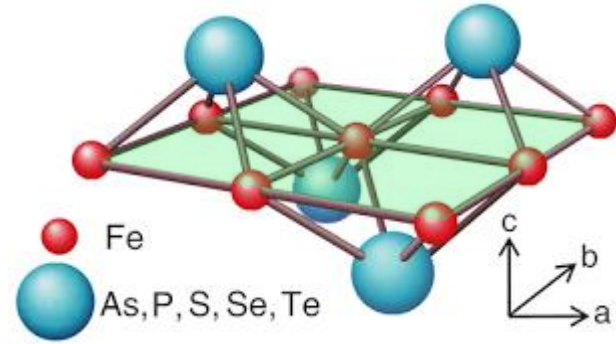


Similarities and differences between cuprates and pnictides

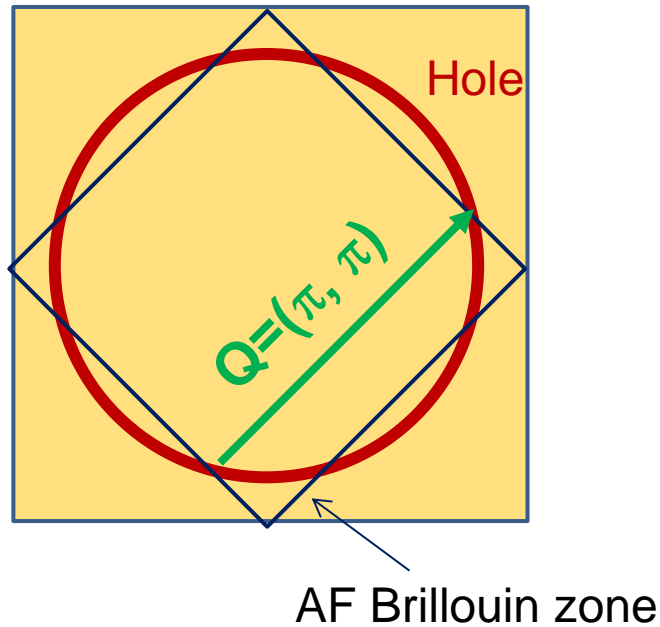
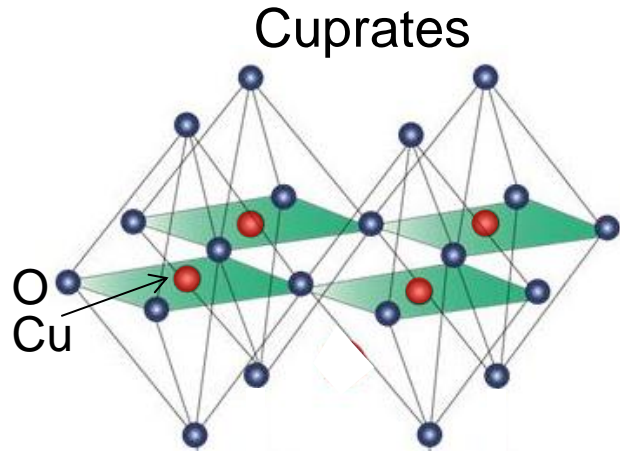
Cuprates



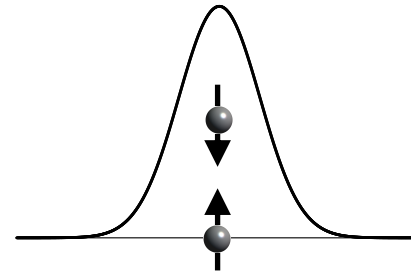
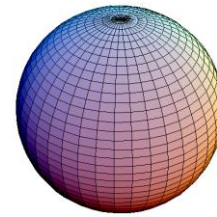
Fe-pnictides



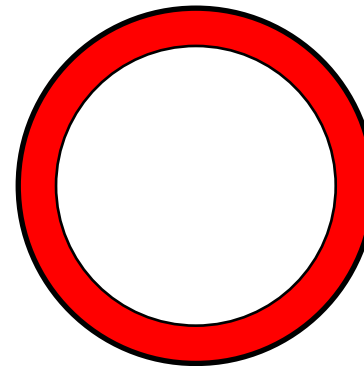
Similarities and differences between cuprates and pnictides



s-wave

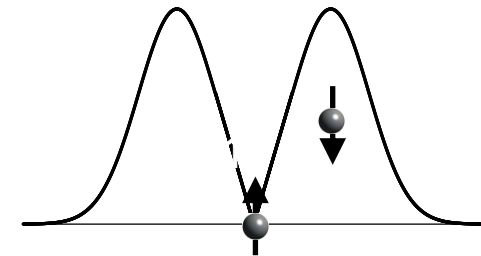
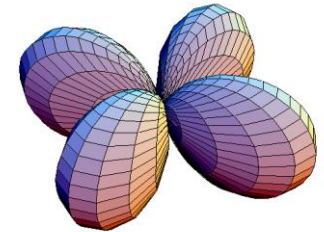


Attractive

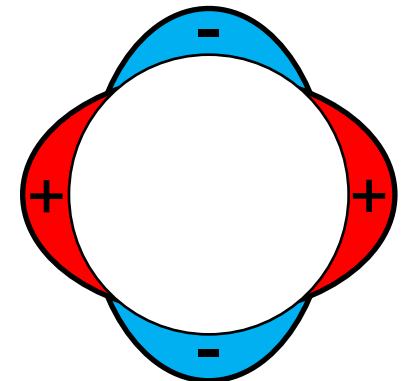


$\Delta = \text{const.}$

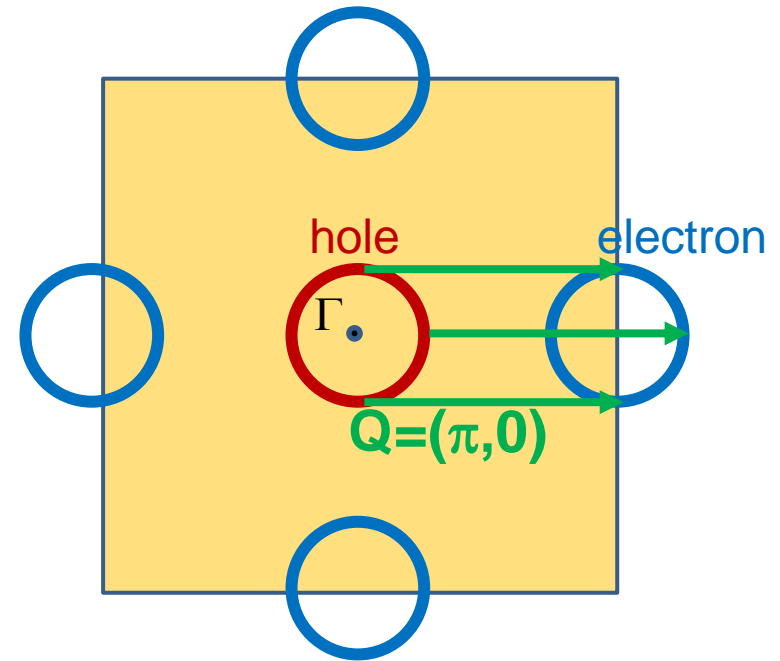
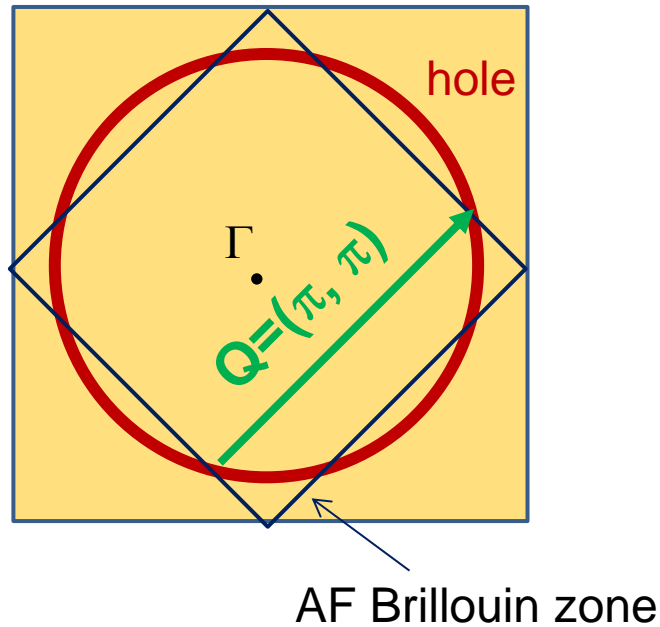
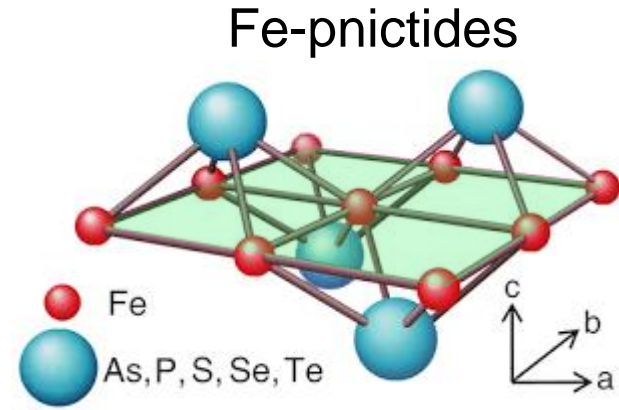
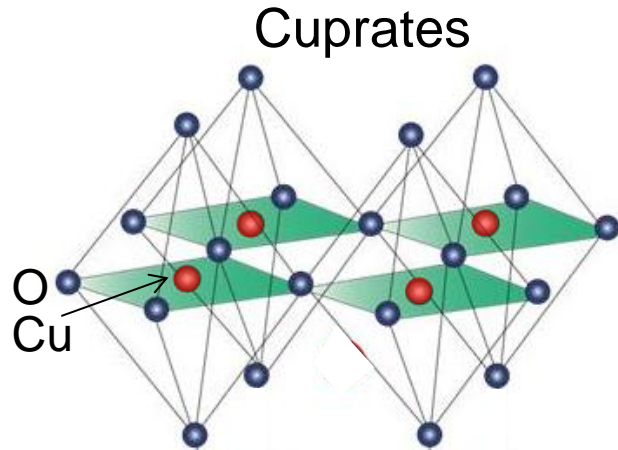
d-wave



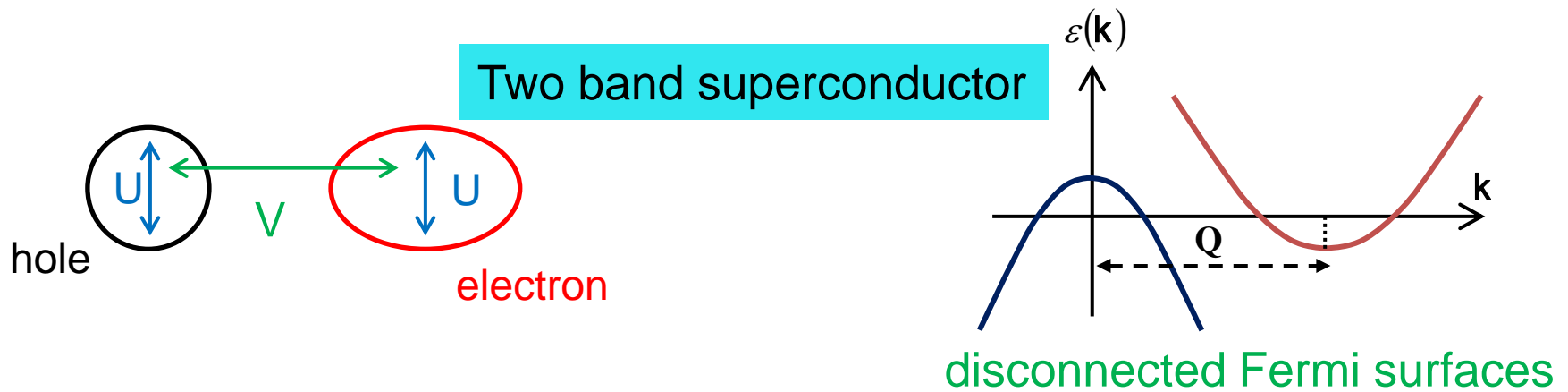
Onsite repulsive



Similarities and differences between cuprates and pnictides



Iron pnictides: candidate for the SC state



Gap equation

$$\Delta_e = -V \Delta_h \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q} - U \Delta_e \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q}$$

$$\Delta_h = -V \Delta_e \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q} - U \Delta_h \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q}$$

$$U = 0$$

$$|V|N(0) \ln \frac{W}{T_c} = 1$$

At T_c :

W : band width

$$\begin{pmatrix} \Delta_e \\ \Delta_h \end{pmatrix} = A \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} \Delta_e \\ \Delta_h \end{pmatrix} \quad A = \pm 1$$

$$V > 0 \quad A = +1 \quad \Delta_e = -\Delta_h \quad \text{Sign change} \quad S_{\pm}$$

repulsive

$$V < 0 \quad A = -1 \quad \Delta_e = \Delta_h \quad \text{No sign change} \quad S_{++}$$

attractive

Superconducting gap structure of iron pnictides

Gap structure is closely related to the pairing interaction

Full gap or nodal?

Full gap

Does the gap change sign between the hole and electron pockets?

Is the major pairing interaction repulsive or attractive?

Nodal

⇒ Presence of repulsive interaction.

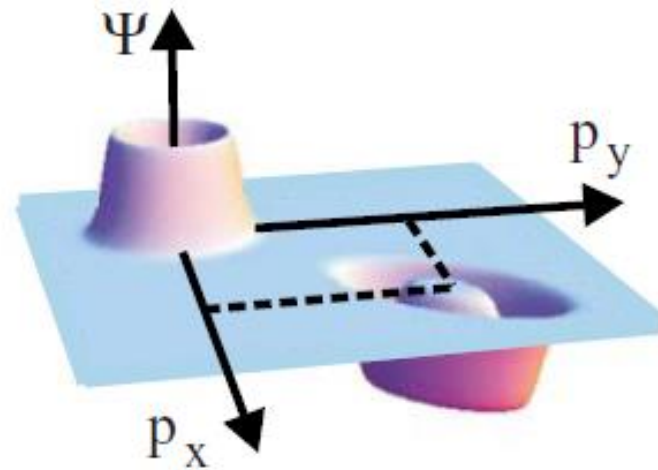
Is the node accidental or symmetry protected?

Accidental : presence of two (or more) competing pairing interactions

Iron pnictides: candidate for the SC state

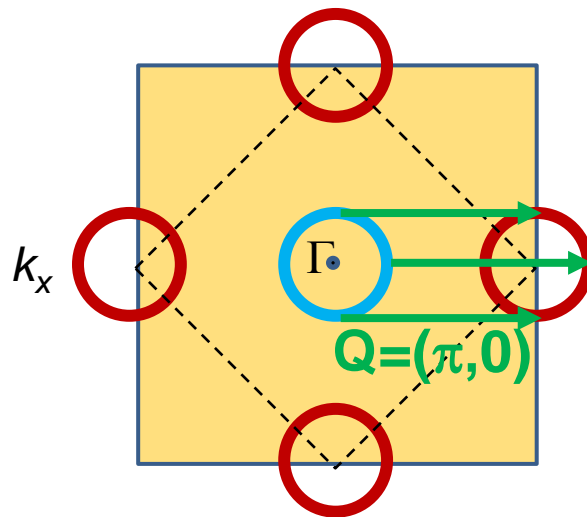
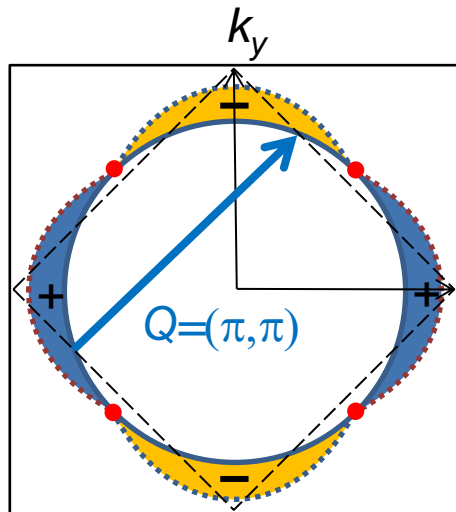
- Pairing due to purely **repulsive** electronic interaction (enhanced by spin fluctuations)

$$V > 0$$



$$S_{+-}$$

cf. *d*-wave cuprate



- I. I. Mazin *et al.*, PRL **101**, 057003 (2008).
- K. Kuroki *et al.*, PRL **101**, 087004 (2008).
- & PRB **79**, 224511 (2009).
- A. V. Chubkov *et al.*, PRB **80**, 140515(R) (2009).
- S. Graser *et al.*, NJP **11**, 025016 (2009).
- H. Ikeda, PRB **81**, 054502 (2010).
- K. Seo *et al.*, PRL **101**, 206404 (2008).
- F. Wang *et al.*, PRL **102**, 047005 (2009).

⋮

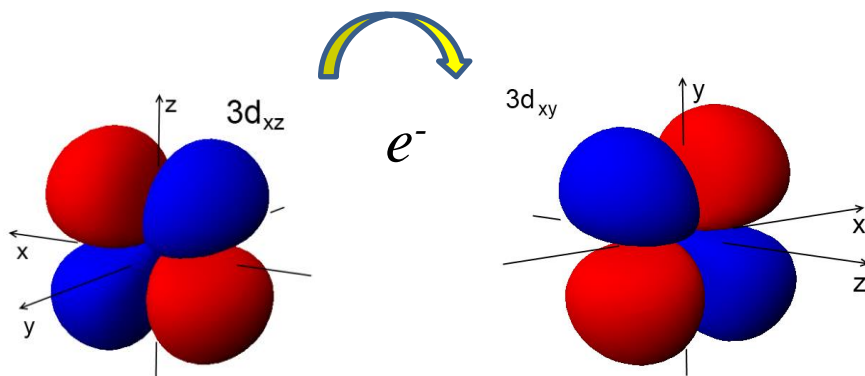
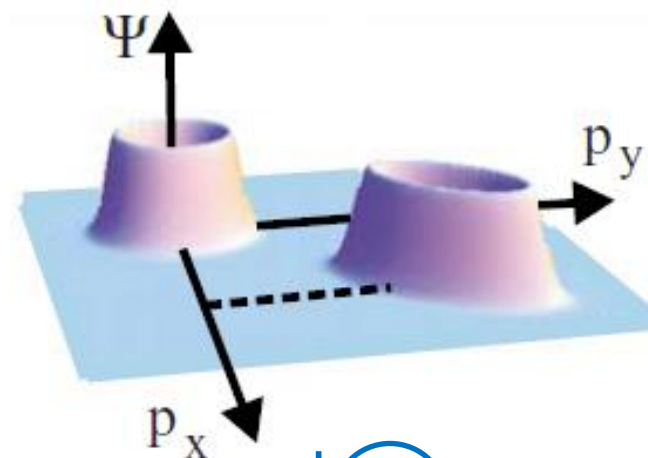
Iron pnictides: candidate for the SC state

- Pairing due to **attractive** interaction caused by charge/orbital fluctuations.

$$S_{++}$$

$$V < 0$$

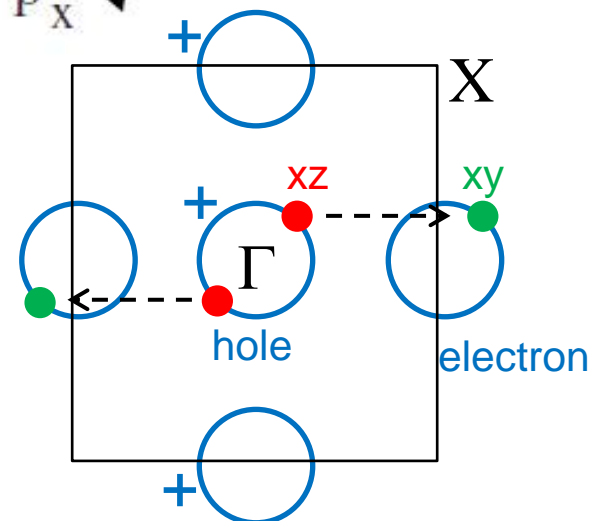
Orbital fluctuations
(Quadrupole fluctuation)



Charge up

Charge down

Occupation number of each orbit
at each Fe site fluctuates

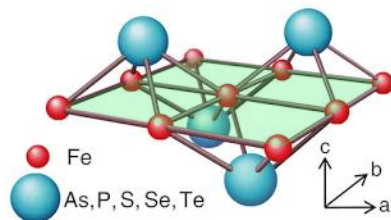


H. Kontani & S. Onari, PRL **104**, 157001 (2010).
 F. Kruger *et al.*, PRB **79**, 054504 (2009).
 Y. Yanagi *et al.*, PRB **81**, 054518 (2010).

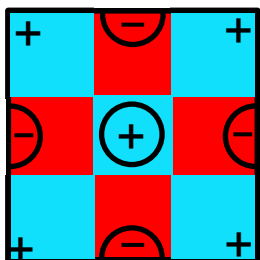
Iron pnictides: candidate for the SC state

S_{+-}

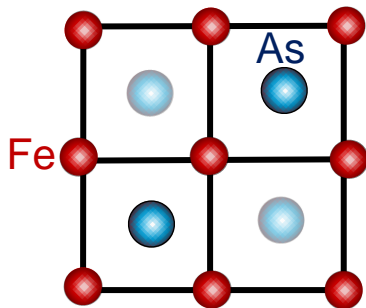
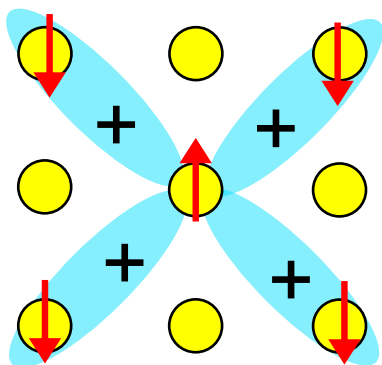
Fe-pnictides



k -space (repulsive)



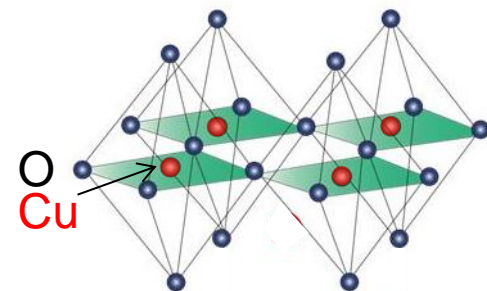
r -space



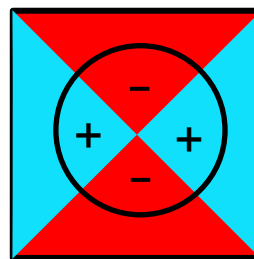
$$\Delta(\cos k_x \cos k_y)$$

$d_{x^2-y^2}$

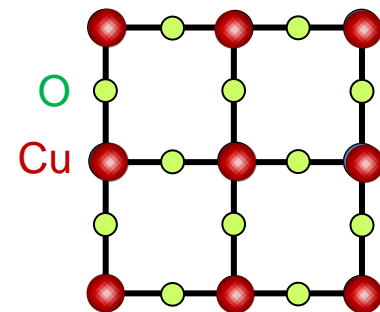
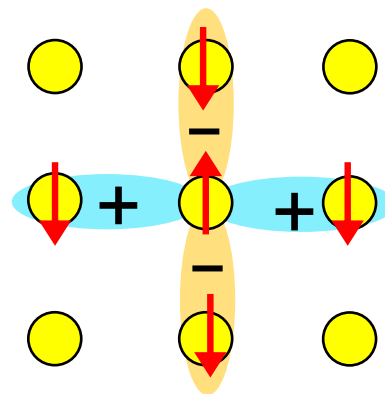
Cuprates



k -space (repulsive)



r -space

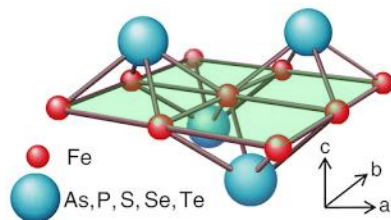


$$\Delta(\cos k_x - \cos k_y)$$

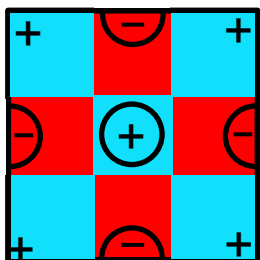
Iron pnictides: candidate for the SC state

S_{+-}

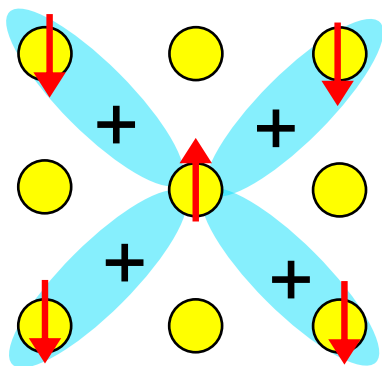
Fe-pnictides



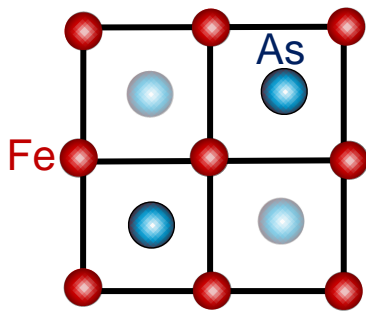
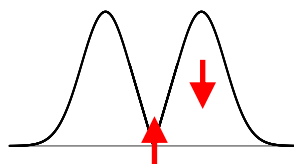
k -space (repulsive)



r -space

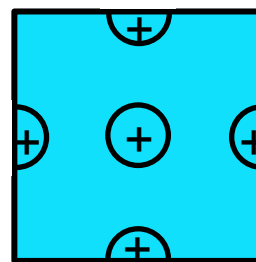


$$\Delta(\cos k_x \cos k_y)$$

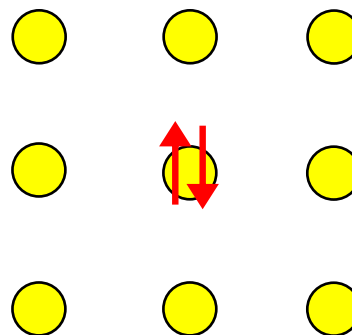


S_{++}

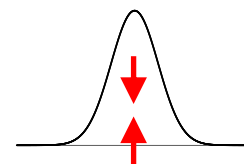
k -space (attractive)



r -space



$$\Delta$$



Iron pnictides: candidate for the SC state



Chicken or the egg?

Spin fluctuations or orbital fluctuations?

AF I

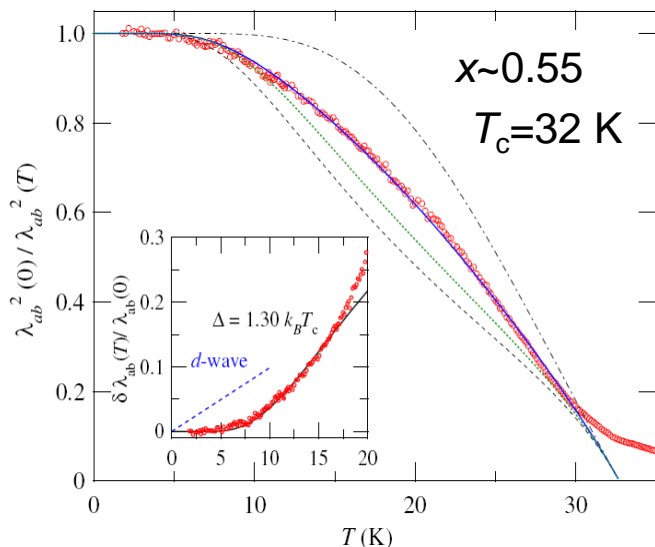
ng

Full gap or nodal?

Full gap superconductivity

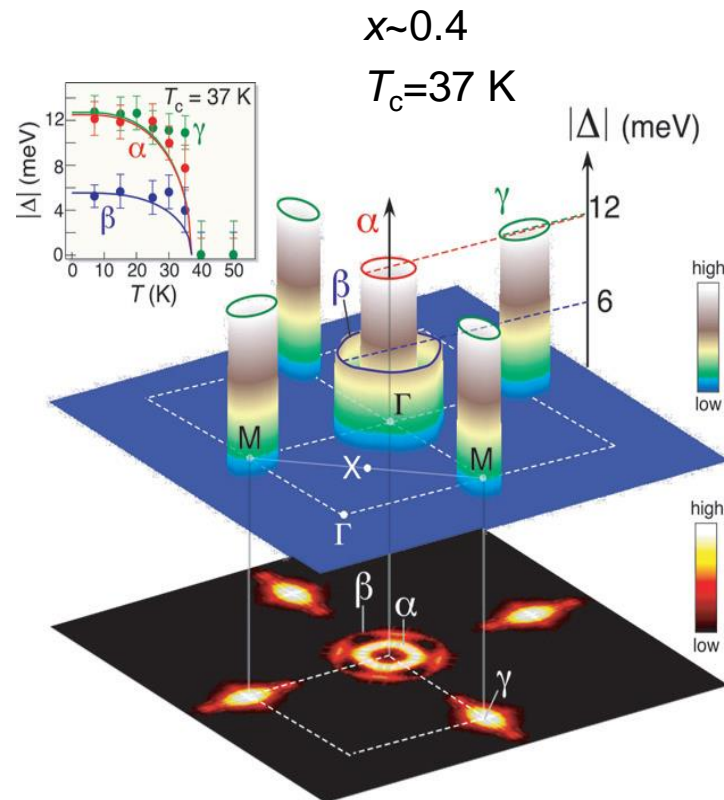
Penetration depth

hole doped $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$



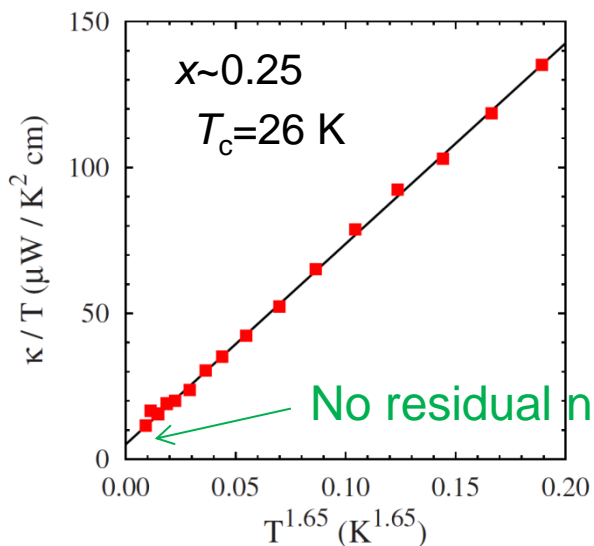
K. Hashimoto, *et al.*, PRL **102**, 027001 (2009).

ARPES



H. Ding *et al.*, EPL **83**, 47001 (2008).

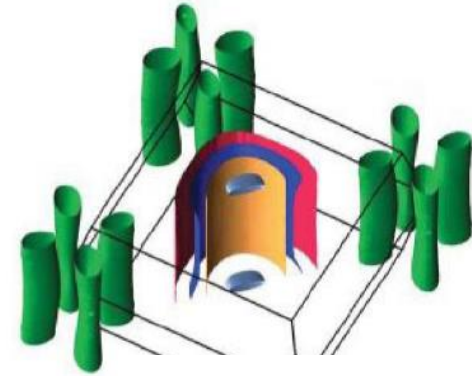
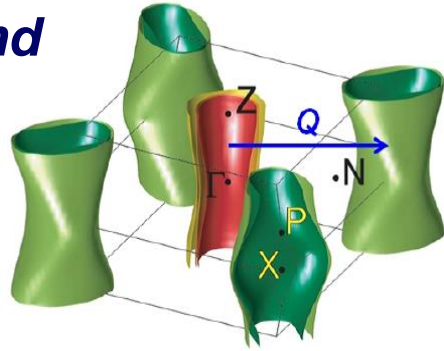
Thermal conductivity



X.G. Luo *et al.* PRB **80**, 140503 (2009).

Superconductivity in BaFe₂As₂ systems

Parent compound
BaFe₂As₂
(AF Metal)



KFe₂As₂ ($T_c = 3$ K)

(Ba_{1-x}K_x) $\gamma \sim 100$ mJ/K²mol

($T_c^{opt} \sim 38$ K) no electron pockets

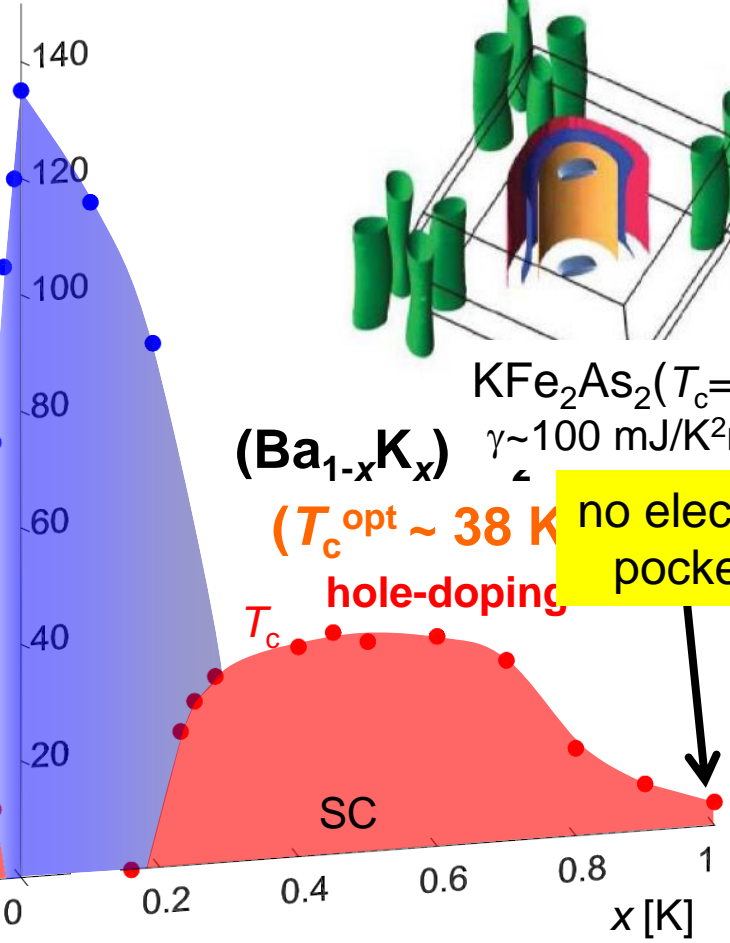
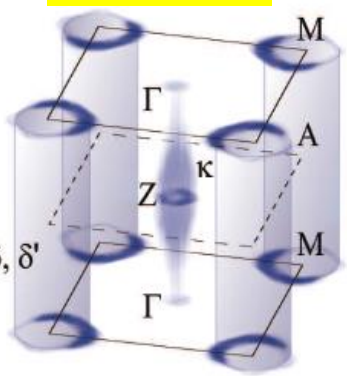
Ba(Fe_{1-x}Co_x)₂As₂

K_xFe_{2-y}Se₂ ($T_c^{opt} \sim 24$ K)

($T_c^{opt} \sim 31$ K)

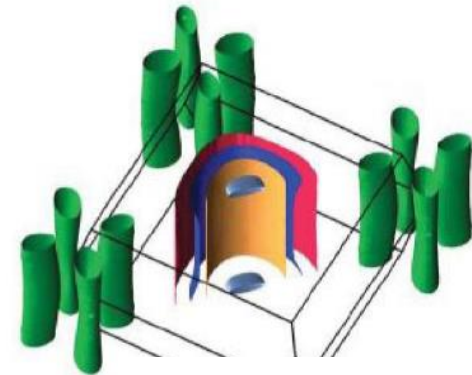
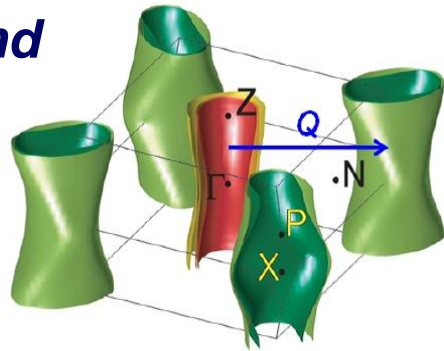
electron-doping

no hole pockets



Superconductivity in BaFe₂As₂ systems

Parent compound
BaFe₂As₂
(AF Metal)



KFe₂As₂ ($T_c = 3$ K)

(Ba_{1-x}K_x) $\gamma \sim 100$ mJ/K²mol

($T_c^{opt} \sim 38$ K) no electron pockets

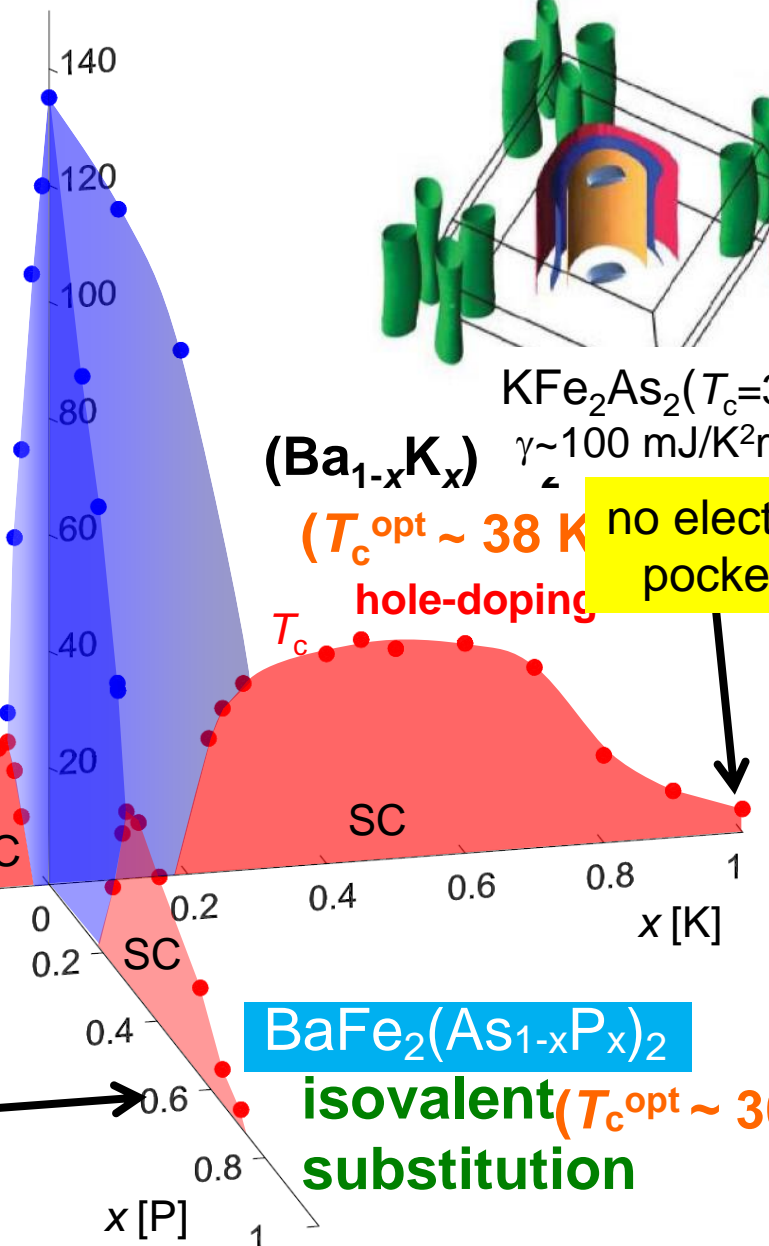
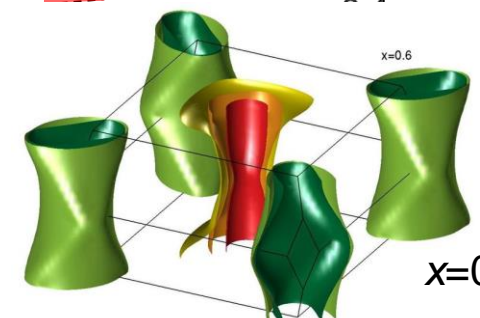
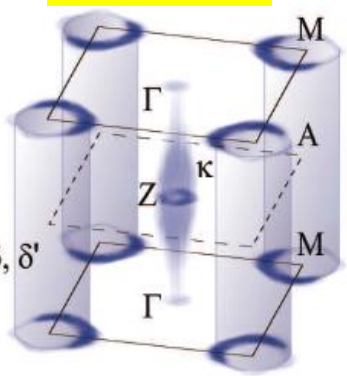
Ba(Fe_{1-x}Co_x)₂As₂

K_xFe_{2-y}Se₂ ($T_c^{opt} \sim 24$ K)

($T_c^{opt} \sim 31$ K)

electron-doping

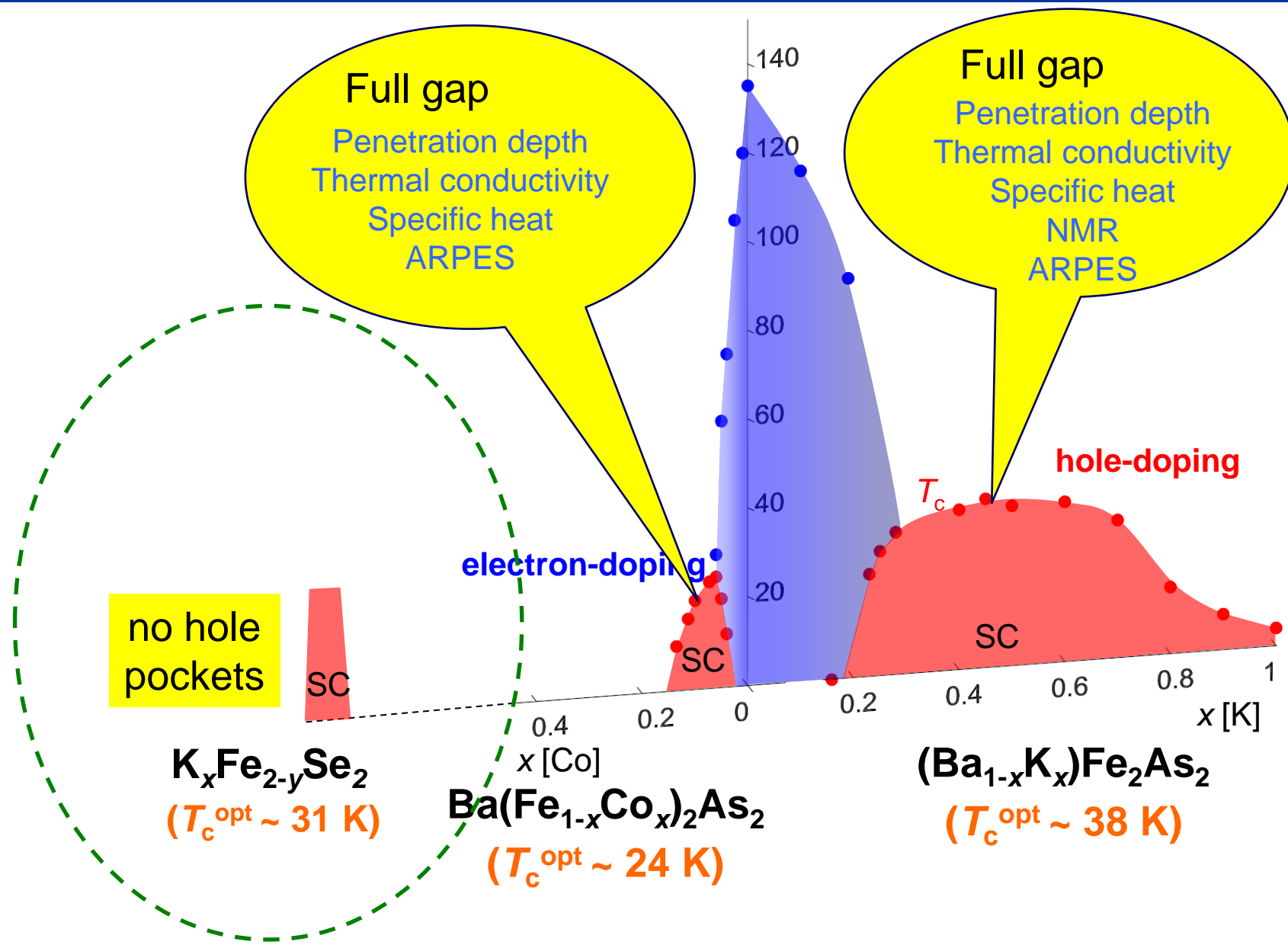
no hole pockets



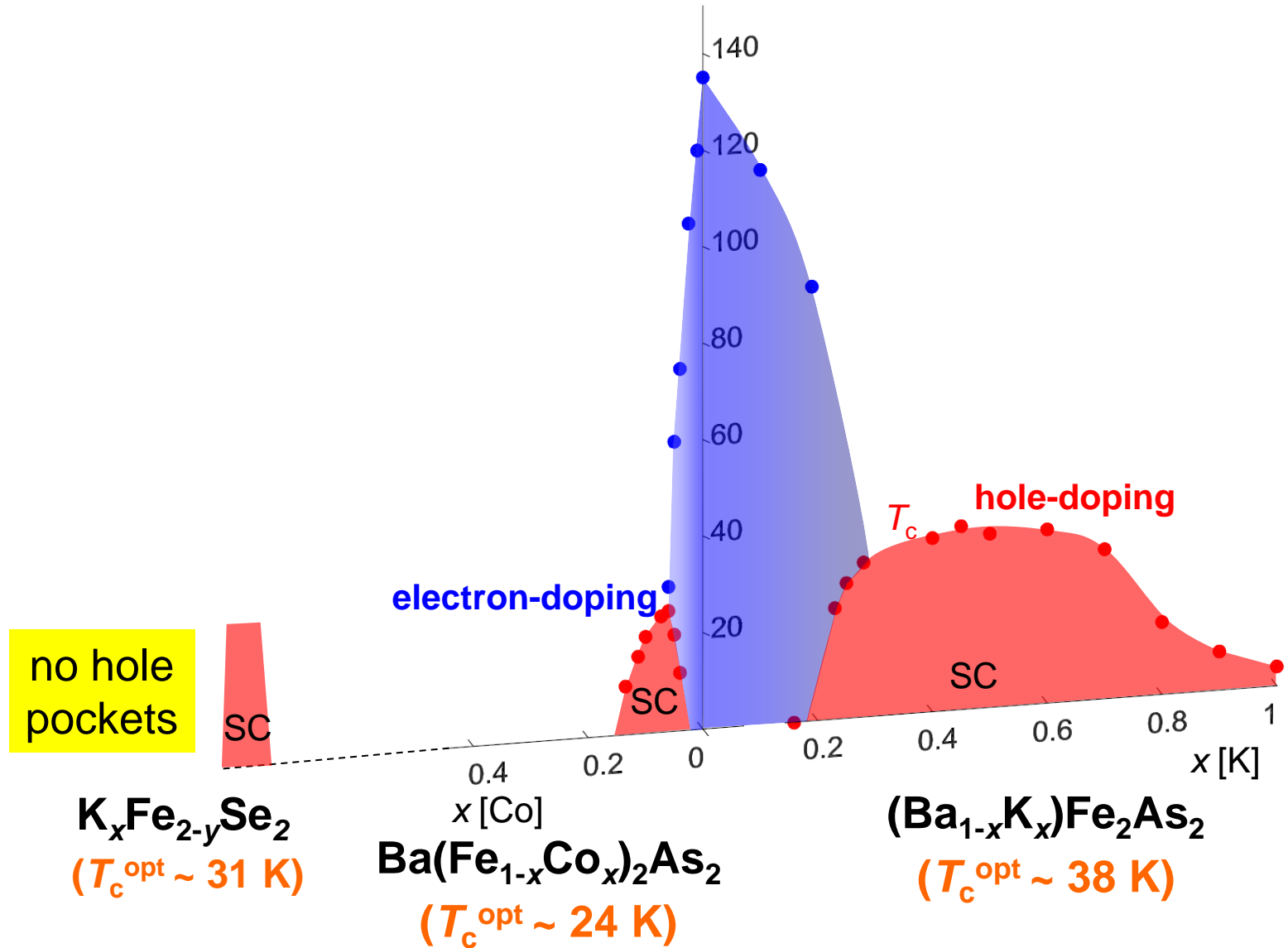
BaFe₂(As_{1-x}P_x)₂
isovalent ($T_c^{opt} \sim 30$ K)
substitution

Ground state can be tuned without doping carriers

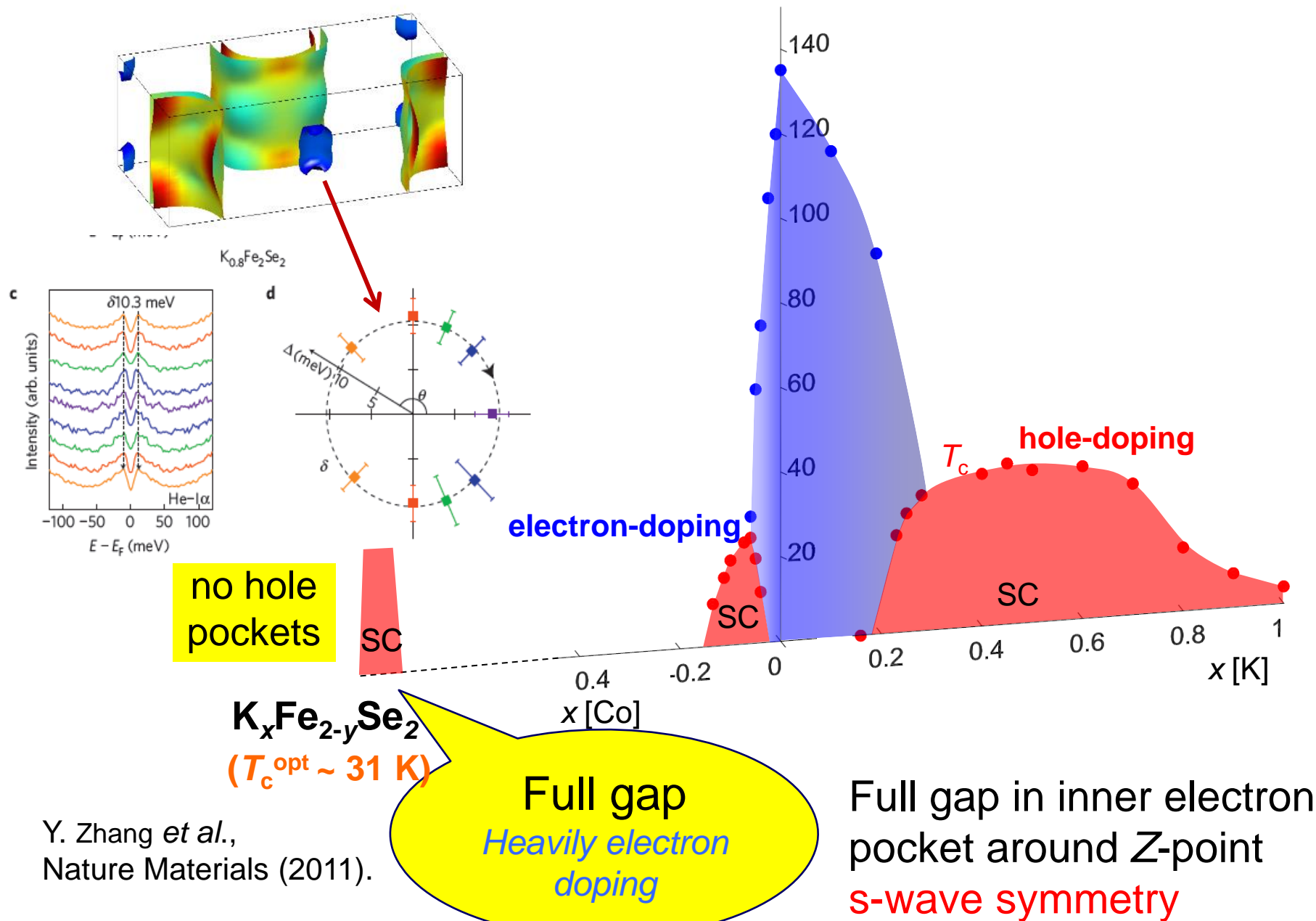
Superconducting gap structure of BaFe₂As₂ systems



Superconducting gap structure of BaFe₂As₂ systems

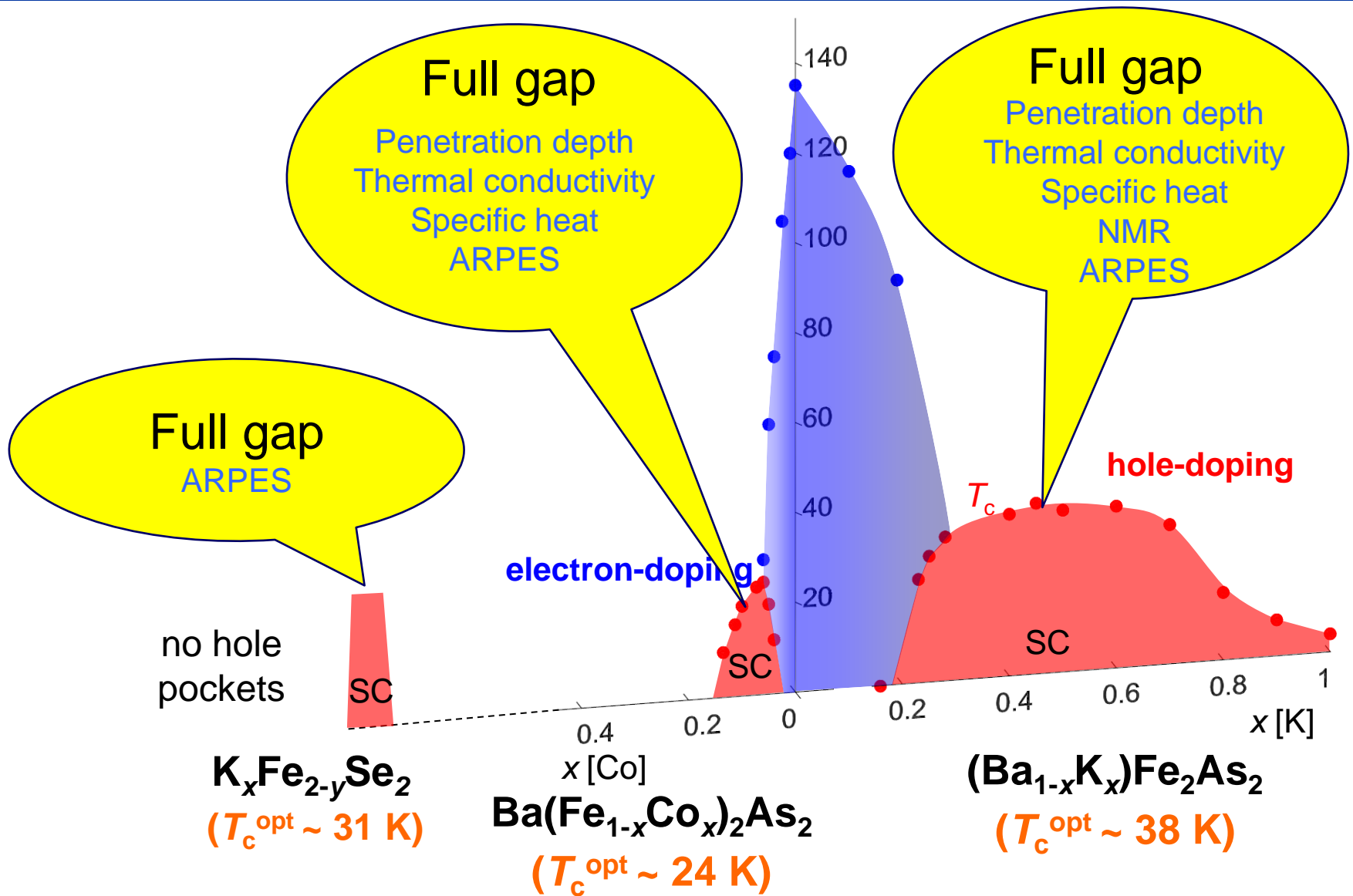


SC gap structure in heavily electron doped systems



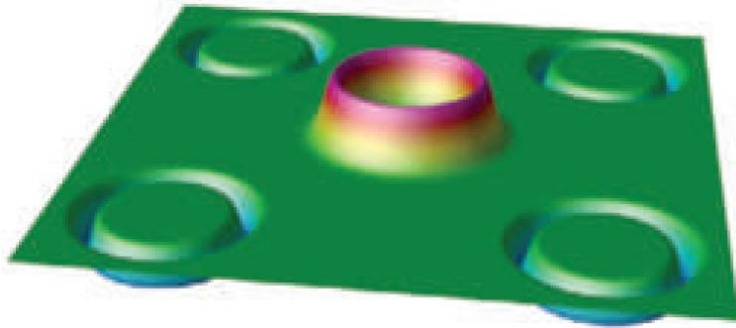
Y. Zhang *et al.*,
Nature Materials (2011).

Superconducting gap structure of BaFe₂As₂ systems

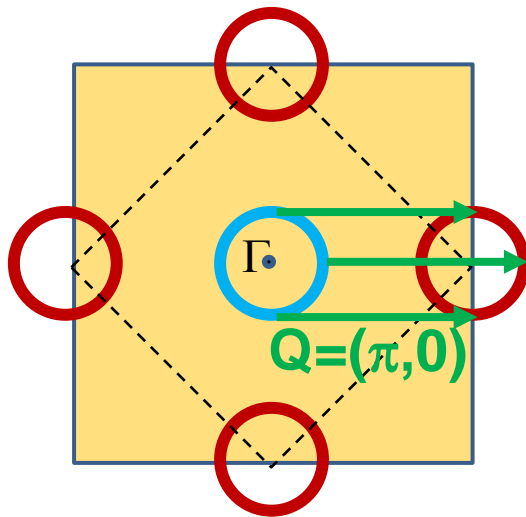


Sign change or no sign change?

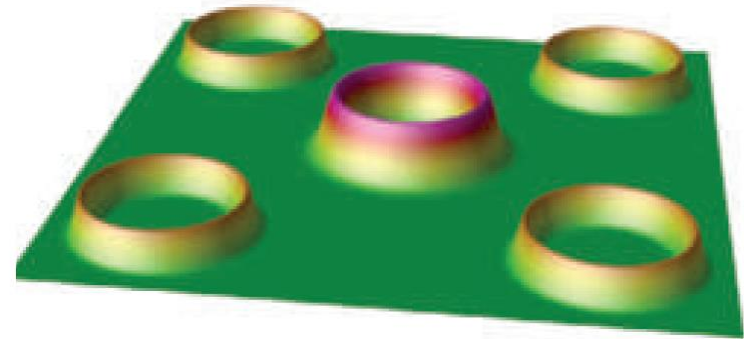
S_{+-}



Spin fluctuations



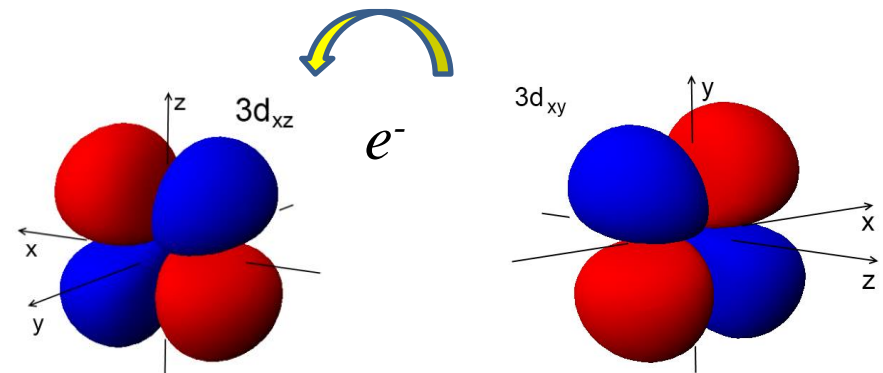
S_{++}



or

?

Orbital fluctuations
(Quadrupole fluctuation)



Charge up

Charge down

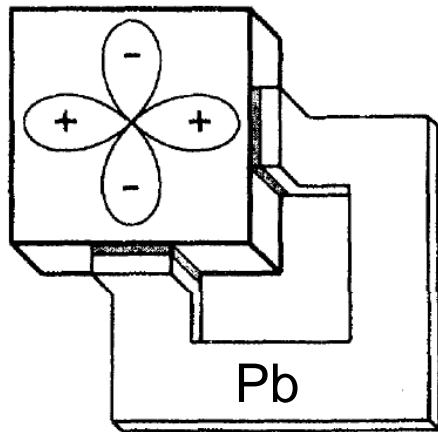
S+- or S++?

1. Phase sensitive test
2. NMR
3. Neutron scattering
4. Quasi-particle interference
5. Impurity effect

S+- or S++?: Phase sensitive tests



d-wave



PRL 102, 227007 (2009)

PHYSICAL REVIEW LETTERS

week ending
5 JUNE 2009

Possible Phase-Sensitive Tests of Pairing Symmetry in Pnictide Superconductors

D. Parker¹ and I.I. Mazin¹

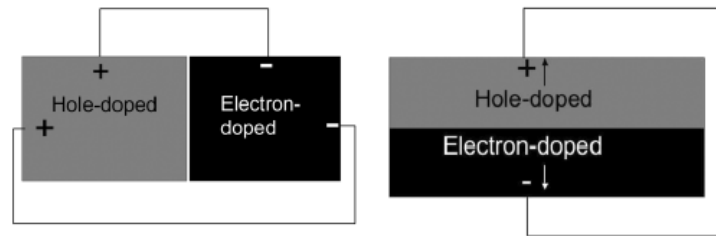
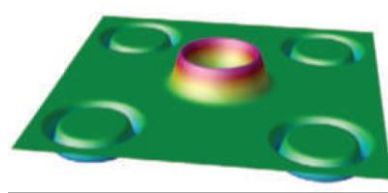


FIG. 3. A schematic view of the tunneling geometry for the proposed bicrystal experiments. Left: an *ab*-plane orientation with two possible lead orientations; right: a *c*-axis orientation.

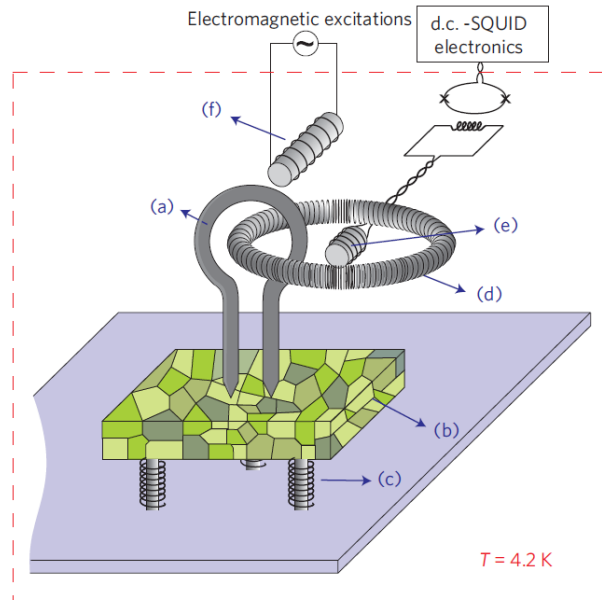
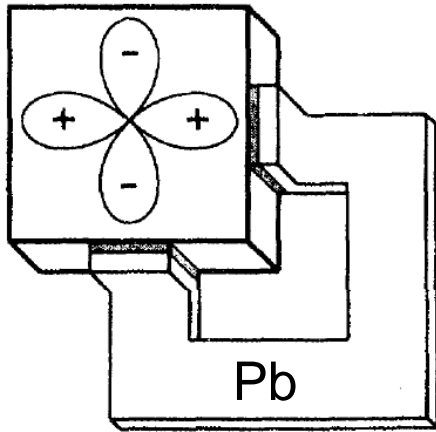
Practically very difficult to fabricate such junctions

S+- or S++?: Phase sensitive tests

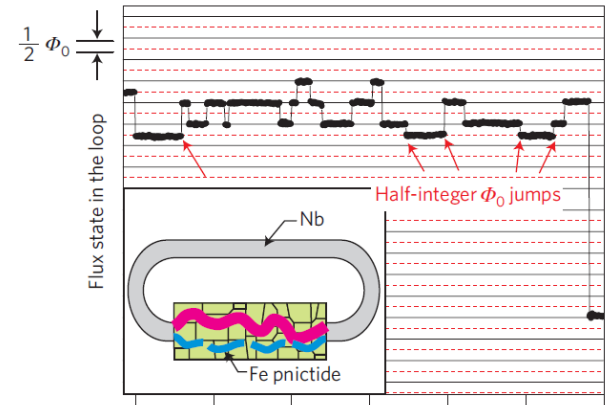


S_{+-}

d-wave



$\text{NdFeAsO}_{0.88}\text{F}_{0.12}$



C.T. Chen et al. Nature Phys. (10)

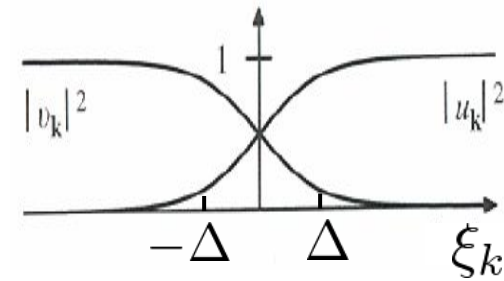
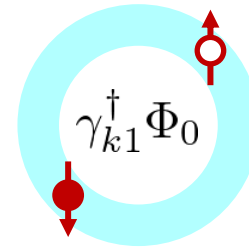
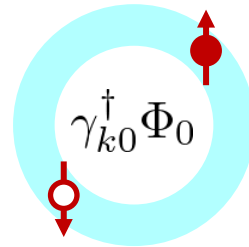
Experiments have been performed on polycrystals

Sign change or no sign change?

Quasiparticle excitations from the SC ground state

$$\gamma_{k0}^\dagger = u_k c_{k\uparrow}^\dagger - v_k c_{-k\downarrow}$$

$$\gamma_{k1}^\dagger = u_k c_{-k\downarrow}^\dagger + v_k c_{k\uparrow}$$



$$|u_k|^2 = \frac{1}{2} \left(1 + \frac{\xi_k}{\sqrt{\Delta_k^2 + \xi_k^2}} \right) \quad |v_k|^2 = \frac{1}{2} \left(1 - \frac{\xi_k}{\sqrt{\Delta_k^2 + \xi_k^2}} \right) \quad \xi_k \equiv \frac{\hbar^2 k^2}{2m} - \varepsilon_F$$

B-quasiparticle: a superposition of an electron and a hole

$$\mathbf{k}\sigma \rightarrow \mathbf{k}'\sigma'$$

$$\mathcal{H}_1 = \sum_{k\sigma, k'\sigma'} B_{k\sigma, k'\sigma'} c_{k\sigma}^\dagger c_{k'\sigma'} \left\{ \begin{array}{l} B_{k\sigma, k'\sigma'} c_{k\sigma}^\dagger c_{k'\sigma'} \\ B_{-k'-\sigma', -k-\sigma} c_{-k'-\sigma'}^\dagger c_{-k-\sigma} \end{array} \right. \quad \text{connected by time-reversal symmetry}$$

Coherence factor

Scattering of QPs

$$(u_k u_{k'} \pm v_k v_{k'})^2 = \frac{1}{2} \left(1 \pm \frac{\Delta^2}{E_k E_{k'}} \right)$$

Creation and annihilation of two QPs

$$(v_k u_{k'} \pm u_k v_{k'})^2 = \frac{1}{2} \left(1 \pm \frac{\Delta^2}{E_k E_{k'}} \right)$$

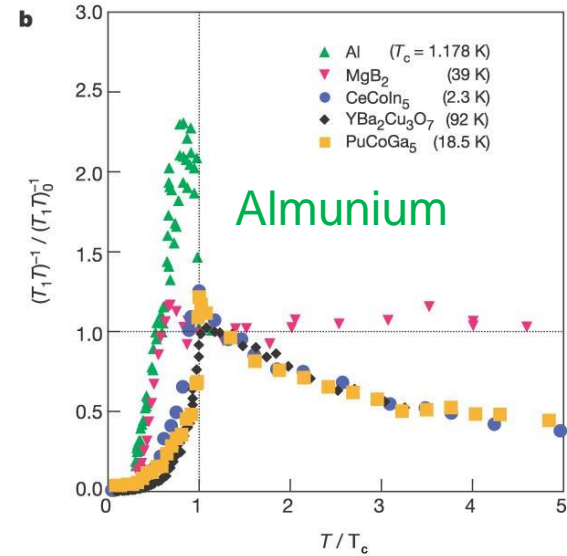
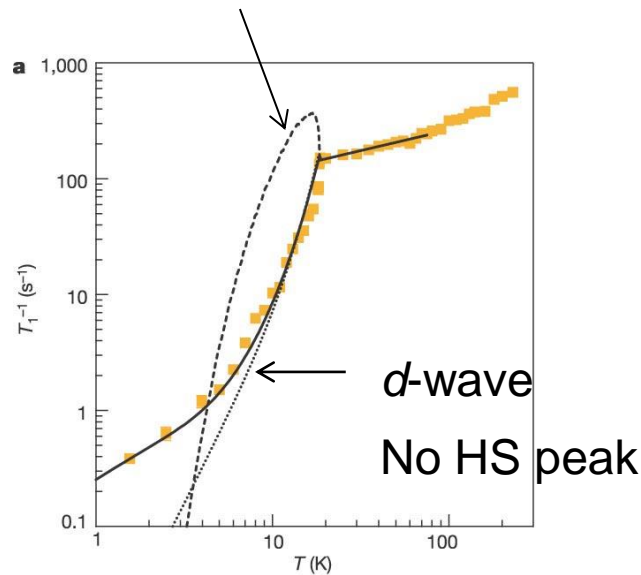
S+- or S++?: NMR

$$\frac{1}{T_1 T} \propto \sum_{kk'} \left(1 + \frac{\Delta_k \Delta_{k'}}{E_k E_{k'}} \right) \left[-\frac{\partial f(E_k)}{\partial E_k} \right] \delta(E_k - E_{k'})$$

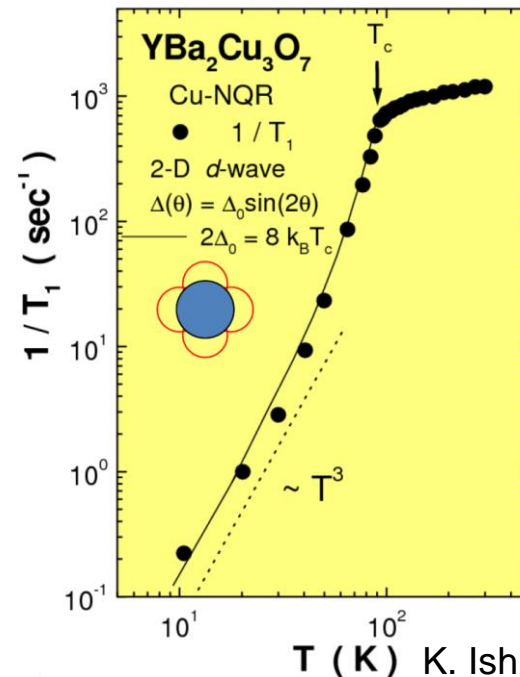
s-wave

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 + \Delta^2}{E^2 - \Delta^2} \operatorname{sech}^2 \left(\frac{E}{2T} \right)$$

Hebel-Slichter peak



N. Curro *et al.* Nature (12)



T (K) K. Ishida *et al.* JPSJ (93)

S+- or S++?: NMR

$$\frac{1}{T_1 T} \propto \sum_{kk'} \left(1 + \frac{\Delta_k \Delta_{k'}}{E_k E_{k'}} \right) \left[-\frac{\partial f(E_k)}{\partial E_k} \right] \delta(E_k - E_{k'})$$

S₊₊

$$\Delta_k = \Delta_{k'} = \Delta$$

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 + \Delta^2}{E^2 - \Delta^2} \operatorname{sech}^2 \left(\frac{E}{2T} \right)$$

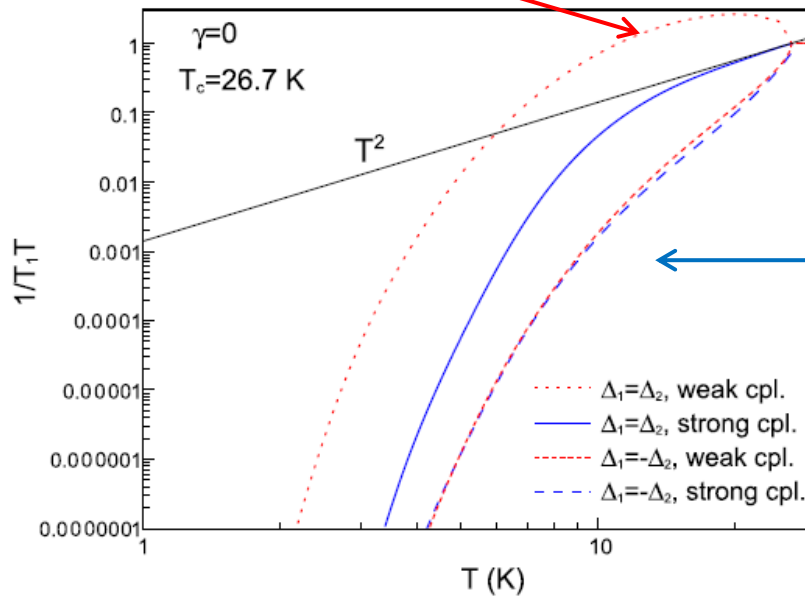
S₊₋

$$\Delta_k = -\Delta_{k'} = \Delta$$

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \operatorname{sech}^2 \left(\frac{E}{2T} \right)$$

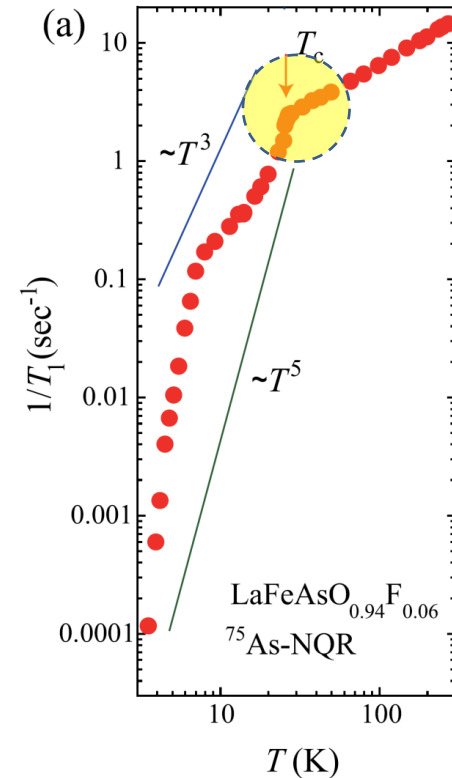
No HS peak

Hebel-Slichter peak



No HS peak

D. Parker *et al.*
PRB (08)



T. Oka *et al.*
PRL (12)

However, the HS peak readily disappears by inelastic scatterings, eg. Pb.

Absence of the coherence peak is not evidence of **S₊₋**

S+- or S++?: Neutron resonance peak at Q

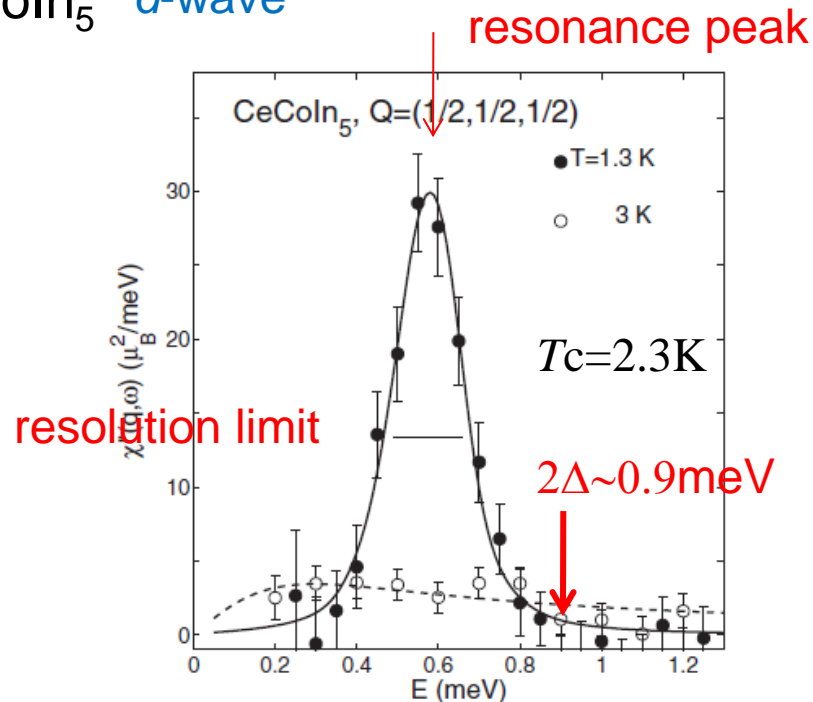
In the superconducting state

$$\text{Im}\chi_0(\mathbf{q}, \omega) = \frac{1}{4} \frac{1}{(2\pi)^3} \int d^3k \left(1 - \frac{\Delta_k \Delta_{k+q}}{E_{k+q} E_k} \right) \delta(\omega - E_{k+q} - E_k) \quad E_k = \sqrt{\xi_k^2 + \Delta_k^2}$$

The coherence factor becomes 2 for $\Delta_{k+Q} = -\Delta_k$

Sharp resonance peak at $\omega_{\text{res}} < 2\Delta$

CeCoIn₅ *d-wave*



S+- or S++?: Neutron resonance peak at Q

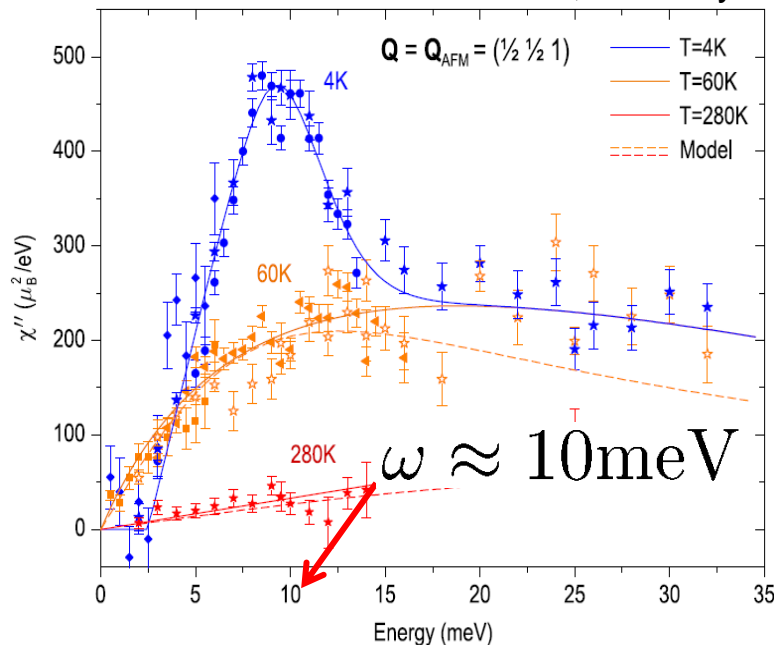
In the superconducting state

$$\text{Im}\chi_0(\mathbf{q}, \omega) = \frac{1}{4} \frac{1}{(2\pi)^3} \int d^3k \left(1 - \frac{\Delta_k \Delta_{k+q}}{E_{k+q} E_k} \right) \delta(\omega - E_{k+q} - E_k) \quad E_k = \sqrt{\xi_k^2 + \Delta_k^2}$$

The coherence factor becomes 2 for $\Delta_{\mathbf{k}+\mathbf{Q}} = -\Delta_{\mathbf{k}}$

- S_{+-} Sharp resonance peak at $\omega_{\text{res}} < 2\Delta$ ($\Delta_{\text{el}} + \Delta_{\text{hole}}$)
- S_{++} Broad peak at $\omega_{\text{res}} > 2\Delta$ ($\Delta_{\text{el}} + \Delta_{\text{hole}}$)

BaFe_{1.85}Co_{0.15}As₂ Inosov *et al.*, Nat. Phys. (10).



ARPES (bulk-sensitive):

$$\Delta_{\text{el}} + \Delta_{\text{hole}} \approx 11.6\text{meV}$$

Terashima *et al.*, PNAS 2009

penetration depth:

$$\Delta_{\text{el}} + \Delta_{\text{hole}} \approx 8.4\text{meV}$$

Luan *et al.*, PRL 2011

specific heat:

$$\Delta_{\text{el}} + \Delta_{\text{hole}} \approx 7\text{meV}$$

Hardy *et al.*, EPL 2010

S+- or S++?: Neutron resonance peak at Q

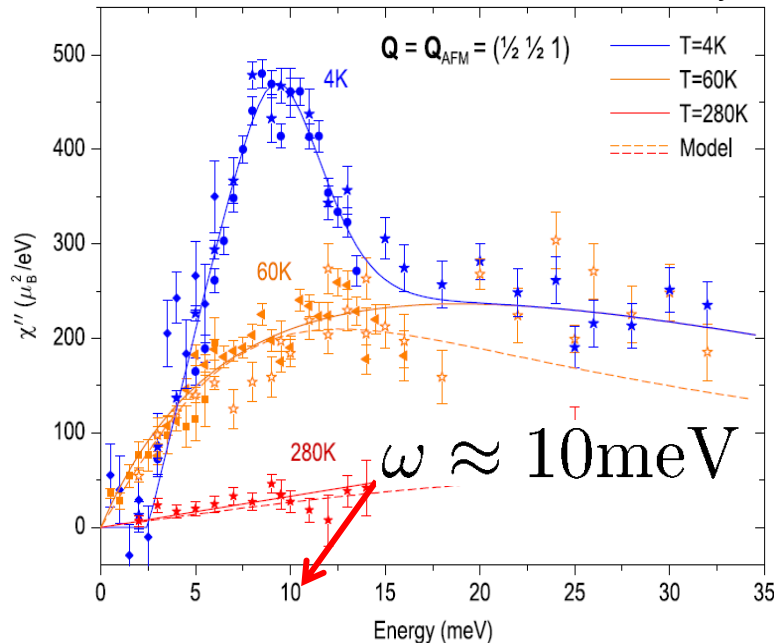
In the superconducting state

$$\text{Im}\chi_0(\mathbf{q}, \omega) = \frac{1}{4} \frac{1}{(2\pi)^3} \int d^3k \left(1 - \frac{\Delta_k \Delta_{k+q}}{E_{k+q} E_k} \right) \delta(\omega - E_{k+q} - E_k) \quad E_k = \sqrt{\xi_k^2 + \Delta_k^2}$$

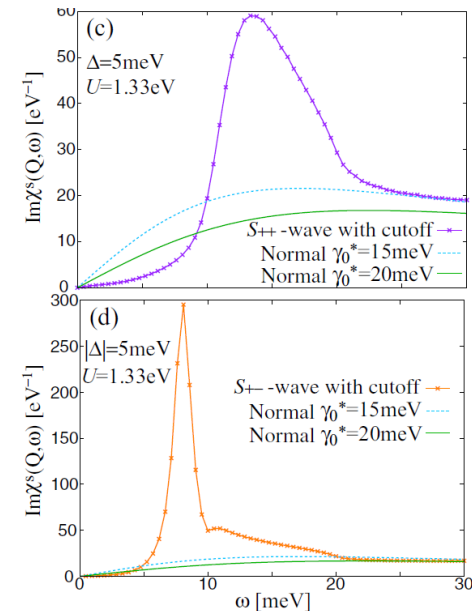
The coherence factor becomes 2 for $\Delta_{k+Q} = -\Delta_k$

- S_{+-} Sharp resonance peak at $\omega_{\text{res}} < 2\Delta$ ($\Delta_{\text{el}} + \Delta_{\text{hole}}$)
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BaFe_{1.85}Co_{0.15}As₂ Inosov *et al.*, Nat. Phys. (10).



S. Onari and H. Kontani, PRB (11)



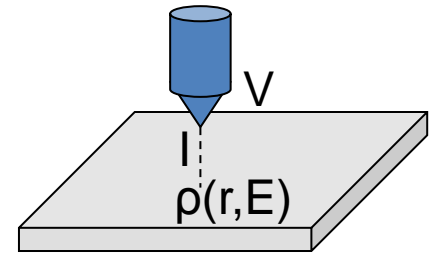
Neutron scattering experiments can be explained by either models.

S+- or S++?: Quasiparticle interference (QPI)

Quasi-Particle Interference

Tunnel conductance

$$Z(\mathbf{r}, E) \equiv \frac{dI/dV(\mathbf{r}, +E)}{dI/dV(\mathbf{r}, -E)} = \frac{\rho(\mathbf{r}, +E)}{\rho(\mathbf{r}, -E)} \xrightarrow{\text{FT}} Z(\mathbf{q}, E)$$



No impurity (no scattering) $Z(\mathbf{q}, E) = 0$ for $\mathbf{q} \neq 0$
 Nonmagnetic impurity

QP scattering probability (SC state)

$$w(\mathbf{k}\sigma \rightarrow \mathbf{k}'\sigma) \propto |V(\mathbf{k}, \mathbf{k}')|^2 \underbrace{(u_k u_{k'} - v_k v_{k'})^2}_{\text{coherence factor}}$$

Nonmagnetic
(no spin flip)

↑
matrix element

↑
coherence factor

$$(u_k u_{k'} - v_k v_{k'})^2 = \frac{1}{2} \left(1 - \frac{\Delta_k \Delta_{k'}}{E_k E_{k'}} \right)$$

sign-preserving scattering

$$\Delta_k \Delta_{k'} > 0 \quad (u_k u_{k'} - v_k v_{k'})^2 \quad \text{small}$$

sign-reversing scattering

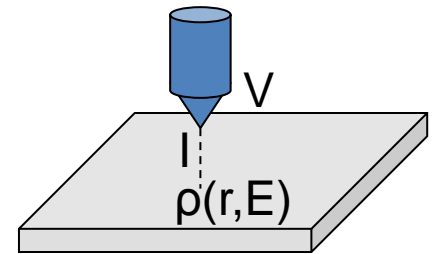
$$\Delta_k \Delta_{k'} < 0 \quad (u_k u_{k'} - v_k v_{k'})^2 \quad \text{large}$$

S+- or S++?: Quasiparticle interference (QPI)

Quasi-Particle Interference

$$Z(\mathbf{r}, E) \equiv \frac{dI/dV(\mathbf{r}, +E)}{dI/dV(\mathbf{r}, -E)} = \frac{\rho(\mathbf{r}, +E)}{\rho(\mathbf{r}, -E)} \xrightarrow{\text{FT}} Z(\mathbf{q}, E)$$

Tunnel conductance

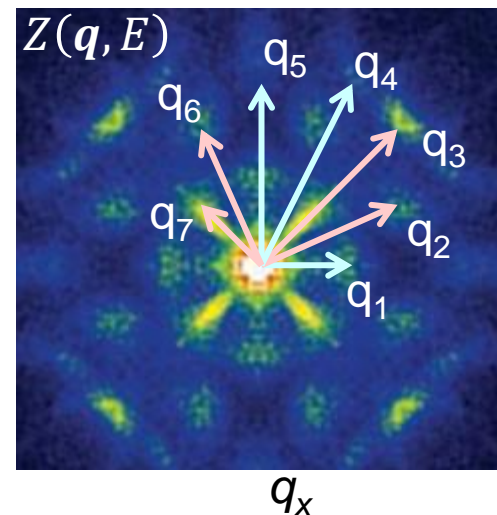
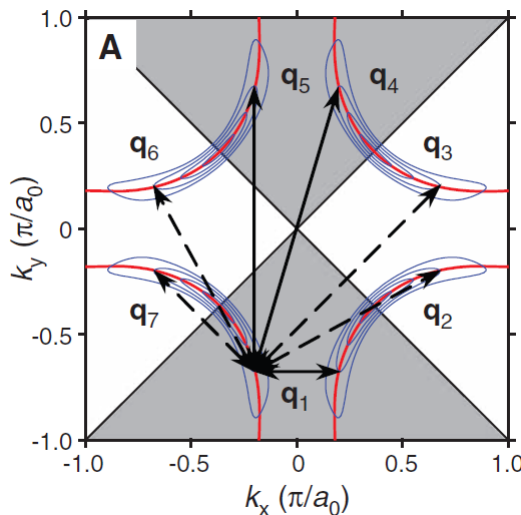


No impurity (no scattering) $Z(\mathbf{q}, E) = 0$ for $\mathbf{q} \neq 0$
 Nonmagnetic impurity

Cuprate : Octet Model

J. Hoffman *et al.*, Science (2002), K. McElroy, *et al.*, Nature (2003).

$\Delta_{\mathbf{k}}$ and $\Delta_{\mathbf{k}+\mathbf{q}}$ {
 sign-preserving scattering => suppression
 sign-reversing scattering => enhancement



sign-preserving
 ($\mathbf{q}_1, \mathbf{q}_4, \mathbf{q}_5$)

sign-reversing
 ($\mathbf{q}_2, \mathbf{q}_3, \mathbf{q}_6, \mathbf{q}_7$)

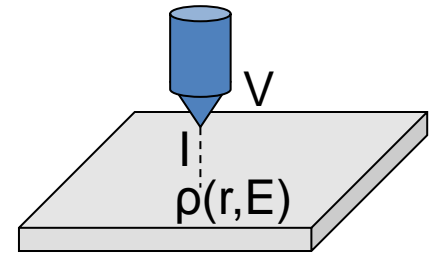
T. Hanaguri *et al.*

S+- or S++?: Quasiparticle interference (QPI)

Quasi-Particle Interference

Tunnel conductance

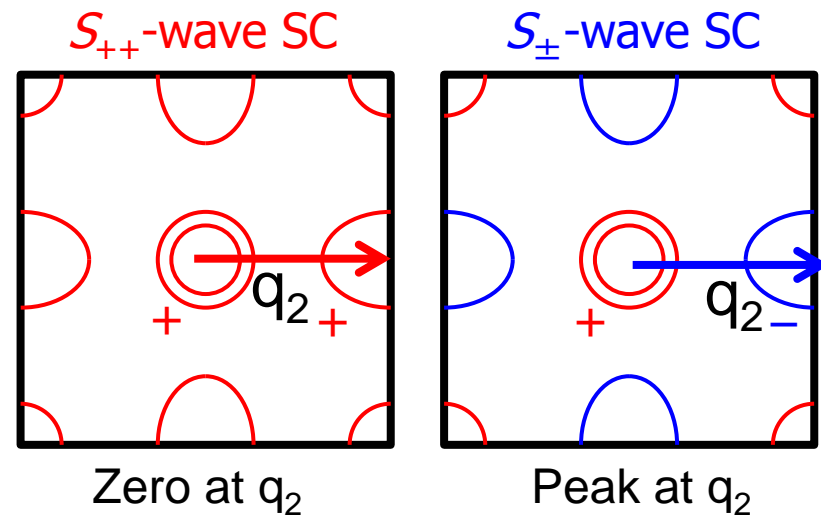
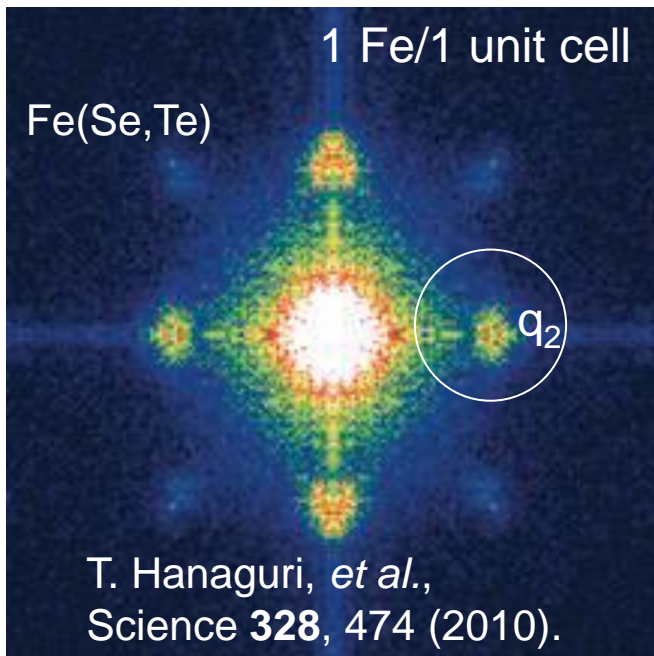
$$Z(\mathbf{r}, E) \equiv \frac{dI/dV(\mathbf{r}, +E)}{dI/dV(\mathbf{r}, -E)} = \frac{\rho(\mathbf{r}, +E)}{\rho(\mathbf{r}, -E)} \xrightarrow{\text{FT}} Z(\mathbf{q}, E)$$



No impurity (no scattering) $Z(\mathbf{q}, E) = 0$ for $\mathbf{q} \neq 0$
 Nonmagnetic impurity

Fe-based superconductor

$\Delta_{\mathbf{k}}$ and $\Delta_{\mathbf{k}+\mathbf{q}}$ $\left\{ \begin{array}{l} \text{sign-preserving scattering} \Rightarrow \text{suppression} \\ \text{sign-reversing scattering} \Rightarrow \text{enhancement} \end{array} \right.$

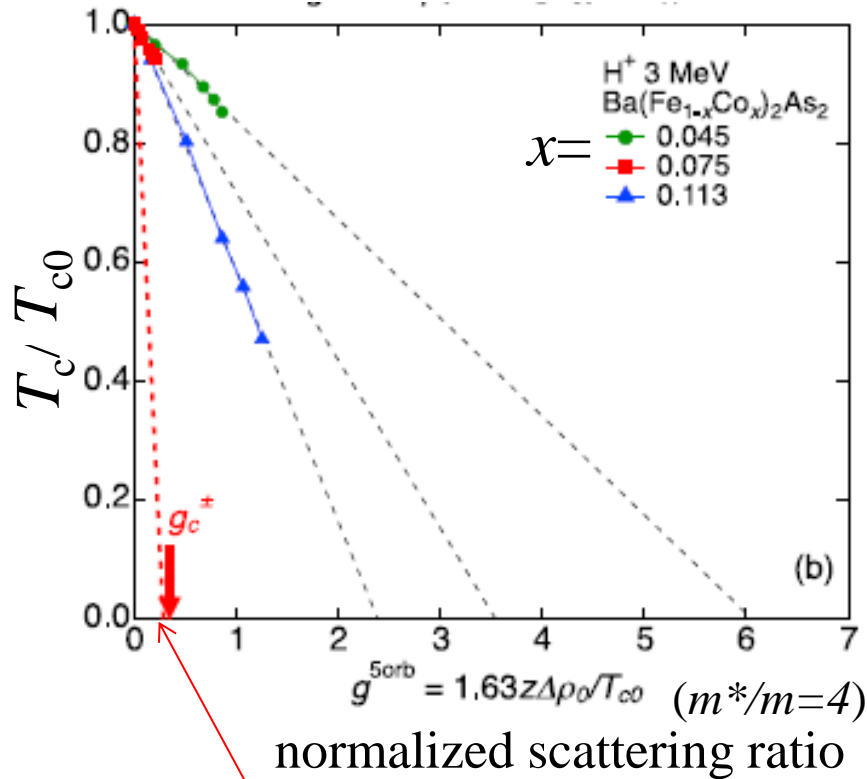


However, q_2 spot can appear even in S_{++} case when $\Delta_e \neq \Delta_h$

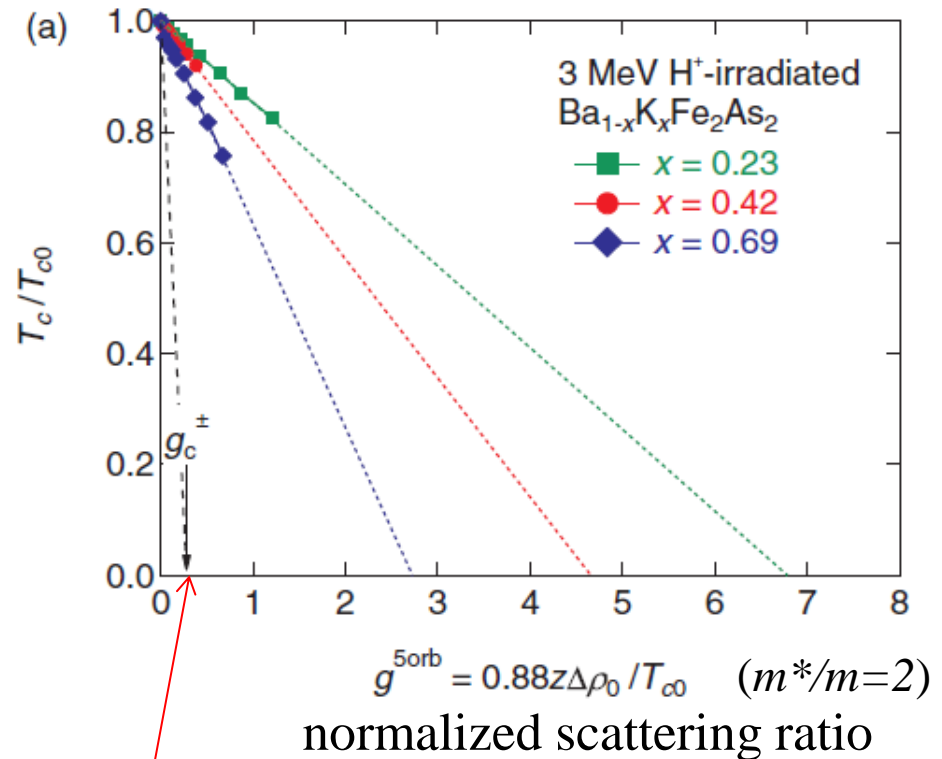
S+- or S++?: Impurity effect



Nakajima *et al.*, Phys. Rev. B 82, 220504(R)



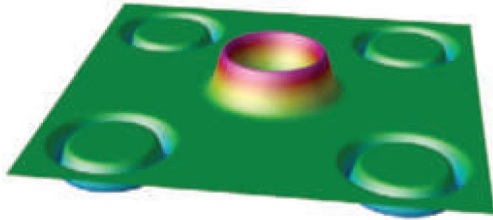
Taen *et al.*, Phys. Rev. B 88, 224514



theoretical prediction for S_{+-} wave (Onari and Kontani, PRL 2009)

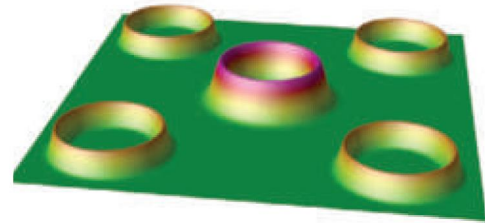
The robustness of the SC state against impurity contradicts with the S_{+-} wave state.

S_{+-}



?

S_{++}



?

No conclusive experimental evidence so far

Are all iron-based high- T_c superconductors fully gapped?

If some are nodal

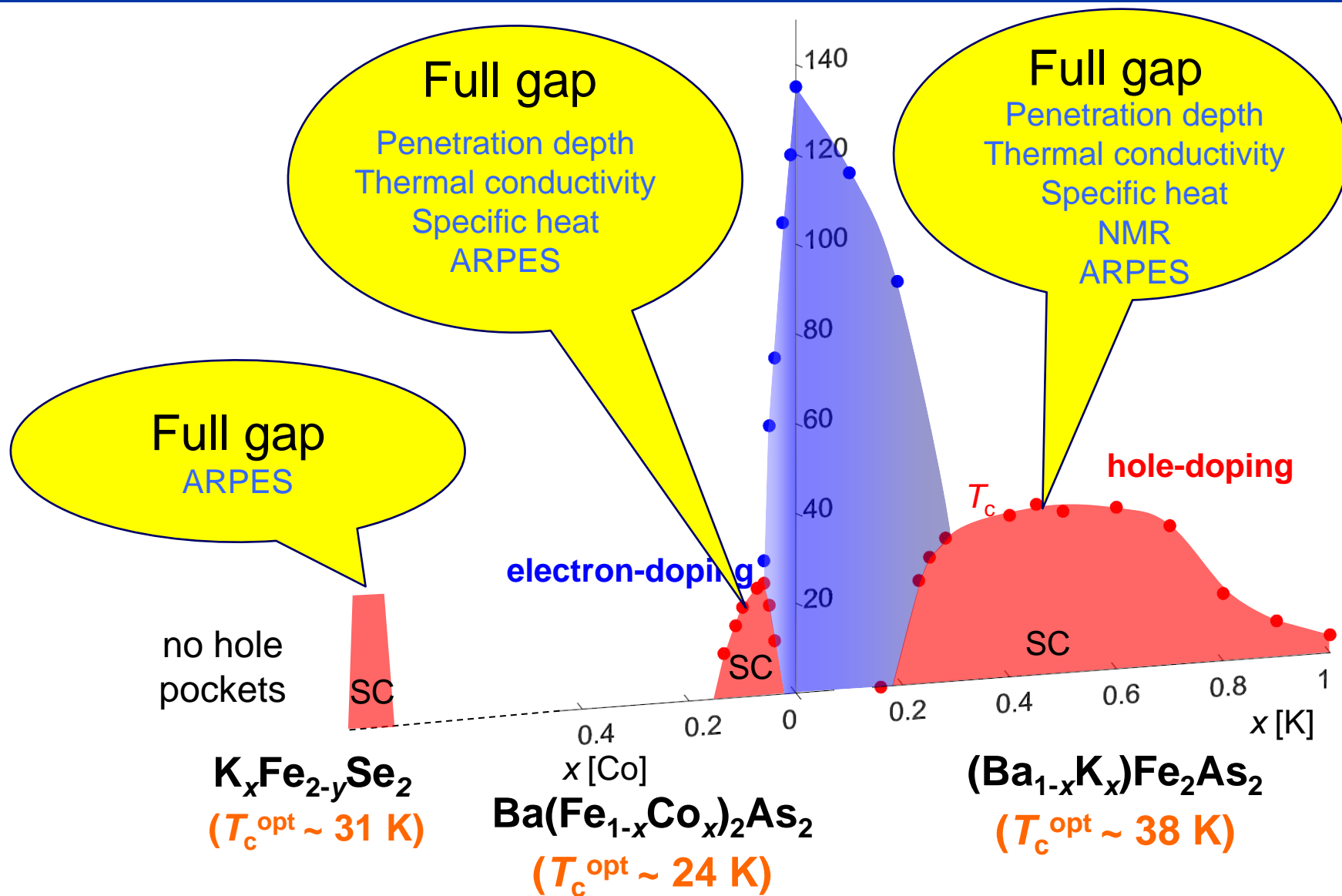
→ Presence of repulsive interaction

Accidental or symmetry protected?

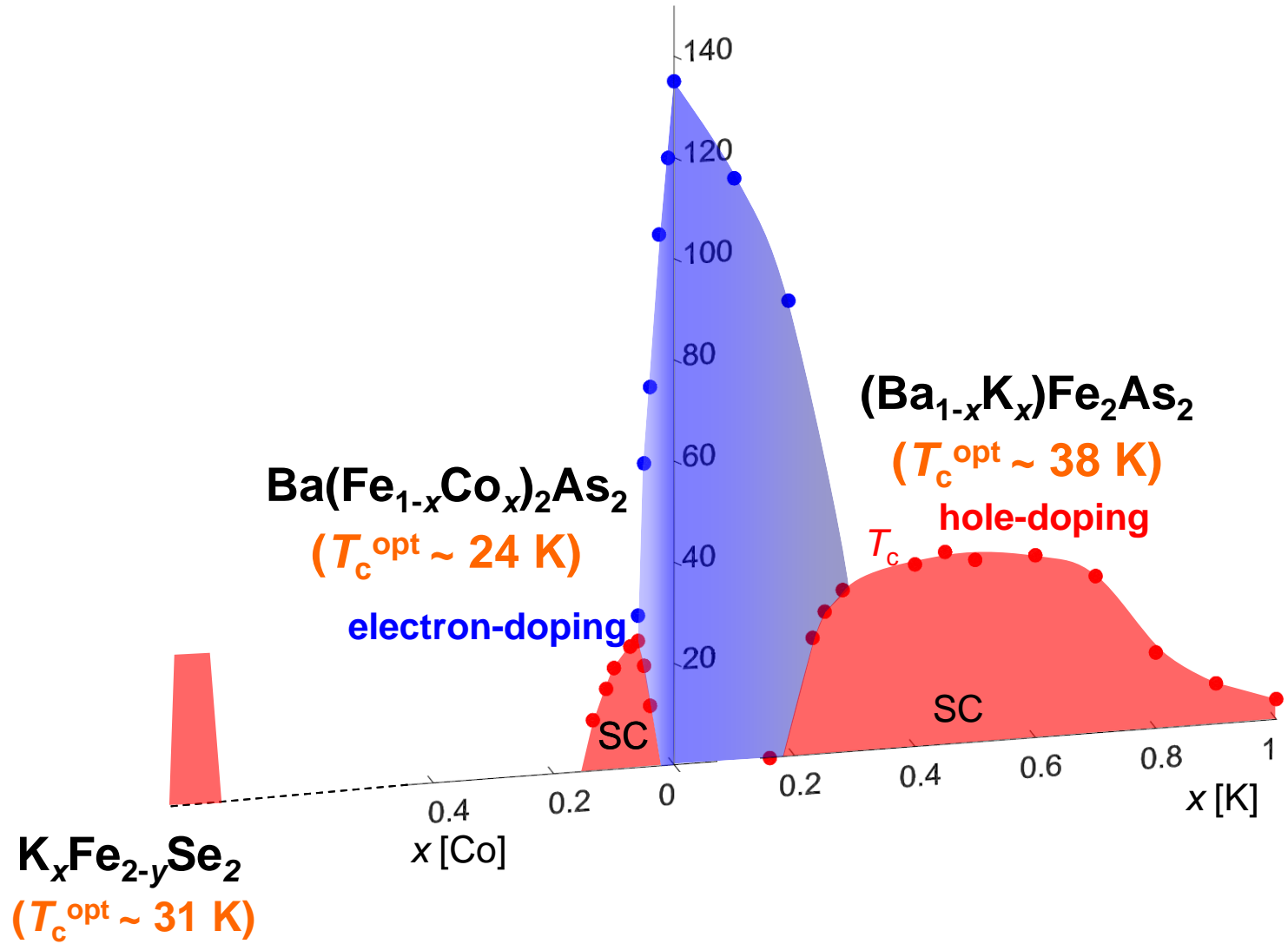
If accidental

→ Presence of two (or more) competing pairing interactions

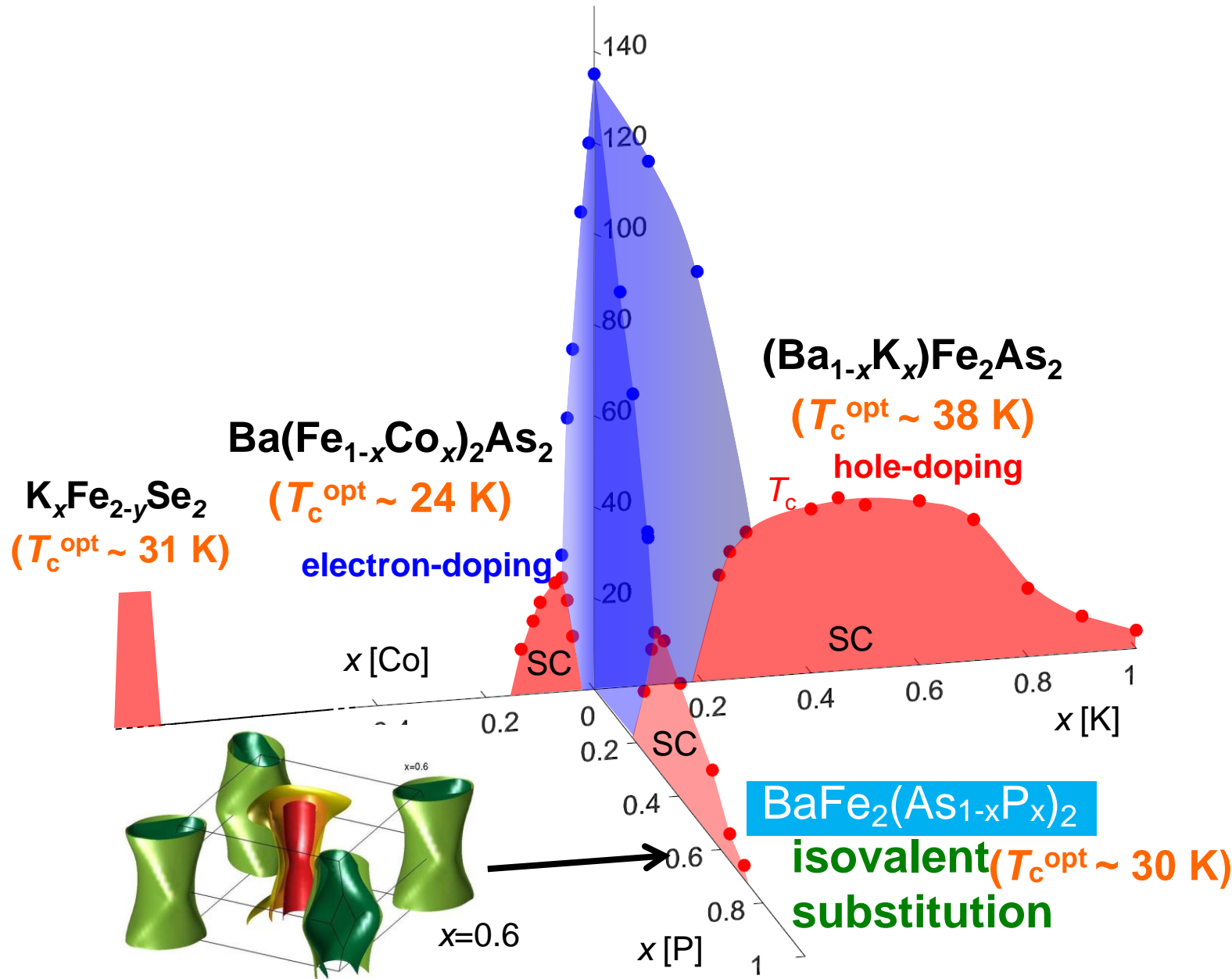
Superconducting gap structure of BaFe₂As₂ systems



SC gap structure in isovalent doped systems

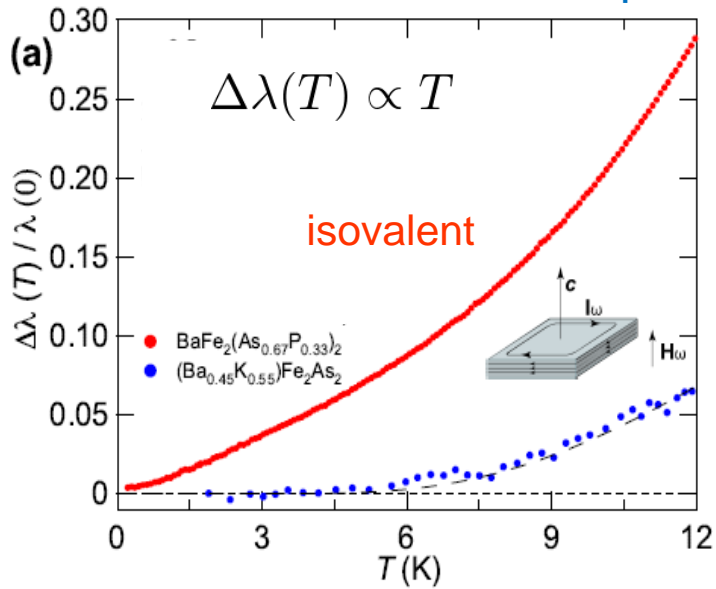


SC gap structure in isovalent doped systems

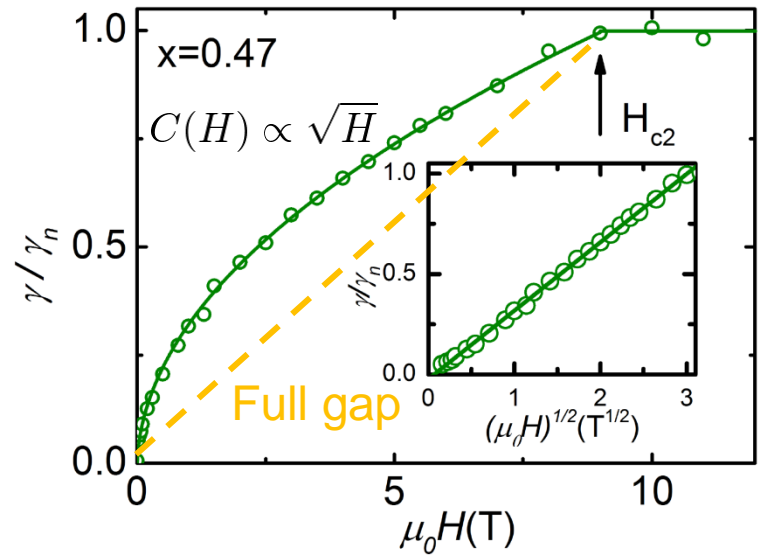


SC gap structure in isovalent doped systems

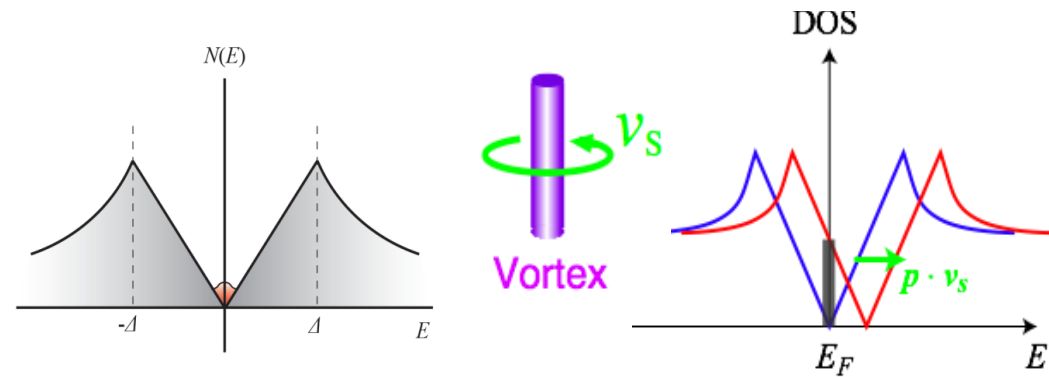
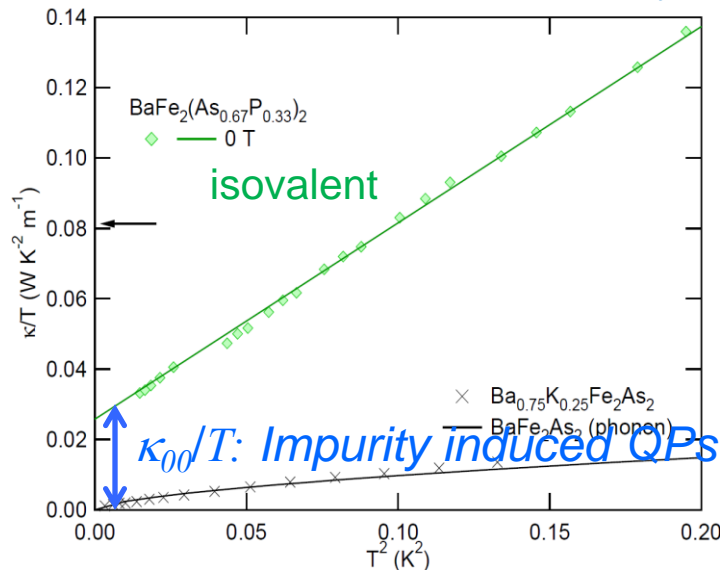
Penetration depth



Specific heat $\text{BaFe}_2(\text{As}_{0.53}\text{P}_{0.47})_2$



Thermal conductivity

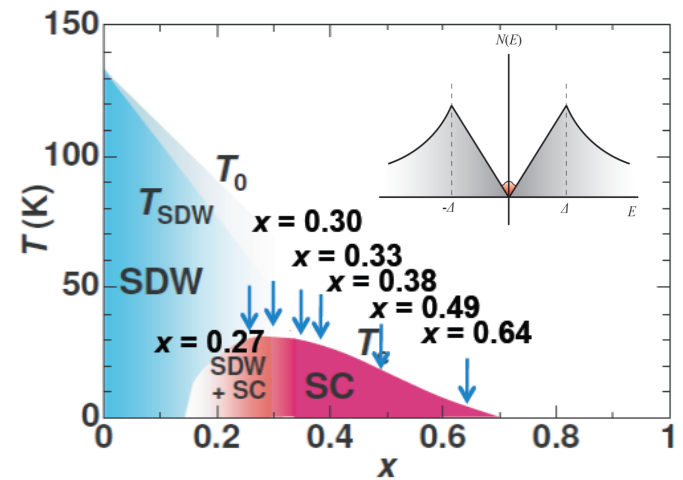
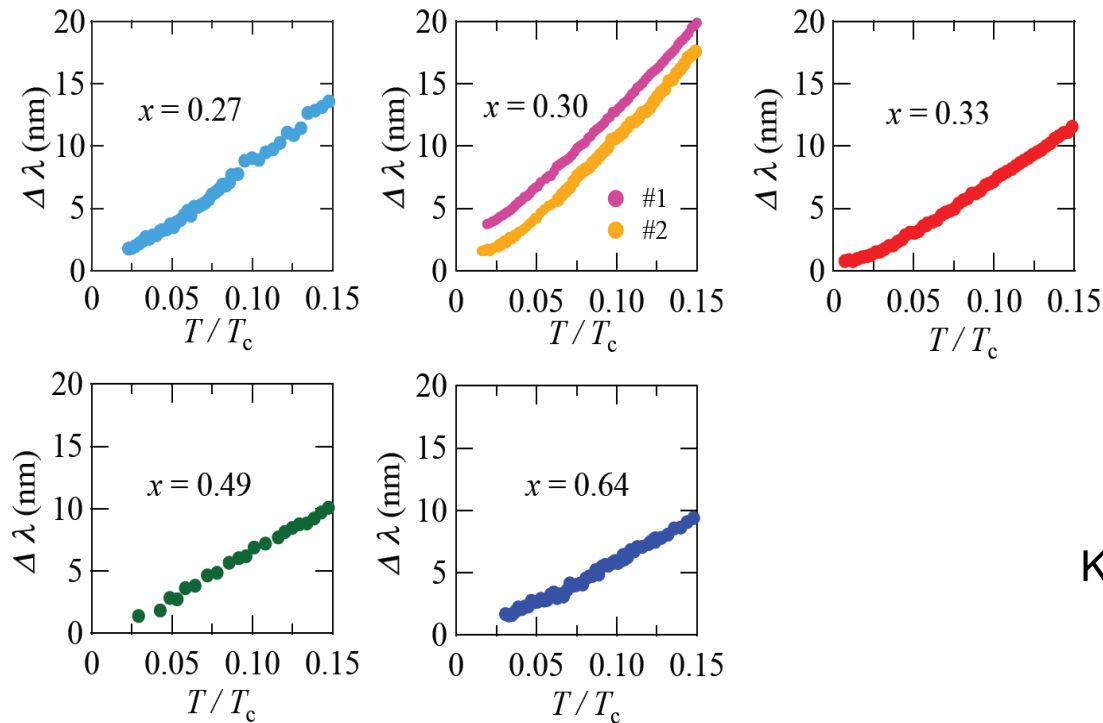


Luo *et al.*
Kurita *et al.*

Doppler shift

K. Hashimoto *et al.*, PRB (2010)
K. Hashimoto *et al.*, PRL (2009)
K. Hashimoto *et al.*, Science (2012)
A. Carrington *et al.* (2014)

SC gap structure in isovalent doped systems



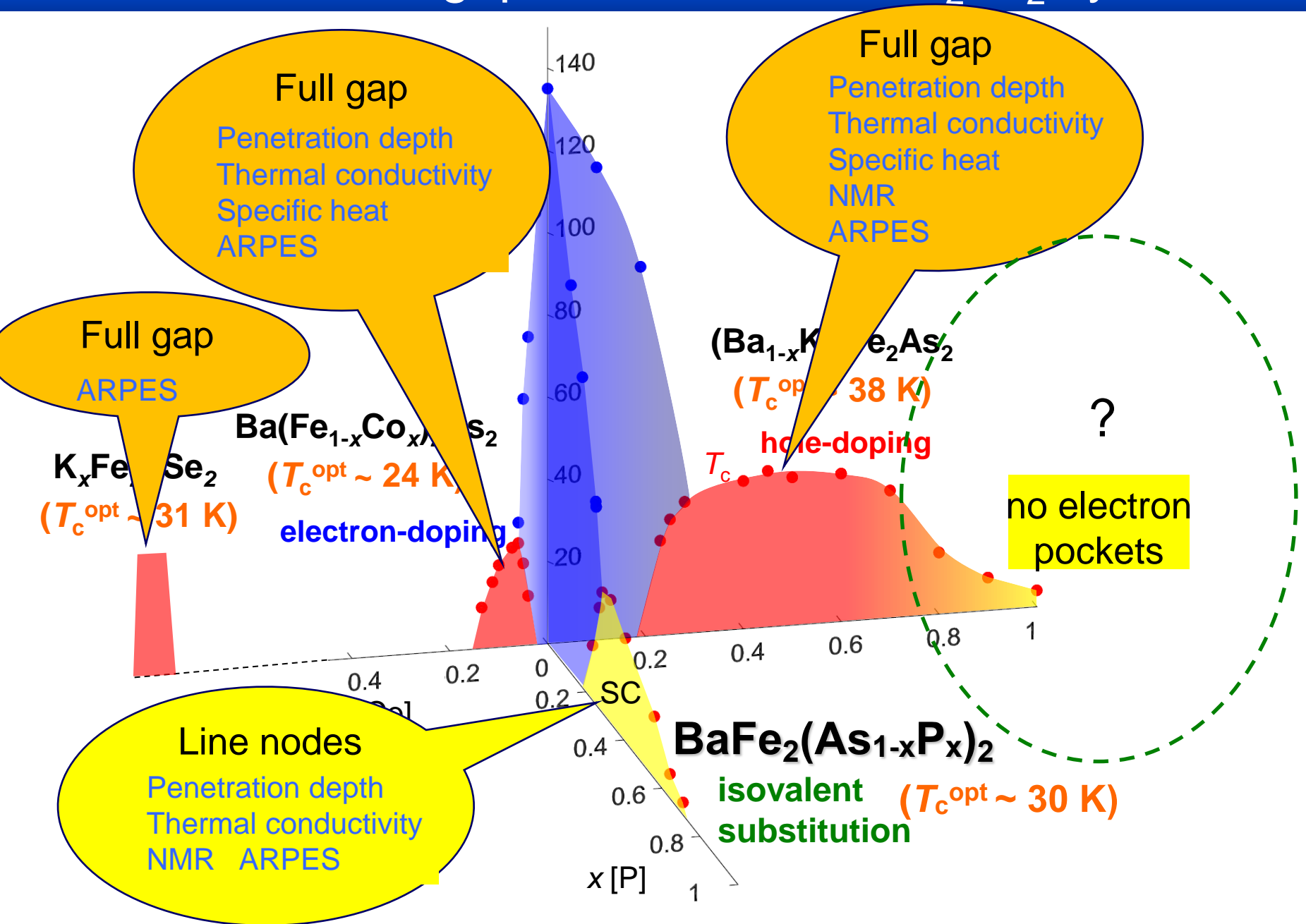
K. Hashimoto *et al.*, Science (2012)

- The presence of line nodes is a robust feature for all x .

Presence of repulsive interaction

non-phononic (magnetic) pairing interaction

Non-universal gap structure in BaFe₂As₂ systems



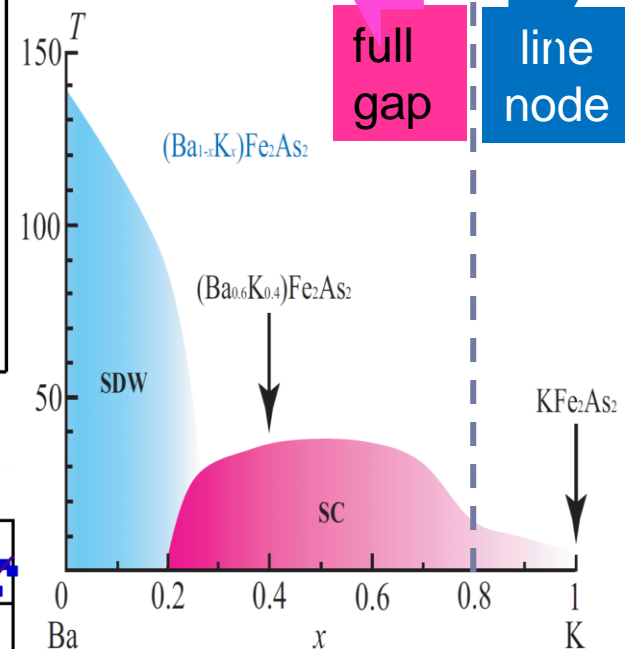
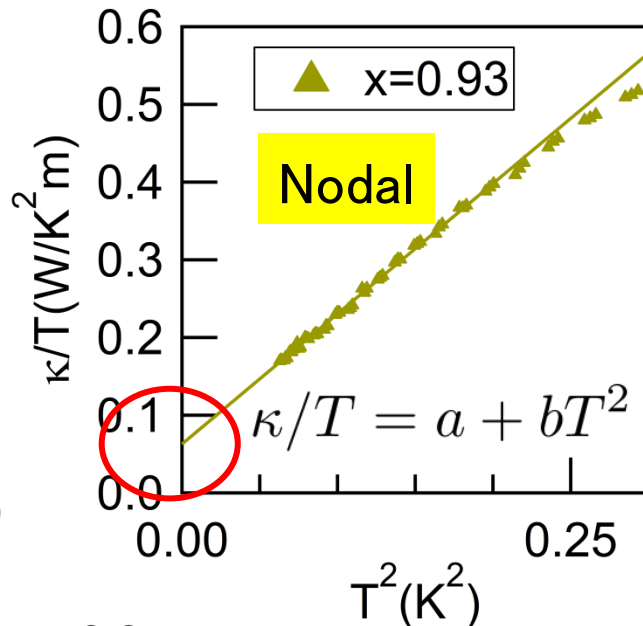
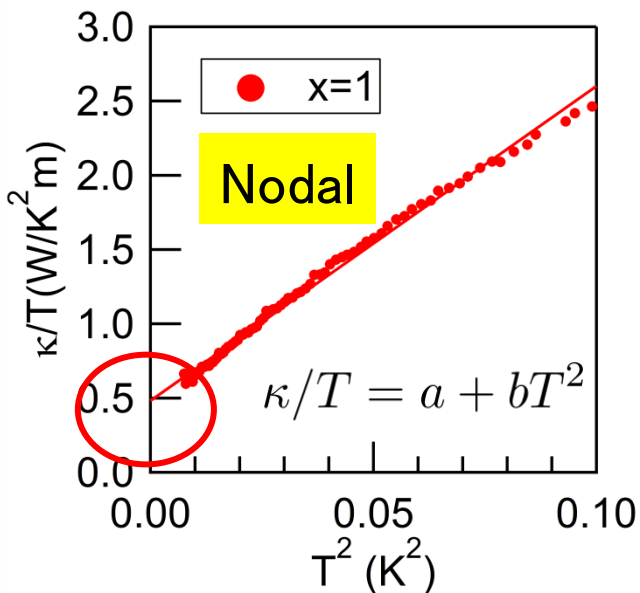
Gap structure of hole doped $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$

D. Watanabe *et al.* PRB (2014)

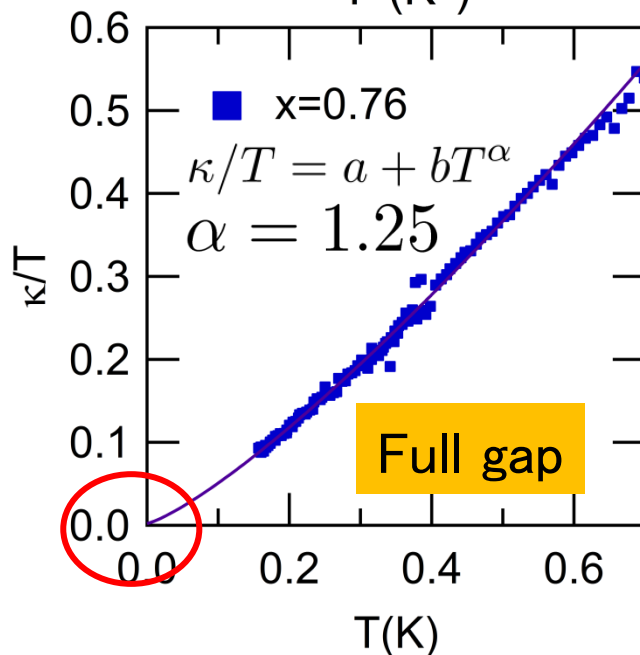
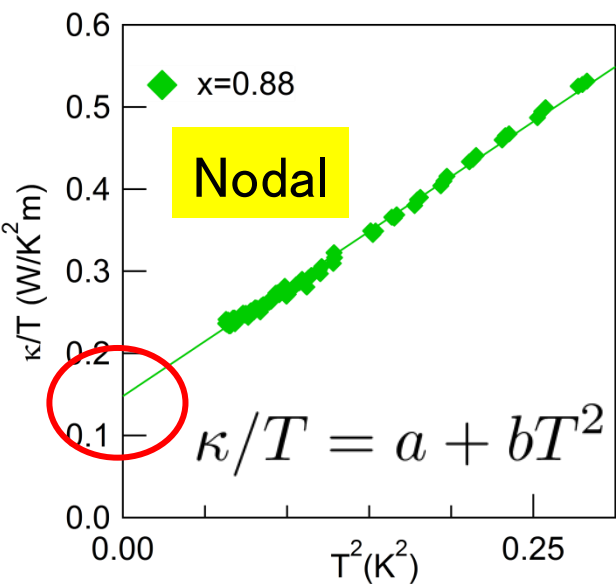
Boundary

$0.76 < x < 0.88$

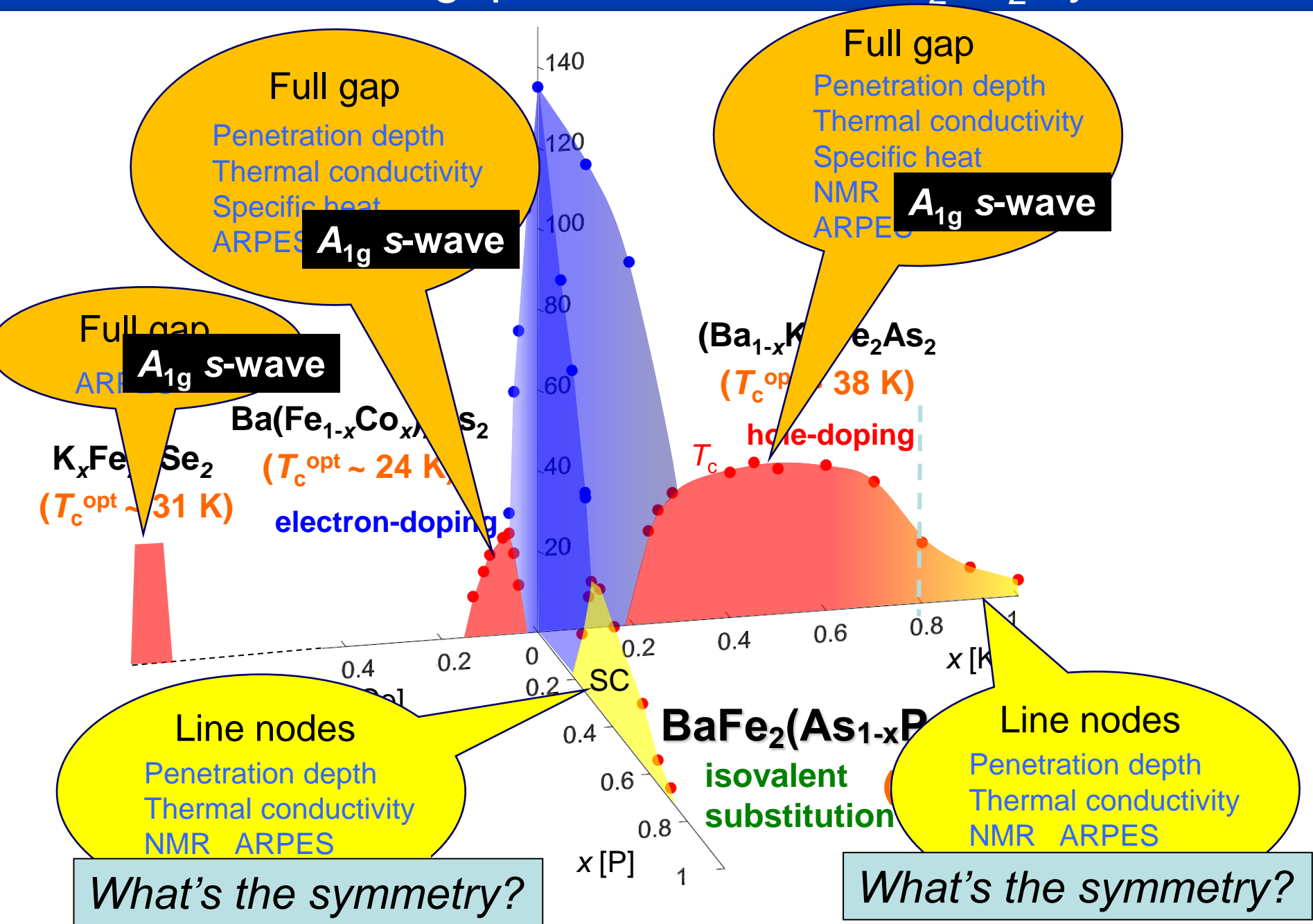
full gap
line node



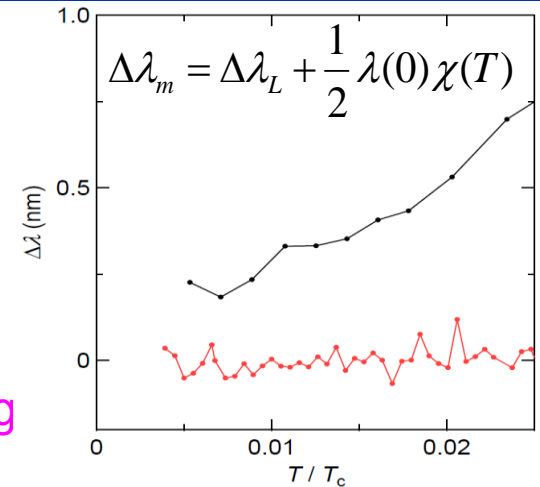
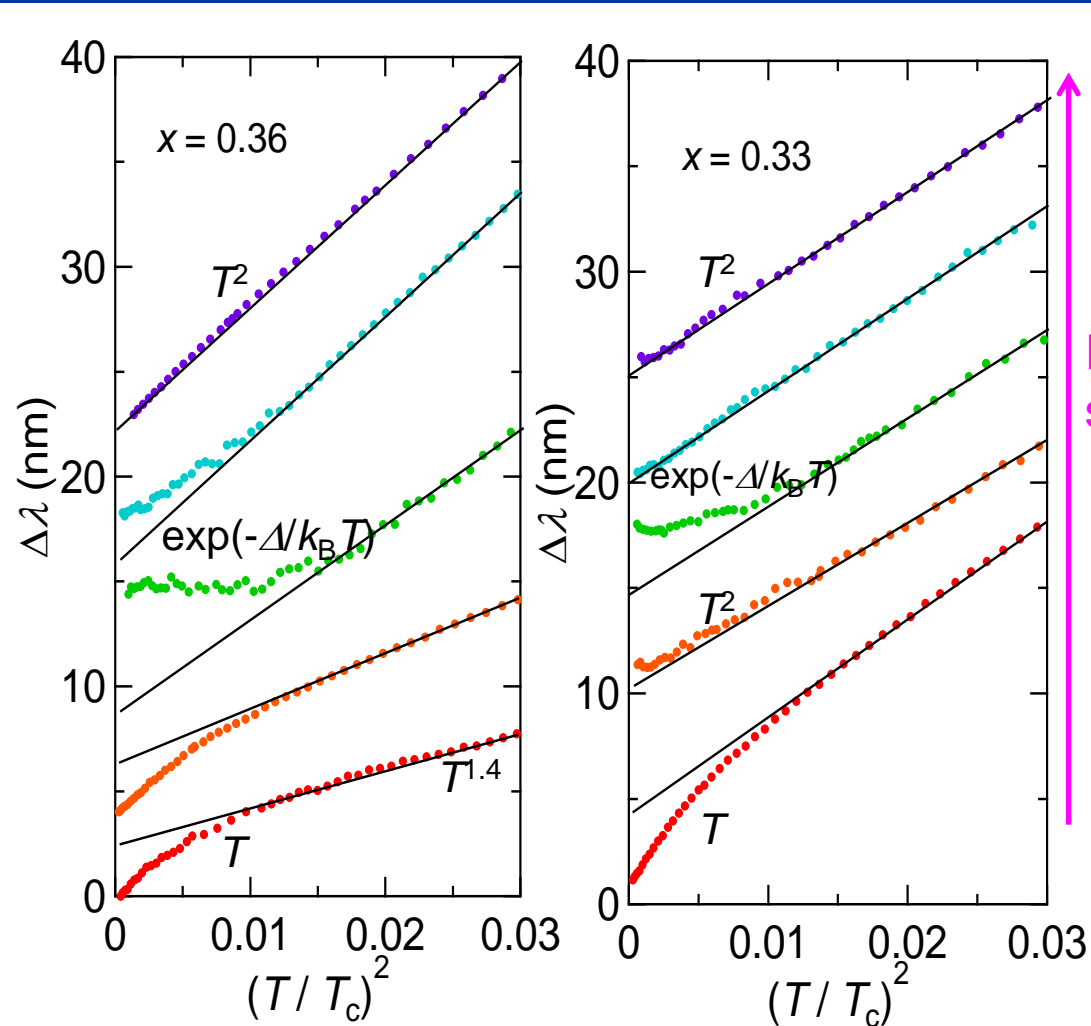
The gap structure changes at $x \sim 0.8$.



Non-universal gap structure in BaFe₂As₂ systems

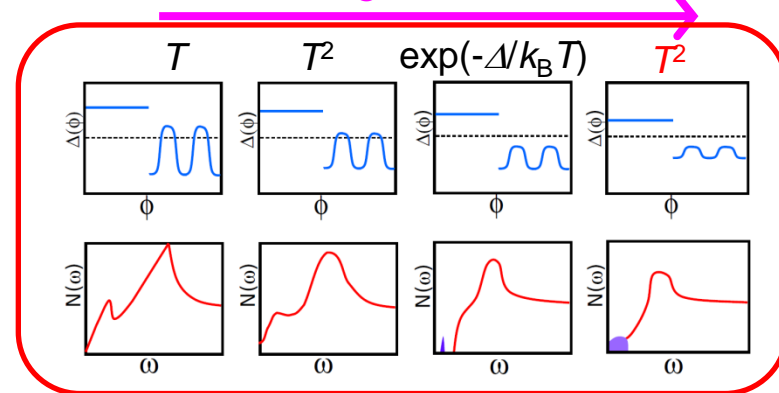


Observation of node lifting by disorder



no evidence of Curie upturn
down to ~ 80 mK
magnetic moment of point disorder
is smaller than $\sim 0.2-0.4\mu_B$

“Nonmagnetic” disorder



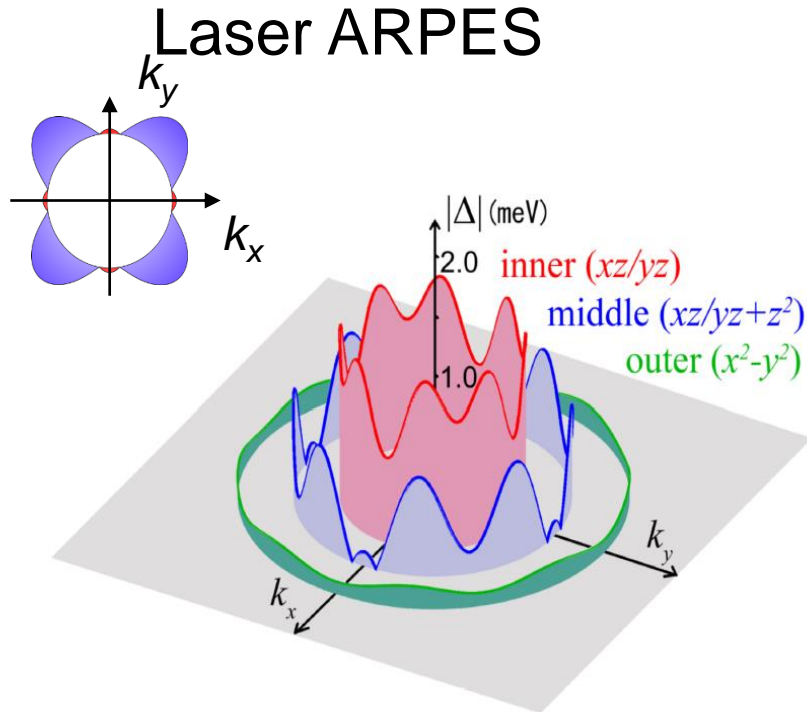
$\Delta\lambda$ changes with irradiation as
 $T \rightarrow T^2 \rightarrow \exp(-\Delta/k_B T) \rightarrow T^2$

Y. Mizukami *et al.*

Y. Wang *et al.*, PRB **87**, 094504 (2013). **S±**

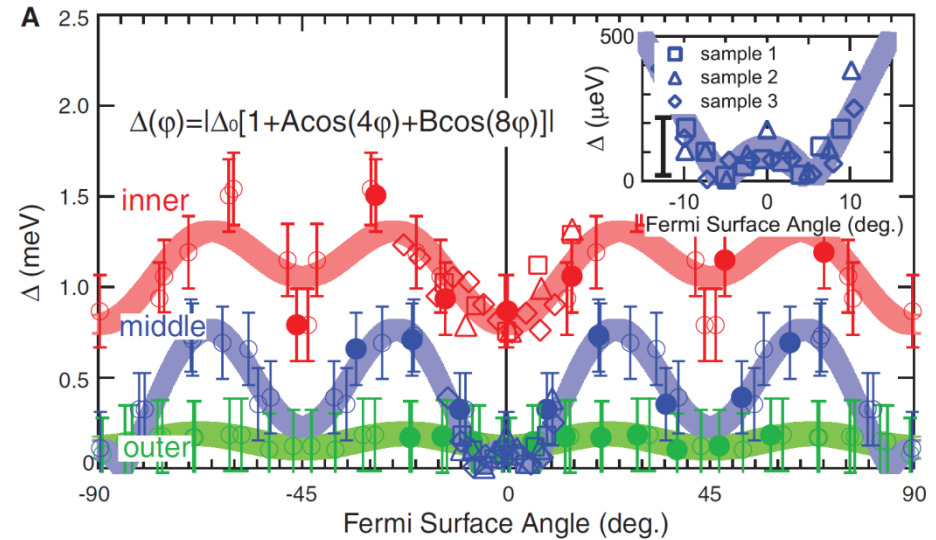
Gap symmetry in KFe_2As_2

Nodal s-wave



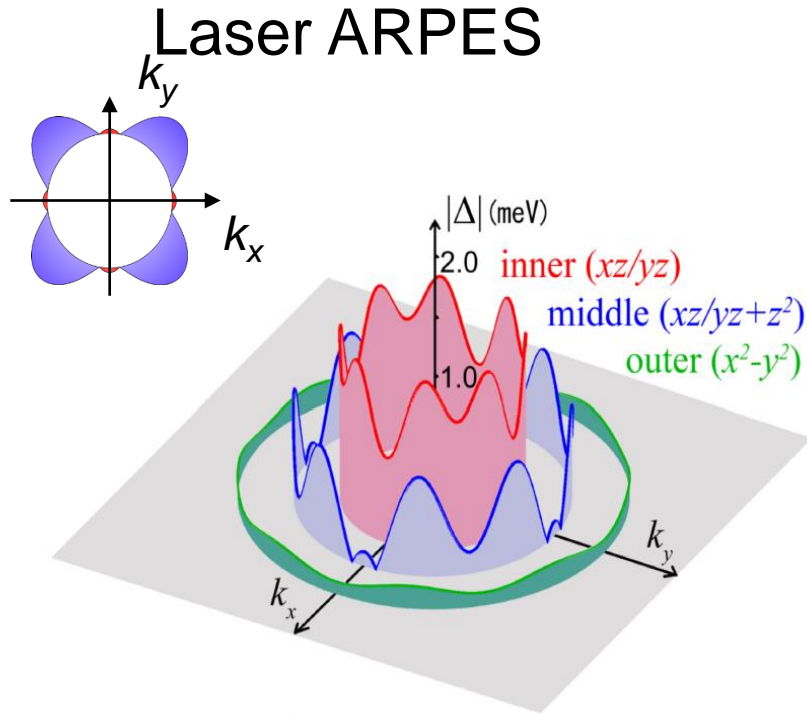
K. Okazaki *et al.*, Science (2012).

Octet-Line Node



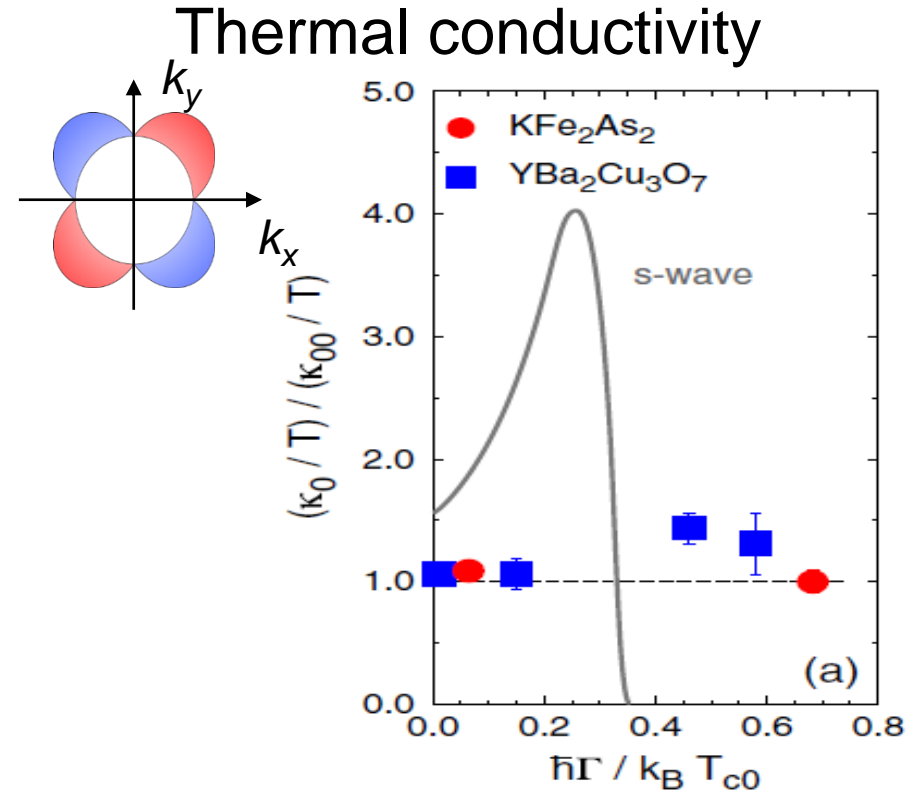
Gap symmetry in KFe_2As_2

Nodal s-wave



K. Okazaki *et al.*, Science (2012).

d-wave

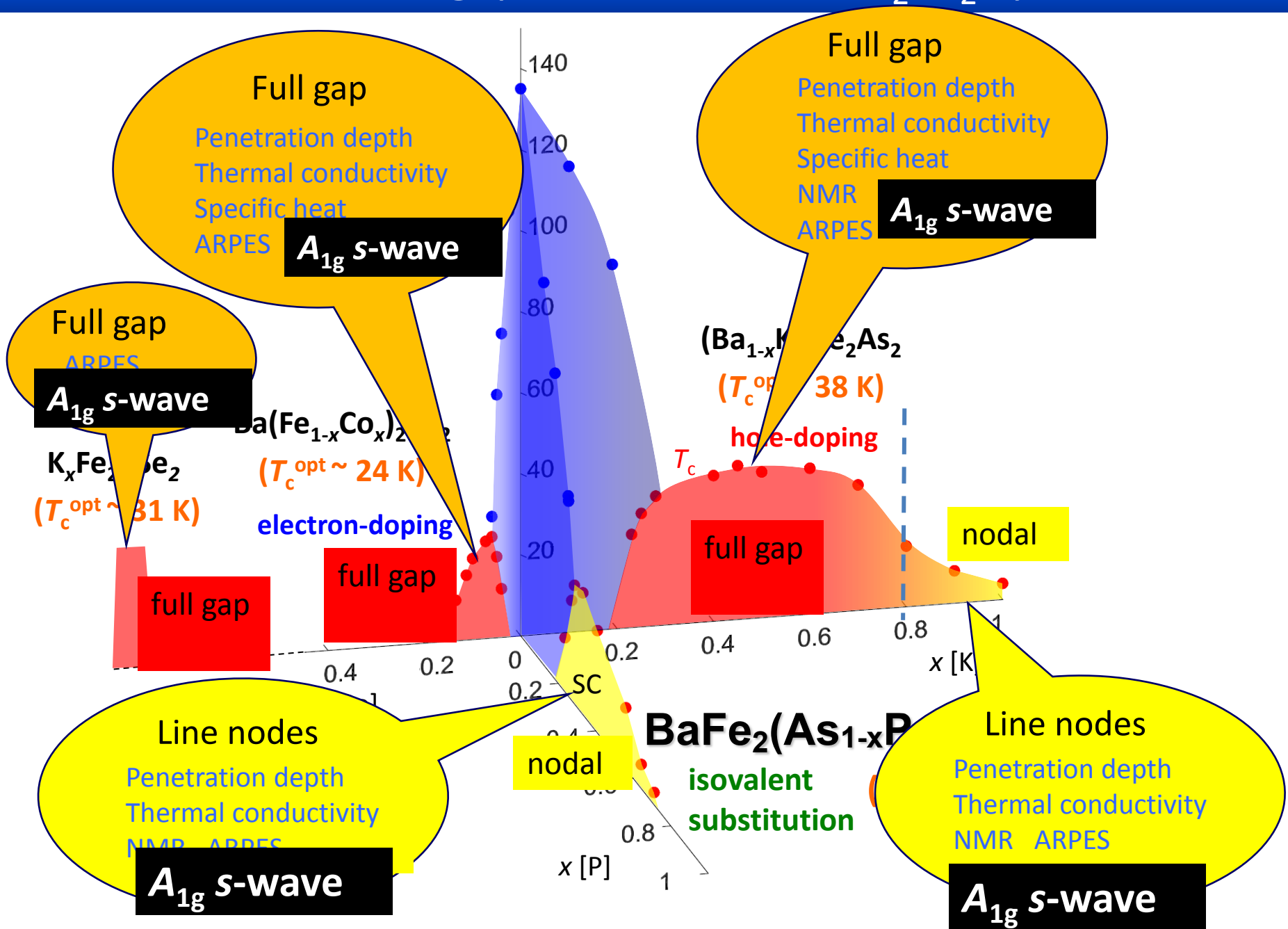


J.P.Reid *et al.* PRL (2012)

Specific heat

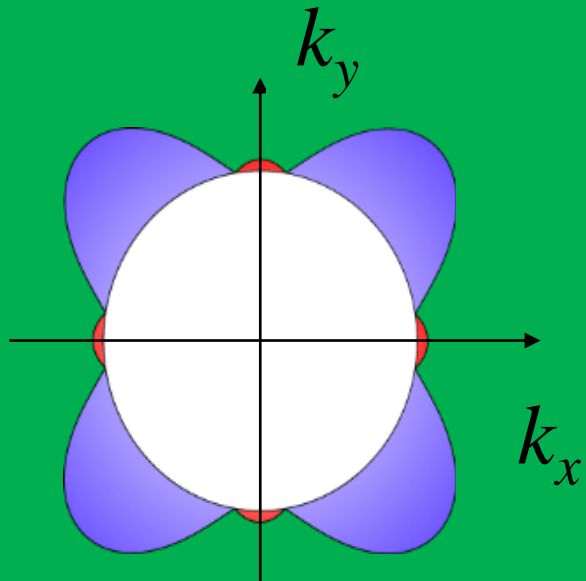
F. Hardy *et al.* JPSJ (2013)

Non-universal gap structure in BaFe₂As₂ systems

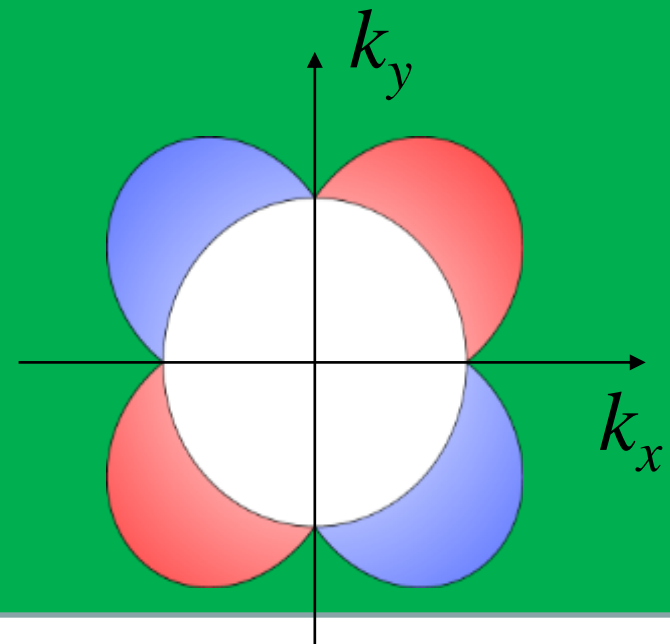


Non-universal gap structure in BaFe_2As_2 systems

s-wave (A_{1g})
Nodes: Accidental



d-wave (B_{1g} or B_{2g})
Nodes: Symmetry-protected



or

What's the symmetry?

What's the symmetry?

鉄系高温超伝導体

銅酸化物、重い電子系との比較

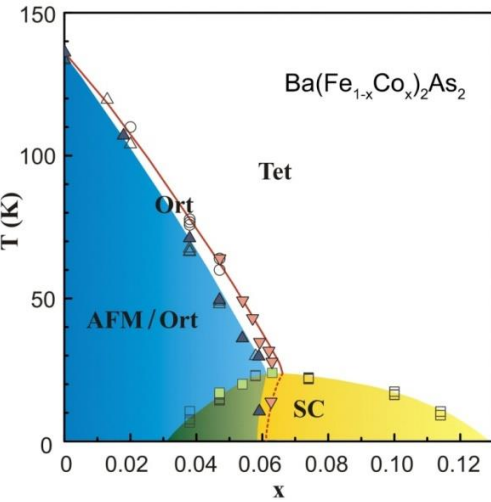
超伝導ギャップ構造

量子臨界点

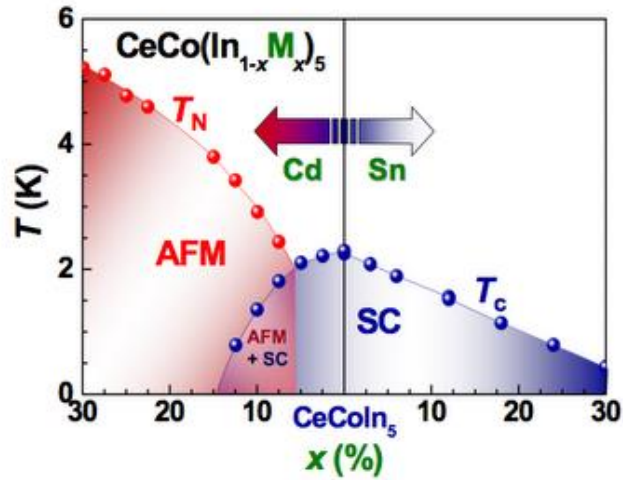


Quantum Critical Point (QCP)

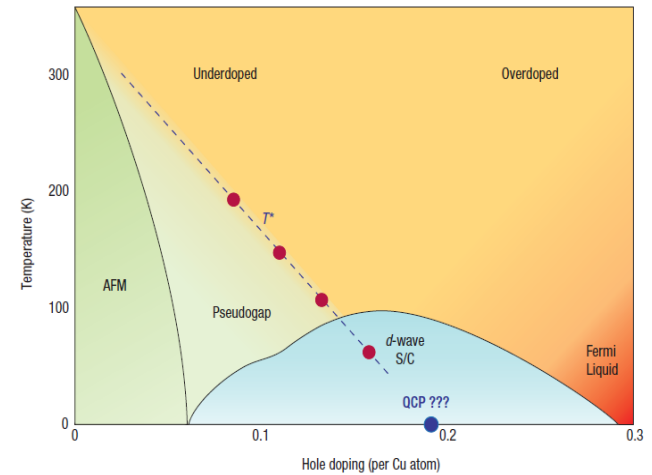
Fe-pnictide



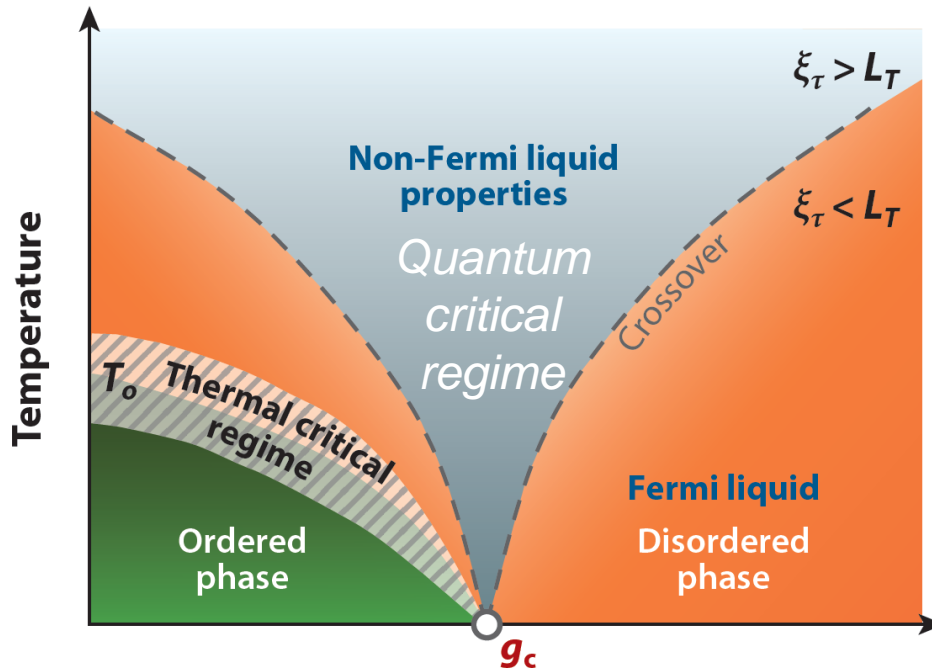
Heavy Fermion



Cuprate



Quantum Critical Point (QCP)



Control parameter g
(Quantum critical point)

g : pressure, chemical substitution, magnetic field

S. Sachdev, Quantum Phase Transitions

Quantum time scale

$$\xi \propto |g - g_c|^\nu \quad \xi_\tau \propto \xi^z$$

Thermal time scale

$$L_T = \frac{\hbar}{k_B T}$$

$$\xi_\tau < L_T$$

QP excitations are well defined

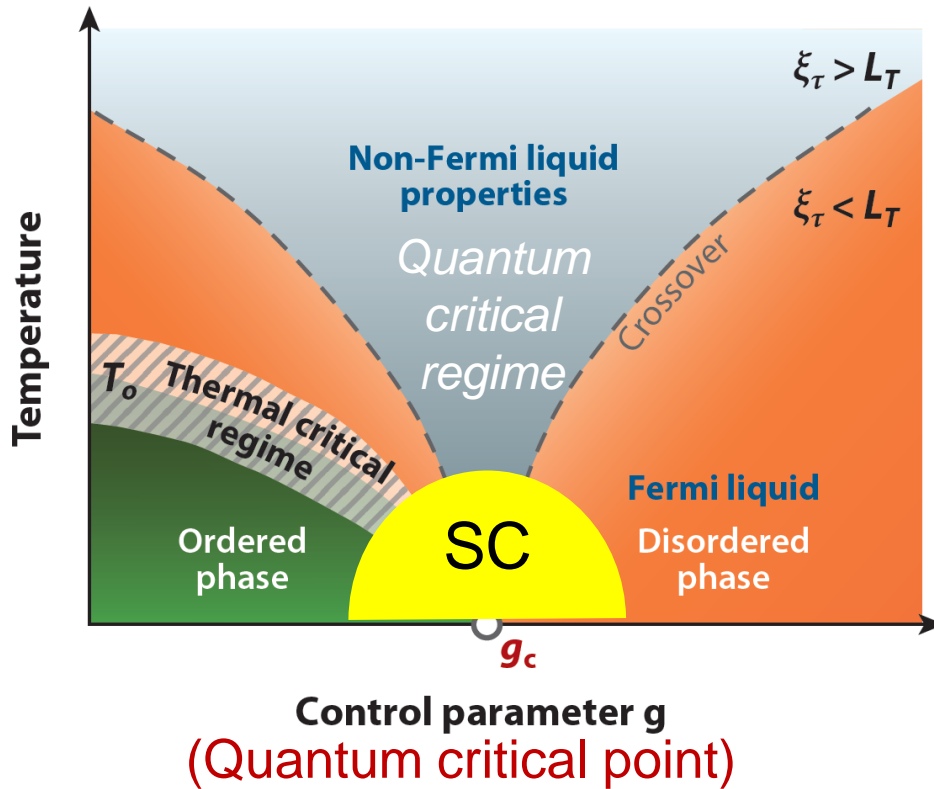
$$\xi_\tau > L_T$$

Physical properties are seriously influenced by QCP at $g=g_c$.

Ordinary phase transition – driven by thermal fluctuations

Quantum phase transition – driven by zero temperature quantum fluctuations associated with Heisenberg's Uncertainty Principle

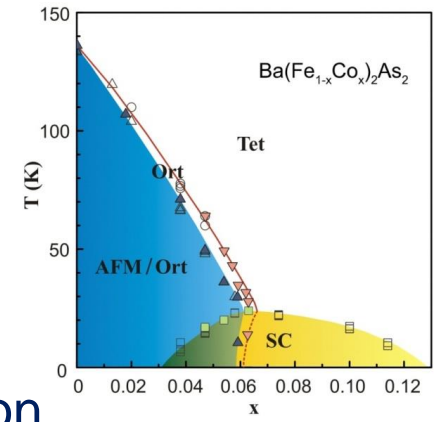
Quantum Critical Point (QCP)



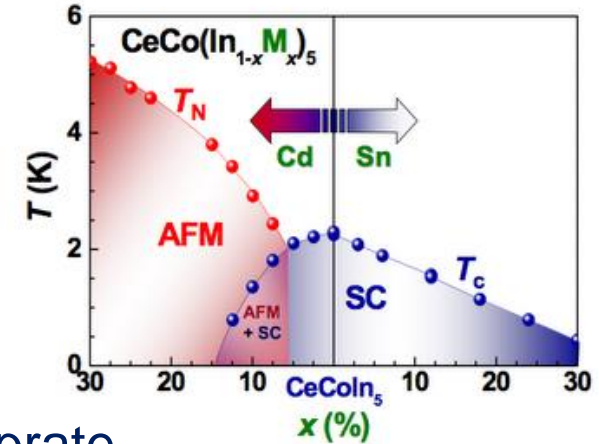
g : pressure, chemical substitution, magnetic field

S. Sachdev, Quantum Phase Transitions

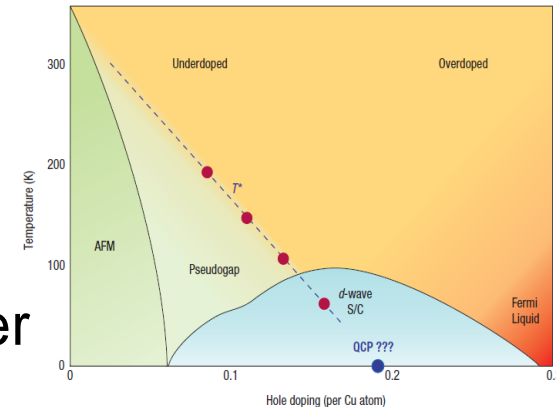
Fe-pnictide



Heavy Fermion



Cuprate

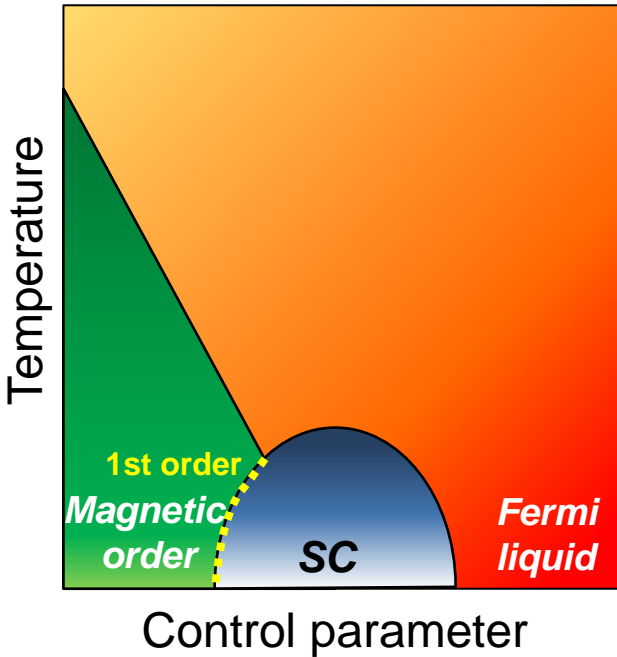


Does the QCP lie beneath the SC dome?

1. Mechanism of superconductivity
2. non-Fermi liquid properties
3. Coexistence of SC and magnetic (exotic) order

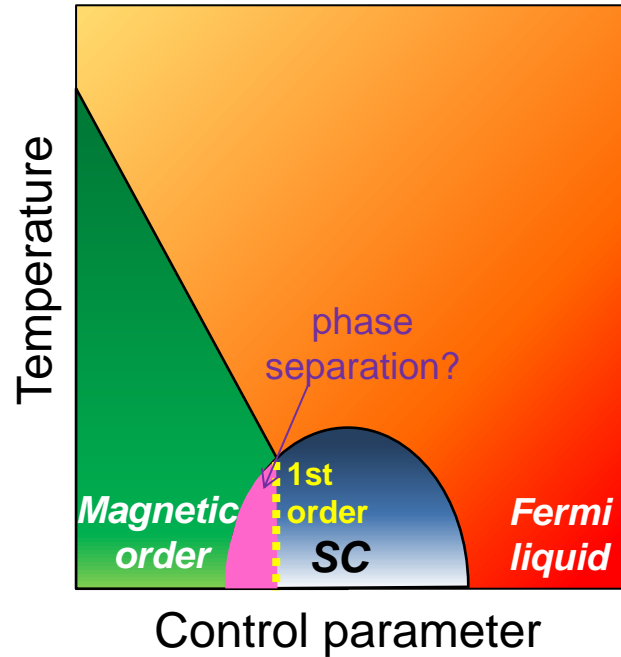
What lies beneath the SC dome?

Case-I



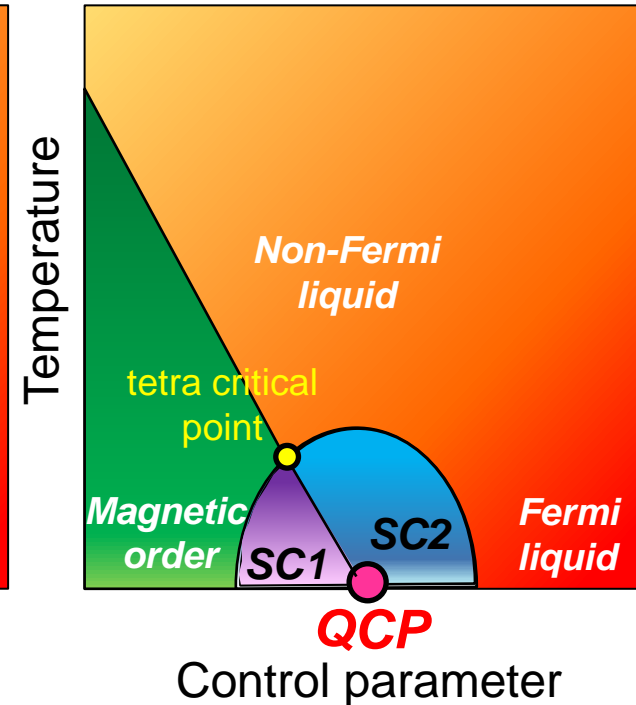
Criticality avoided by the transition to the SC state

Case-II



QCP lying beneath the SC dome

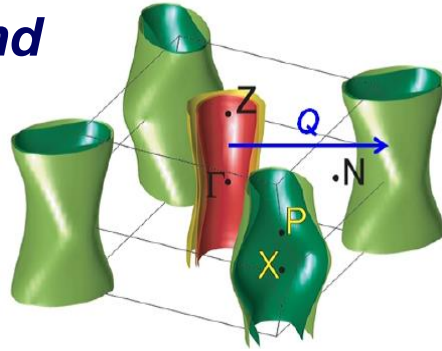
Case-III



Superconductivity in BaFe₂As₂ systems

Parent compound

BaFe₂As₂
(AF Metal)



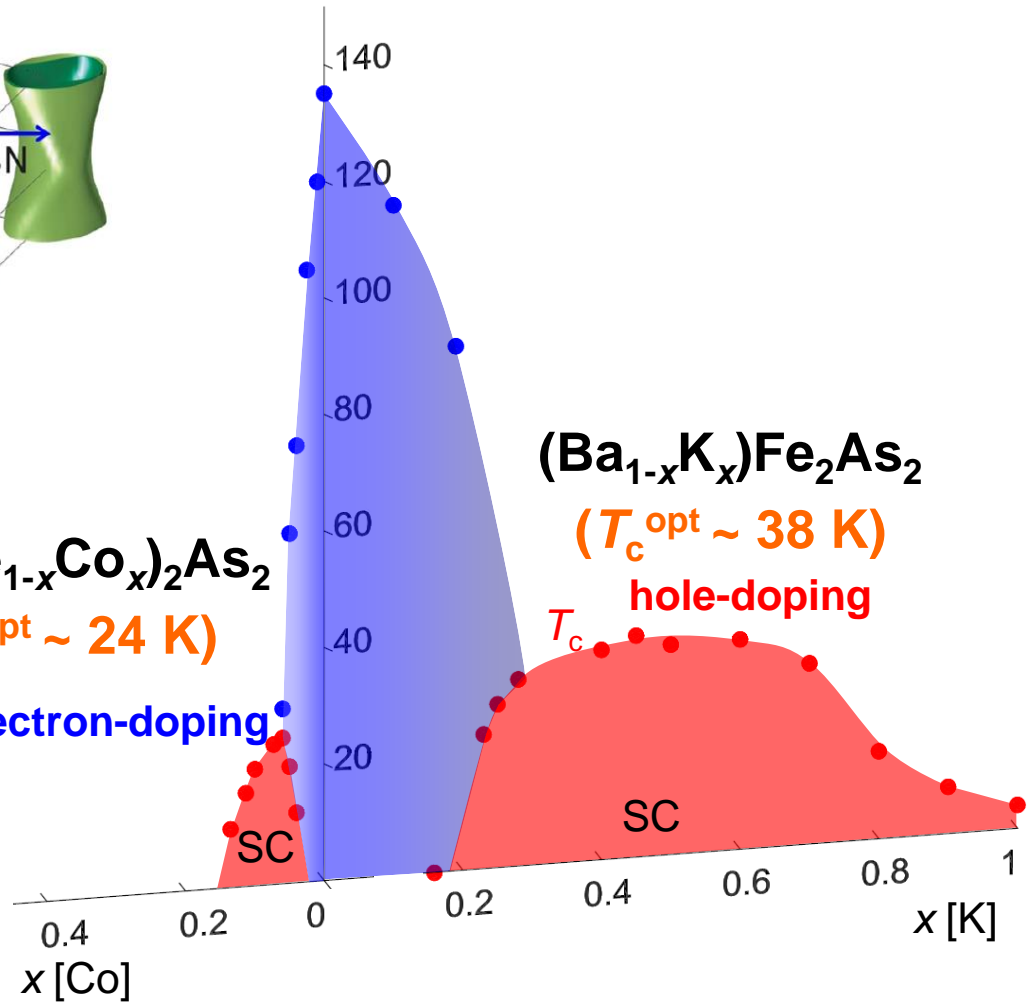
Ba(Fe_{1-x}Co_x)₂As₂
($T_c^{opt} \sim 24$ K)

electron-doping

(Ba_{1-x}K_x)Fe₂As₂

($T_c^{opt} \sim 38$ K)

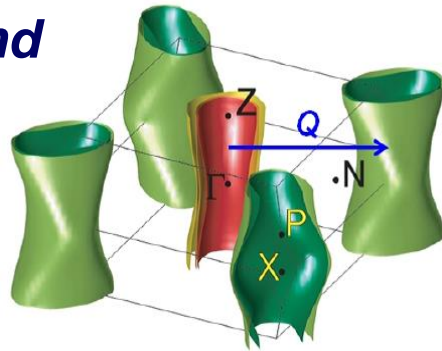
hole-doping



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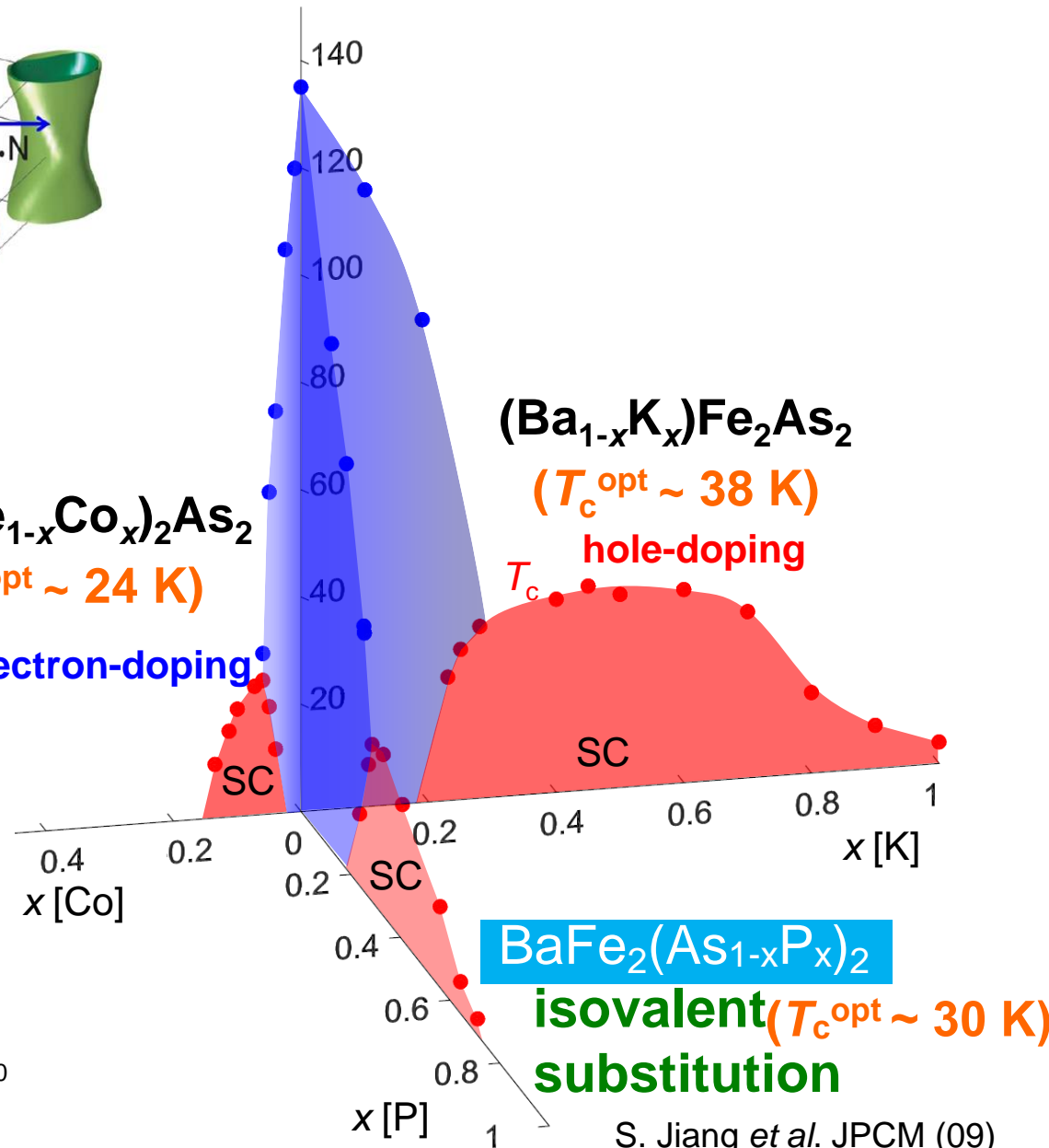
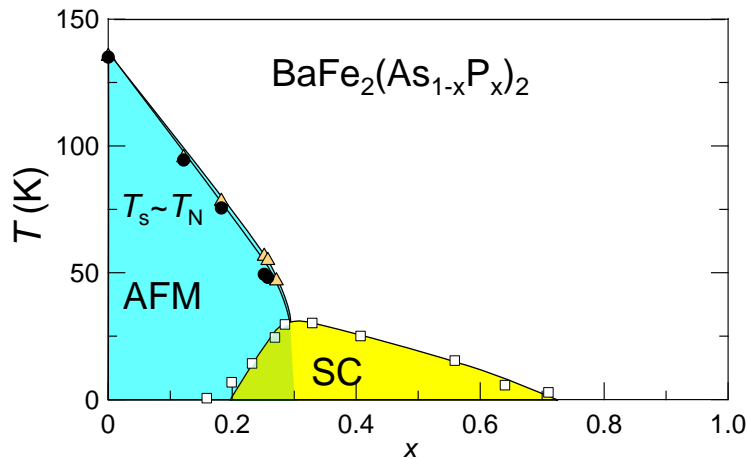
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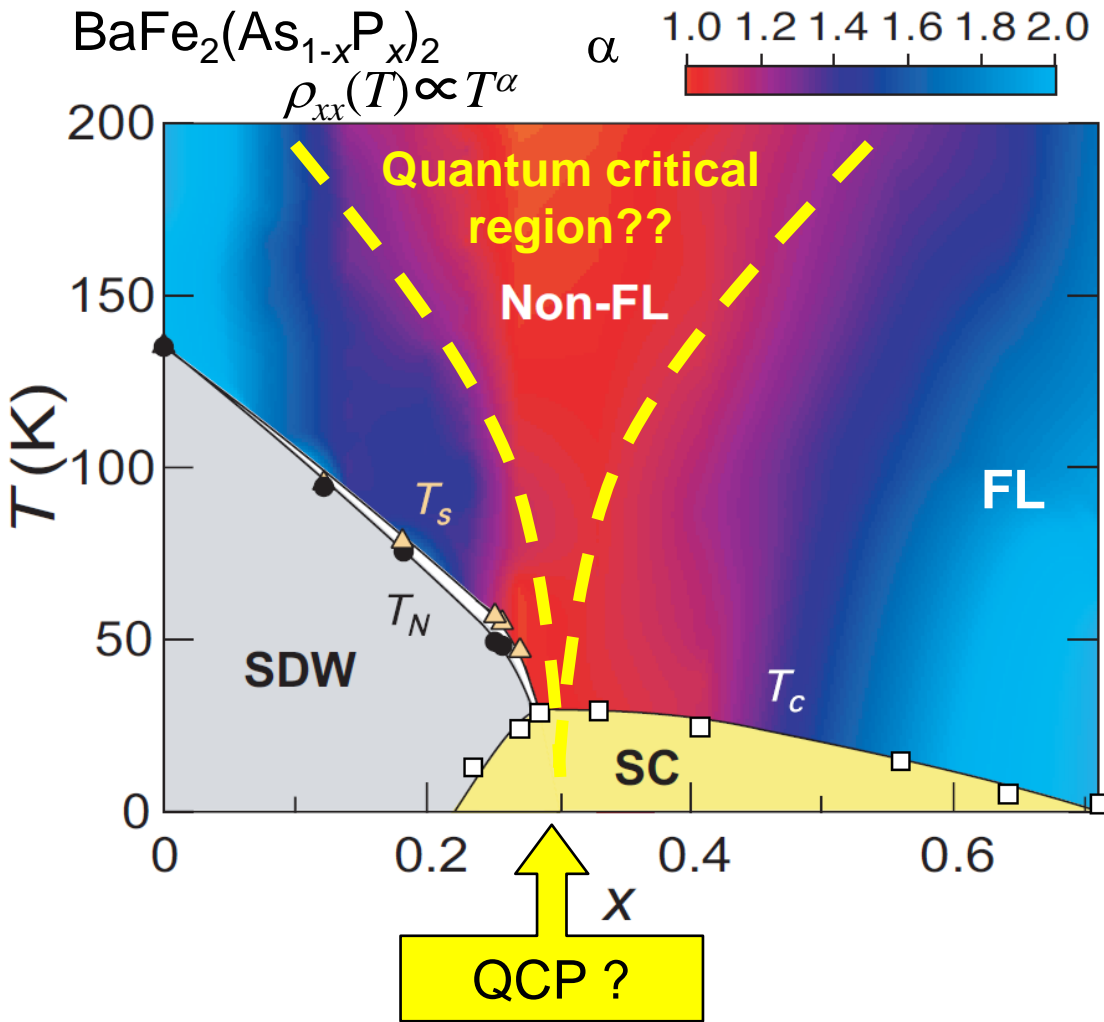
hole-doping

T_c

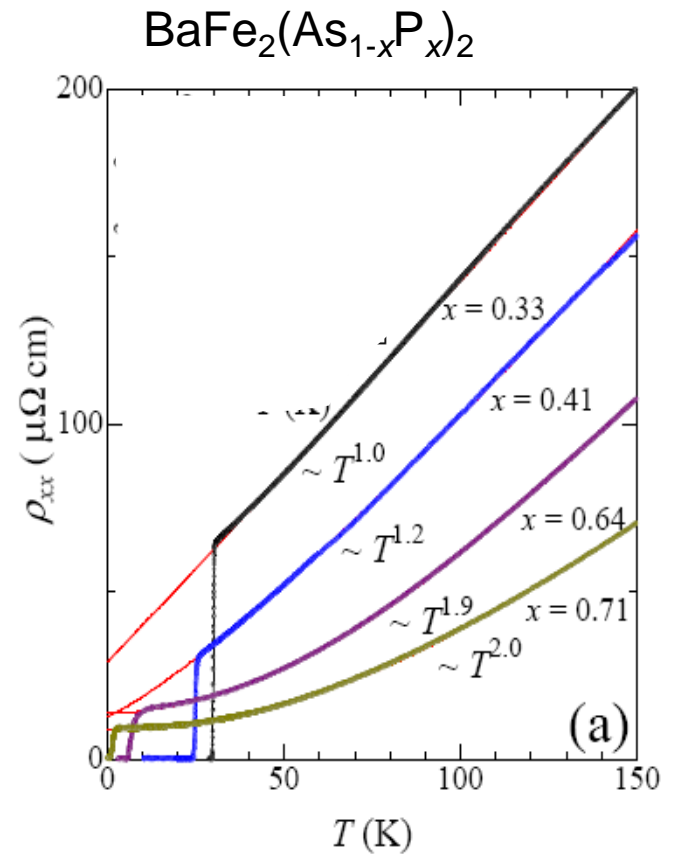


Ground state can be tuned without doping carriers

Doping evolution of the transport property



S. Kasahara *et al.*, PRL (10)



T -linear resistivity at $x=0.33$ just beyond SDW end point ($x_c=0.3$)

Hallmark of non-Fermi liquid

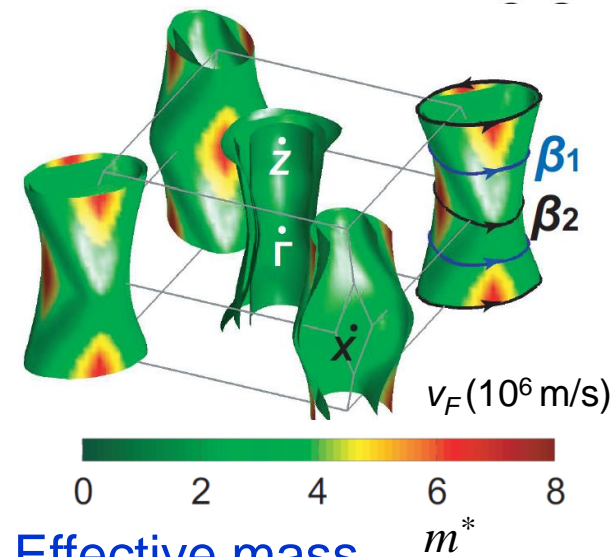
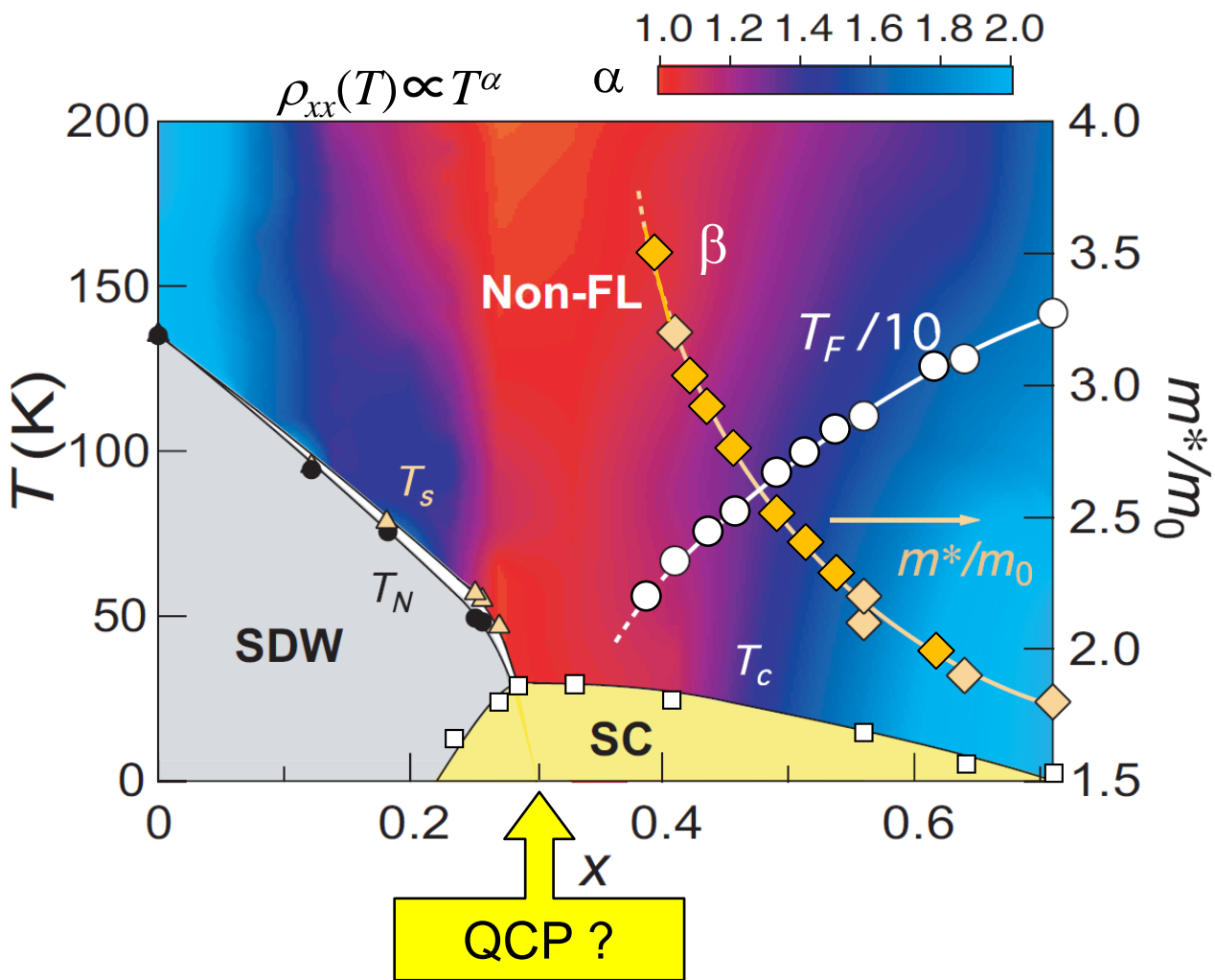
T^2 -dependence at $x=0.71$

Fermi-liquid behavior

See also

S. Sachdev and B. Keimer, Physics Today (11)

Fermi surface and mass renormalization

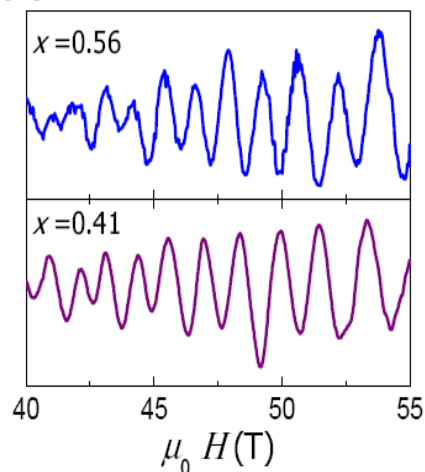


Effective mass

Fermi temperature

$$T_F = \hbar e F / m^* k_B$$

dHvA



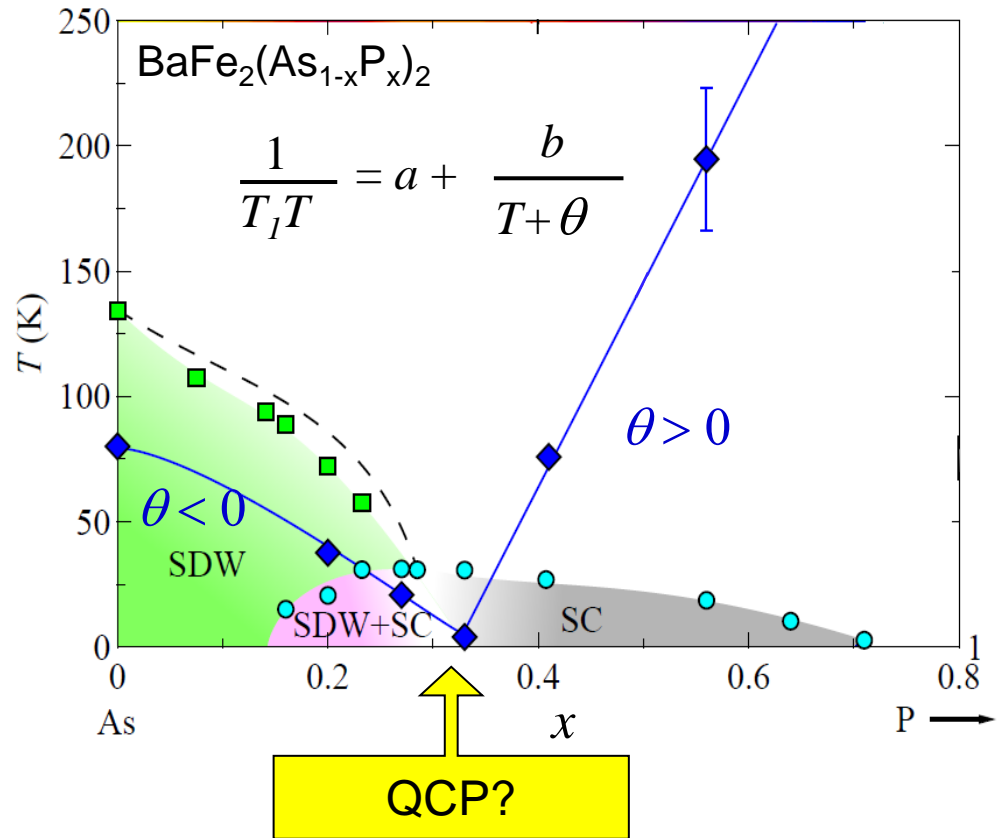
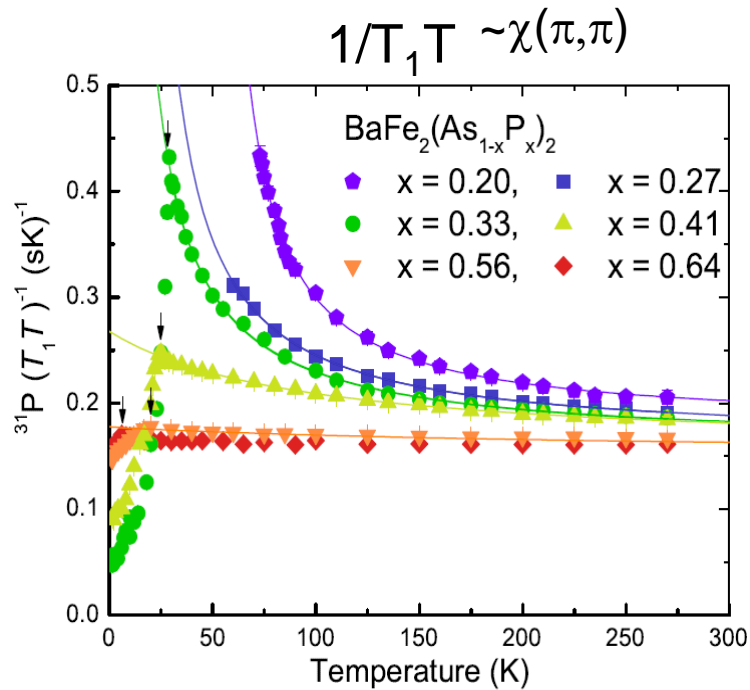
As x is tuned towards the maximum T_c ,

Effective mass m^* is strongly enhanced

Fermi temperature $T_F = \hbar e F / m^* k_B$ tends to zero

Doping evolution of the magnetic fluctuations (^{31}P NMR)

θ : Weiss temperature

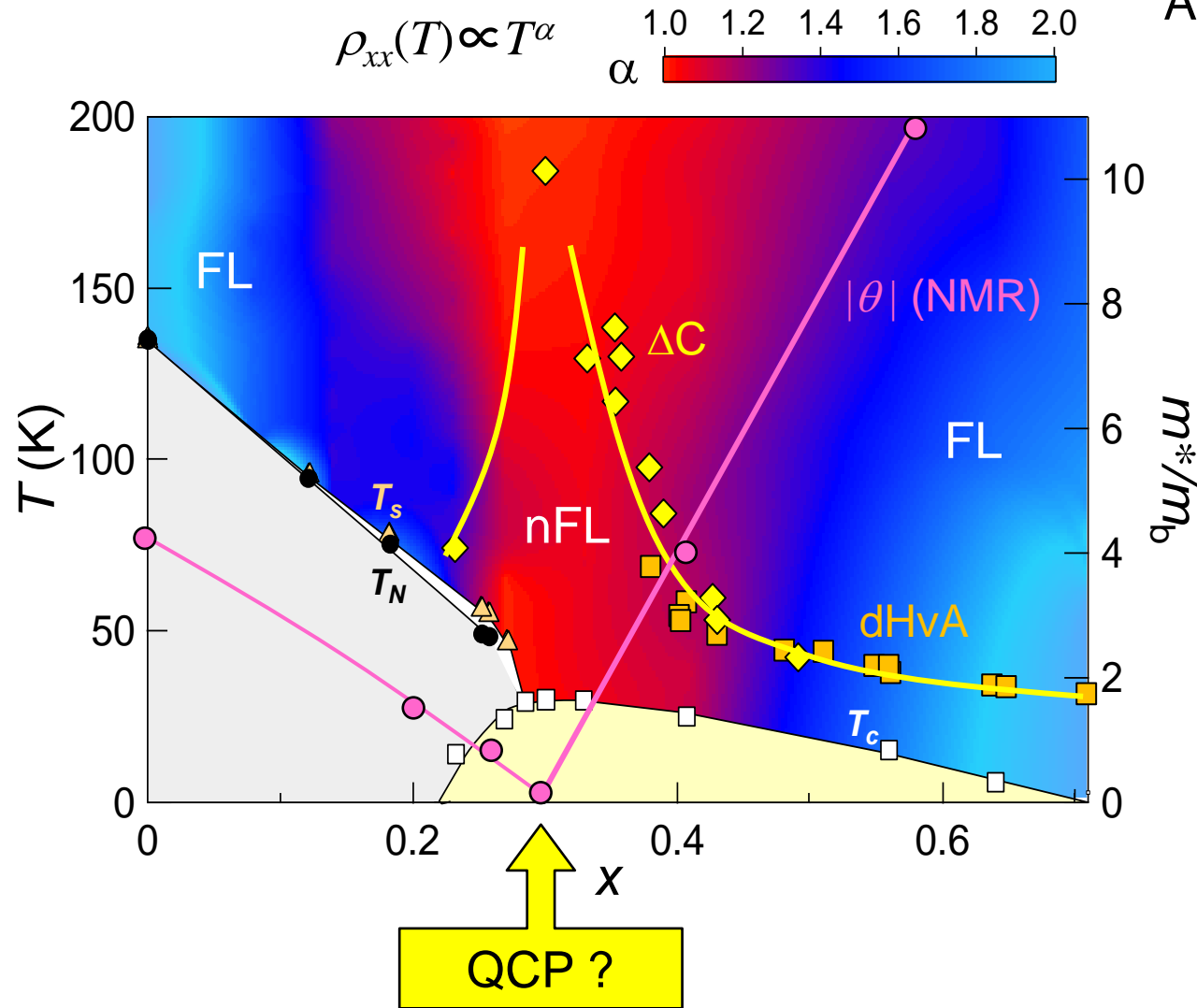


θ goes to zero at $x \sim 0.3$

Dynamical susceptibility diverse at $T=0$ K.

Doping evolution of normal electrons

As x is tuned towards the maximum T_c at $x=0.30$



Hallmark of non-Fermi liquid behavior

Resistivity

Effective mass m^ is strongly enhanced*

dHvA

Specific heat

Weiss temperature goes to zero

NMR

We need evidence at zero temperature and zero field.

Doping evolution of the London penetration depth at $T=0$

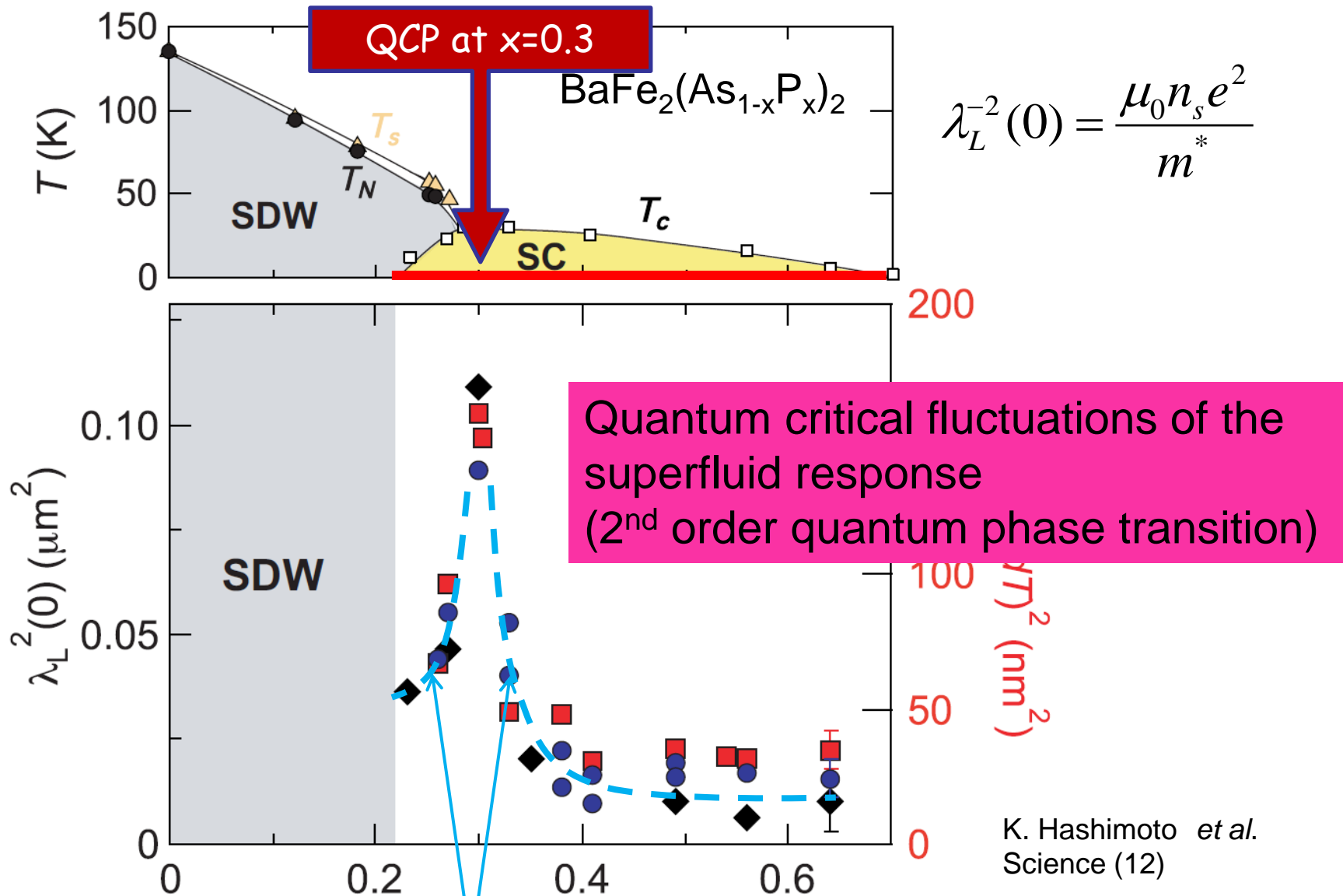
London penetration depth λ_L is the quantity that can probe the electronic structure **at zero temperature limit**.

$$\lambda_L^{-2}(0) = \frac{\mu_0 n_s e^2}{m^*}$$

Number of superfluid

Mass of superfluid

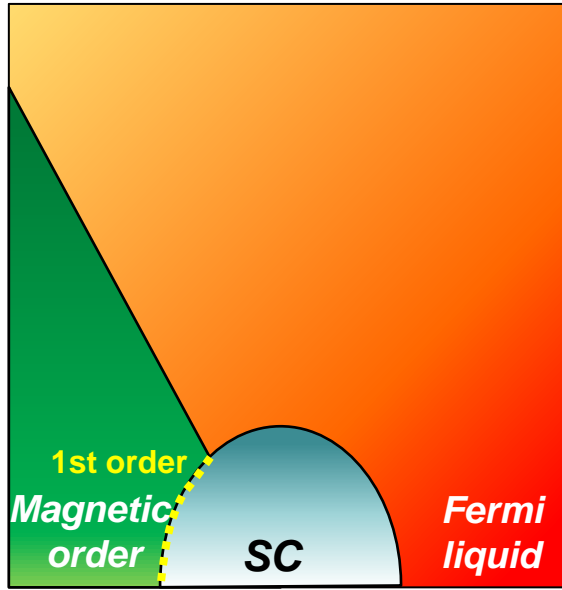
Doping evolution of the London penetration depth at $T=0$



Striking enhancement of $\lambda_L^2(0)$ on approaching $x=0.3$ from *either* side.
 The data represents the behavior at *the zero temperature limit*.

What lies beneath the SC dome?

Case-I



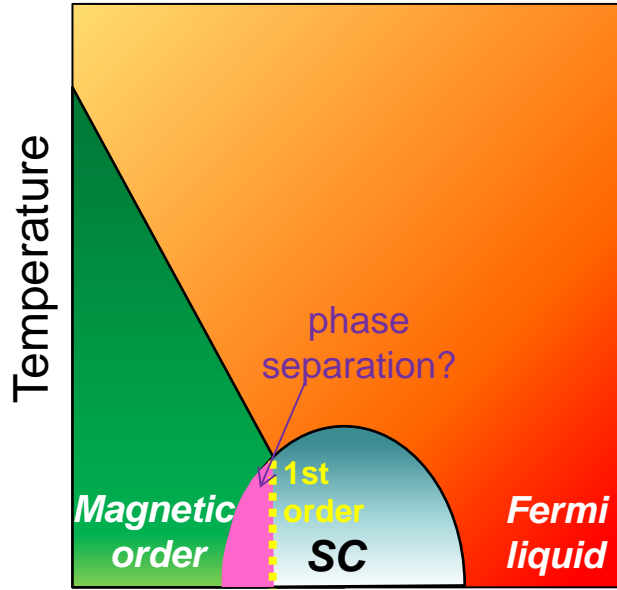
Control parameter



NMR

T. Kawasaki *et al.* J. Phys. Soc. Jpn (04)

Case-II



Control parameter

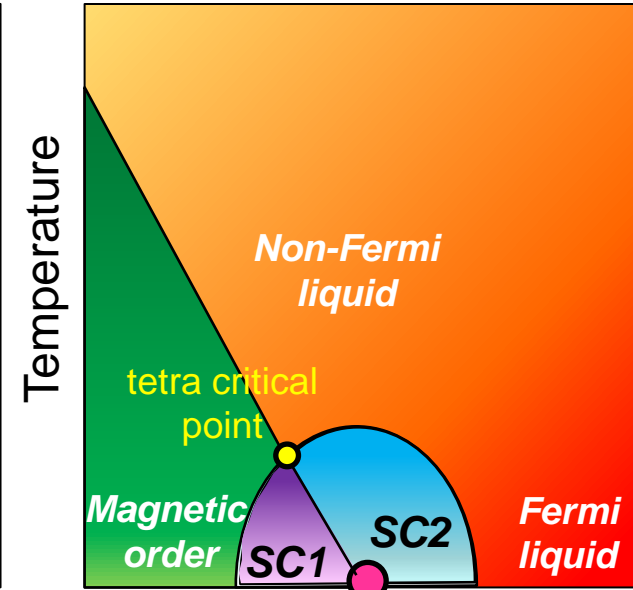


Specific heat

T. Park *et al.* Nature (06)

G. Knebel *et al.* Phys. Rev. B (06)

Case-III



Control parameter

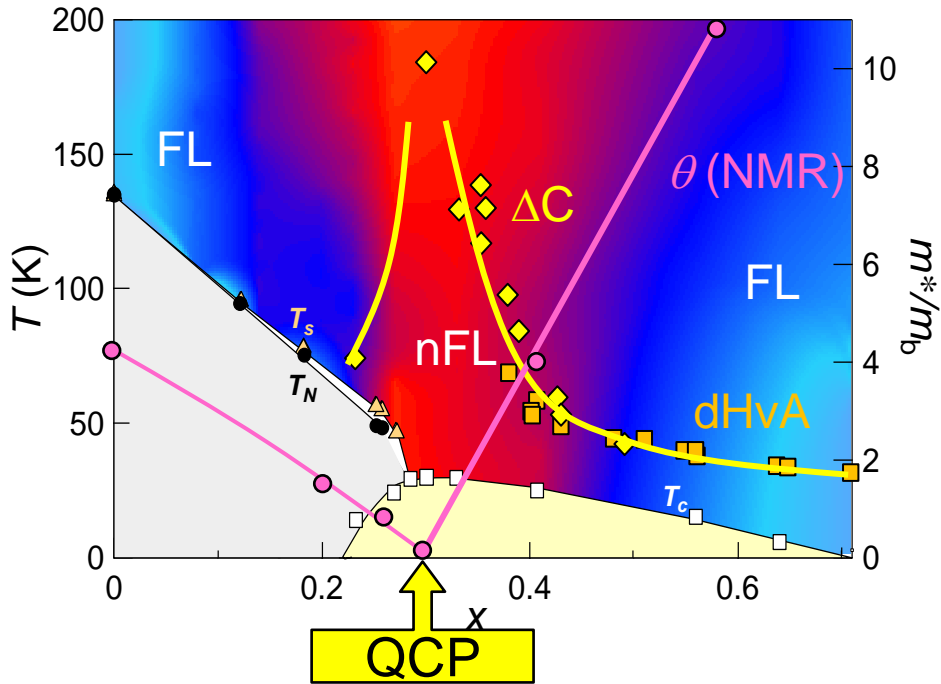
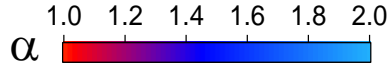


K. Hashimoto *et al.*
Science (12)

QCP lies beneath the dome

Normal electrons

$$\rho_{xx}(T) \propto T^\alpha$$



Hallmark of non-Fermi liquid behavior

S. Kasahara, Y.M. *et al.* PRB (10)

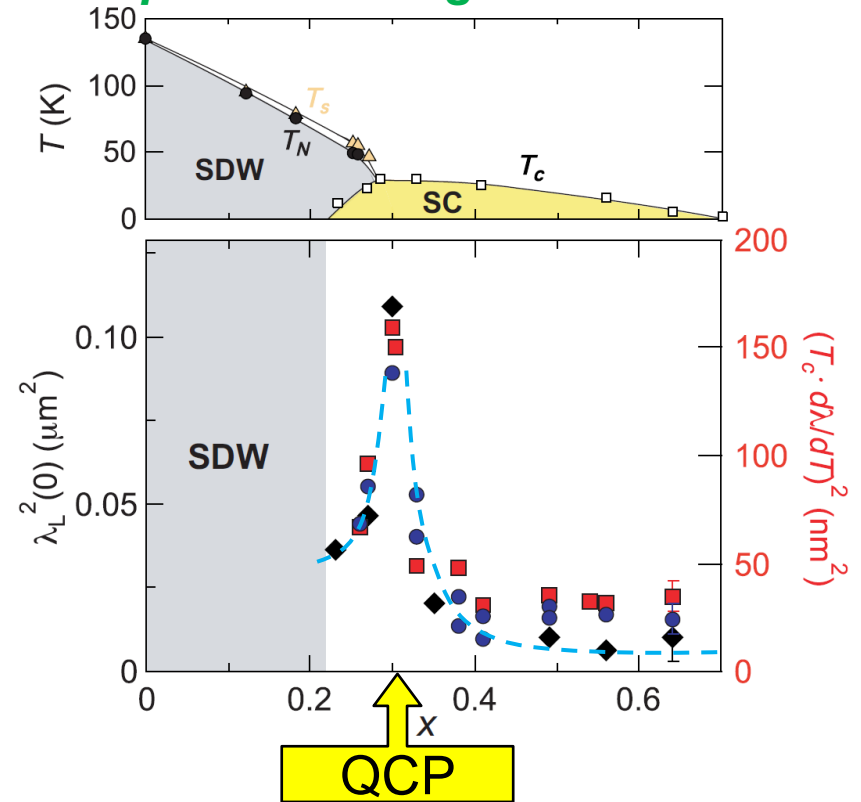
Enhancement of normal electron mass

H. Shishido, Y.M. *et al.* PRL (10), P. Walmsley, Y.M. *et al.* PRL(13)

Vanishing of Weiss temperature

Y. Nakai *et al.* PRL (10)

Superconducting electrons



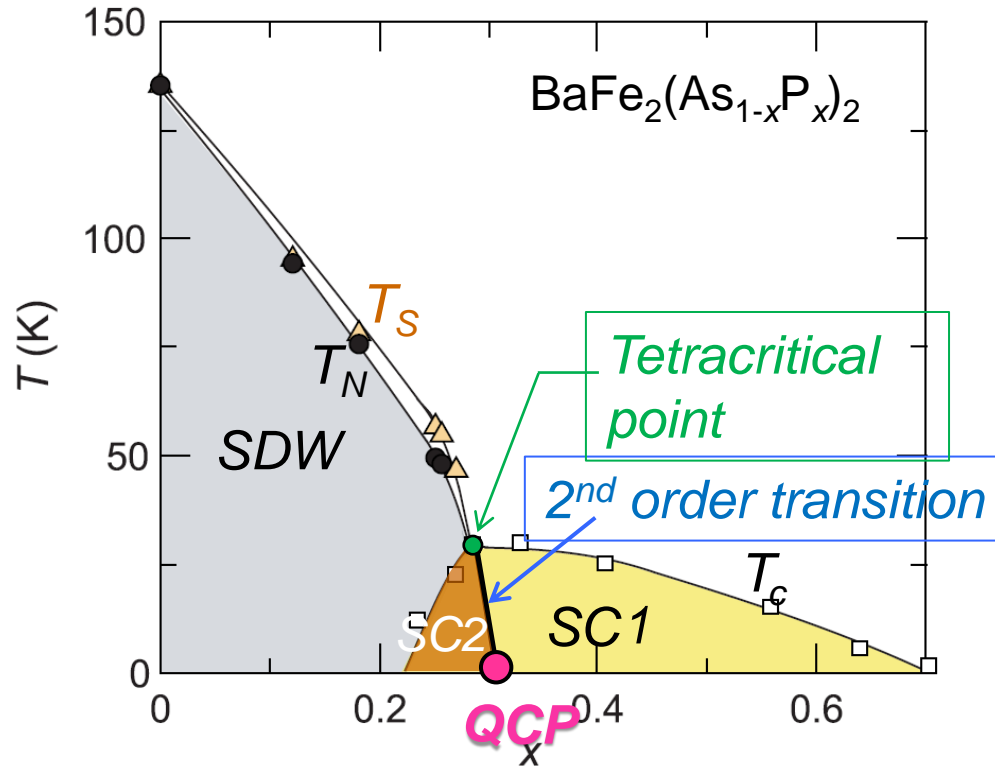
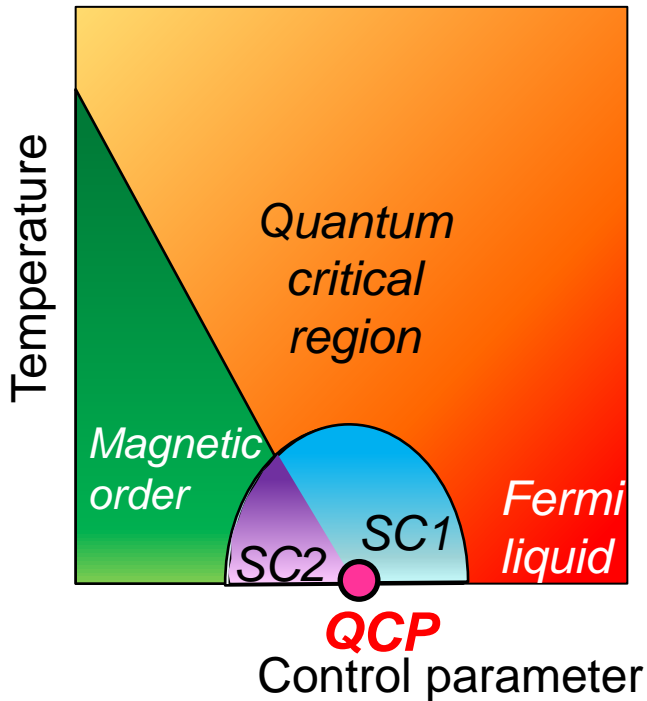
Striking enhancement of superfluid mass

K. Hashimoto, Y.M. *et al.* Science (12), PNAS (13)

QCP lies beneath the superconducting dome

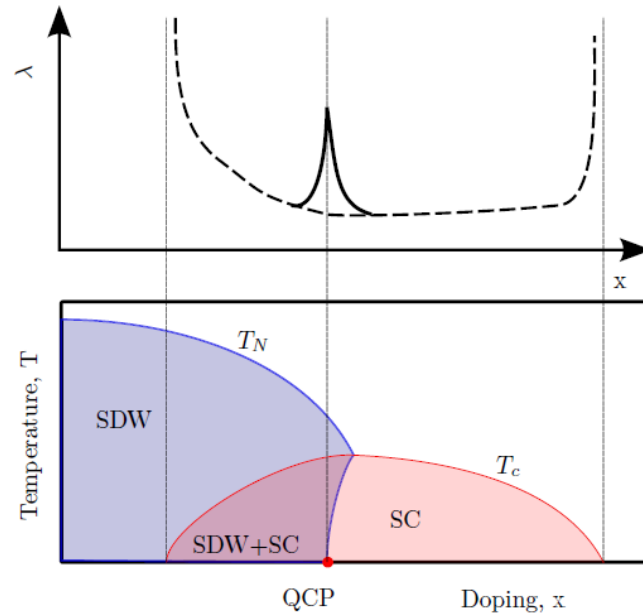
T. Shibauchi, A. Carrington and Y. M., Annu. Rev. Condens. Matter Phys. 5, 113 (14)

QCP lies beneath the dome



1. The QCP is the origin of the non-Fermi liquid behavior above T_c .
2. Microscopic coexistence of superconductivity and SDW.
3. The quantum critical fluctuations help to enhance the high- T_c superconductivity.

Singularity of the London penetration depth at QCP



1) Mass renormalization of superfluid by critical magnetic fluctuations

A. Levchenko, M. G. Vavilov, M. Khodas, and A. V. Chubukov, PRL (13)
T. Nomoto and H. Ikeda, PRL (13)

2) SDW fluctuations + nematic order

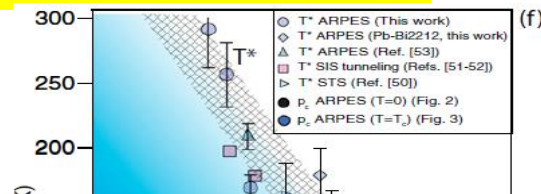
D. Chowdhury, B. Swingle, E. Berg, and S. Sachdev, PRL (13)

Doping evolution of the London penetration depth at $T=0$

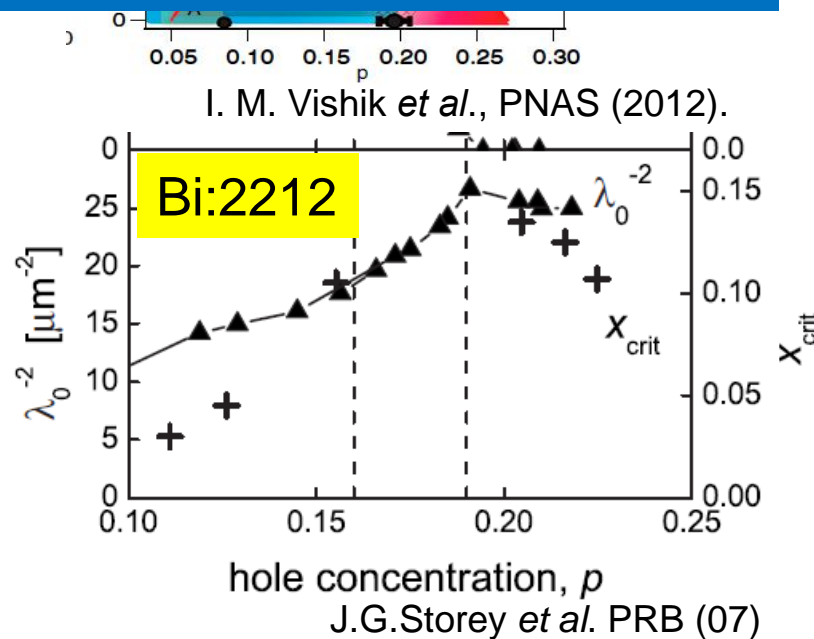
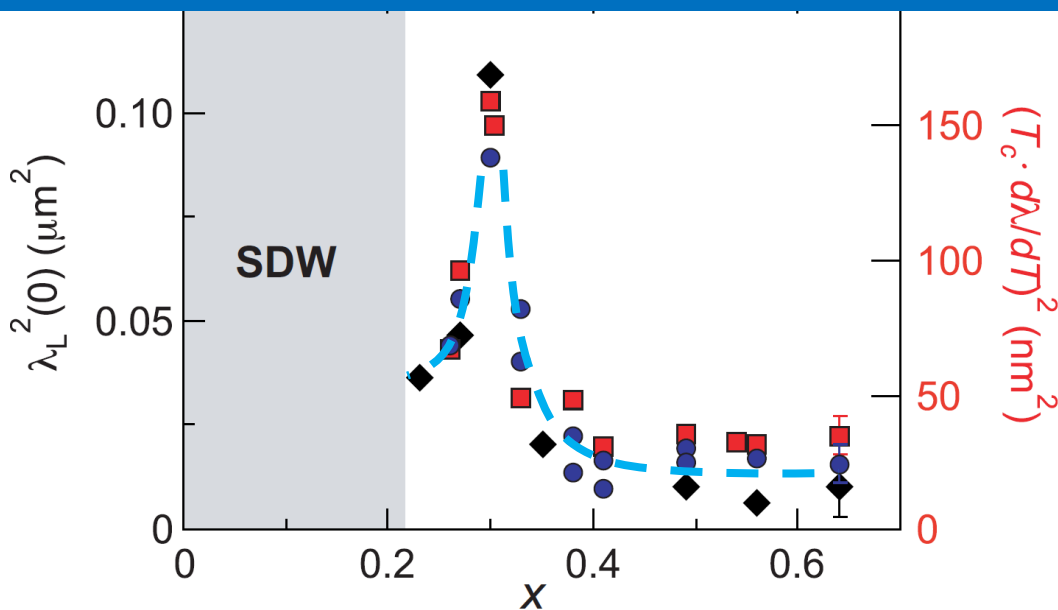
BaFe₂(As_{1-x}P_x)₂



High- T_c cuprates



Superfluid density n_s/m^* at (putative) QCP
 Contrasting behavior between pnictides and cuprates

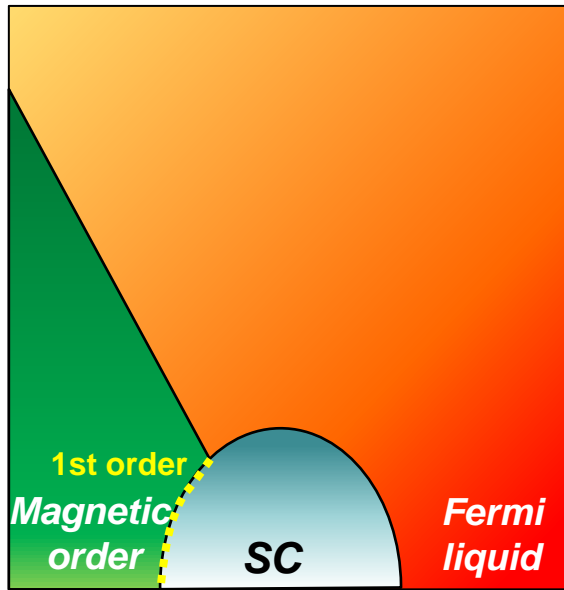


Bi:2212 : broad maximum in $1/\lambda_L^2(0)$ (enhancement of n_s/m^*) at $p \sim 0.19$

BaFe₂(As_{1-x}P_x)₂ : sharp peak in $\lambda_L^2(0)$ (suppression of n_s/m^*) at $x=0.3$

What lies beneath the SC dome?

Case-I



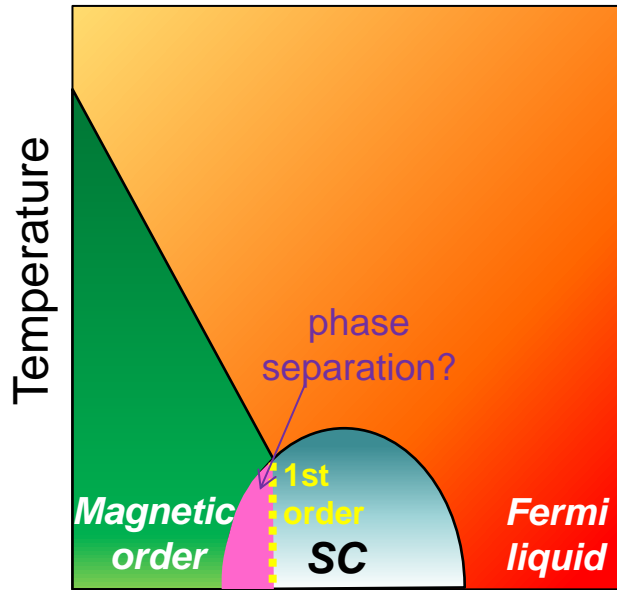
Control parameter



NMR

T. Kawasaki *et al.* J. Phys. Soc. Jpn (04)

Case-II



Control parameter



Specific heat

T. Park *et al.* Nature (06)

G. Knebel *et al.* Phys. Rev. B (06)



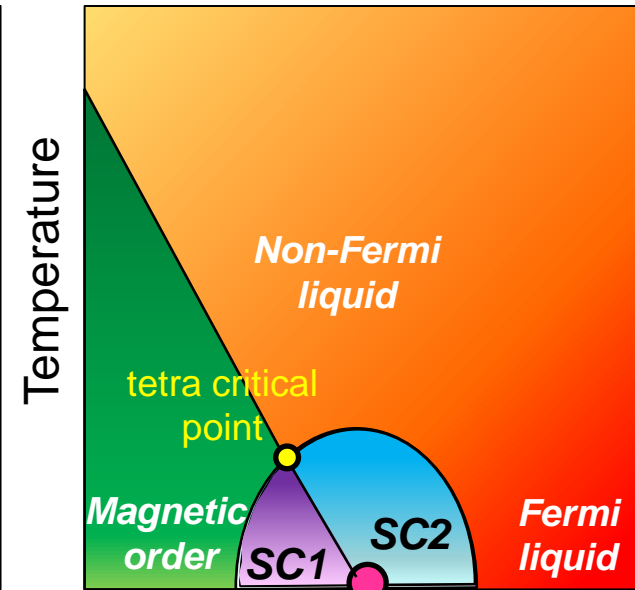
Neutron

Xingye Lu *et al.* PRL (13)

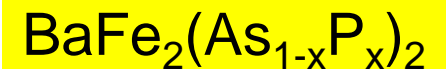


No anomaly in λ_L

Case-III



Control parameter

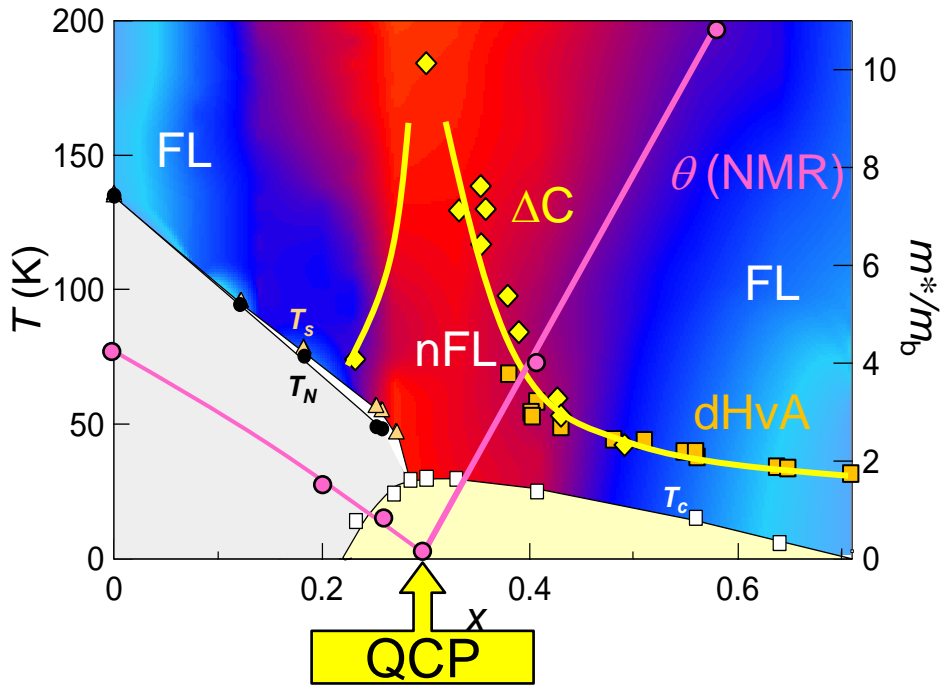
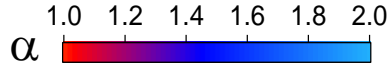


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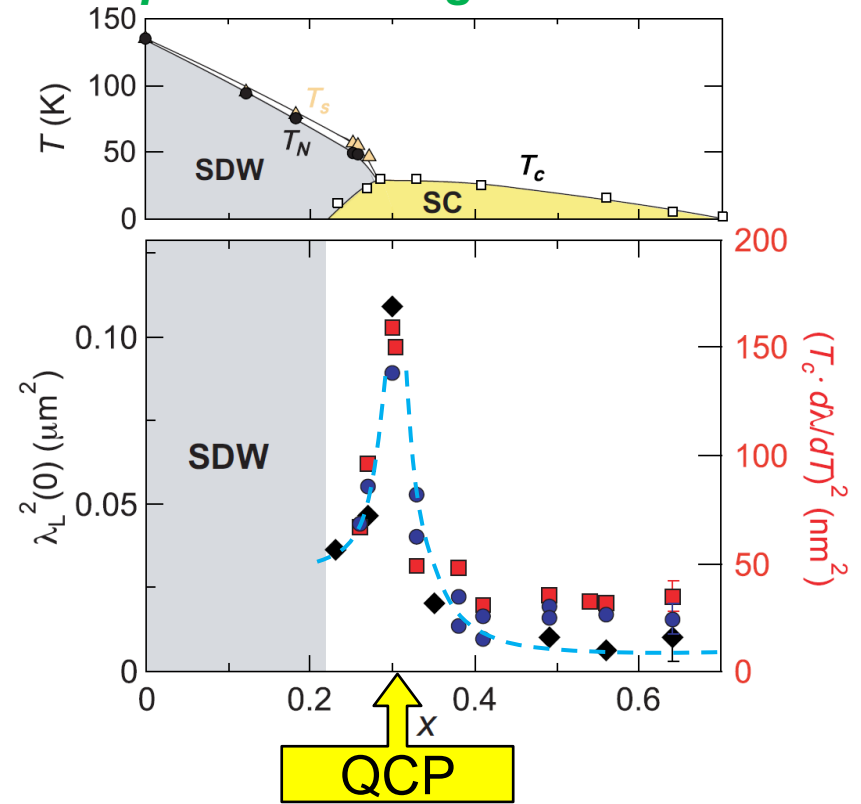
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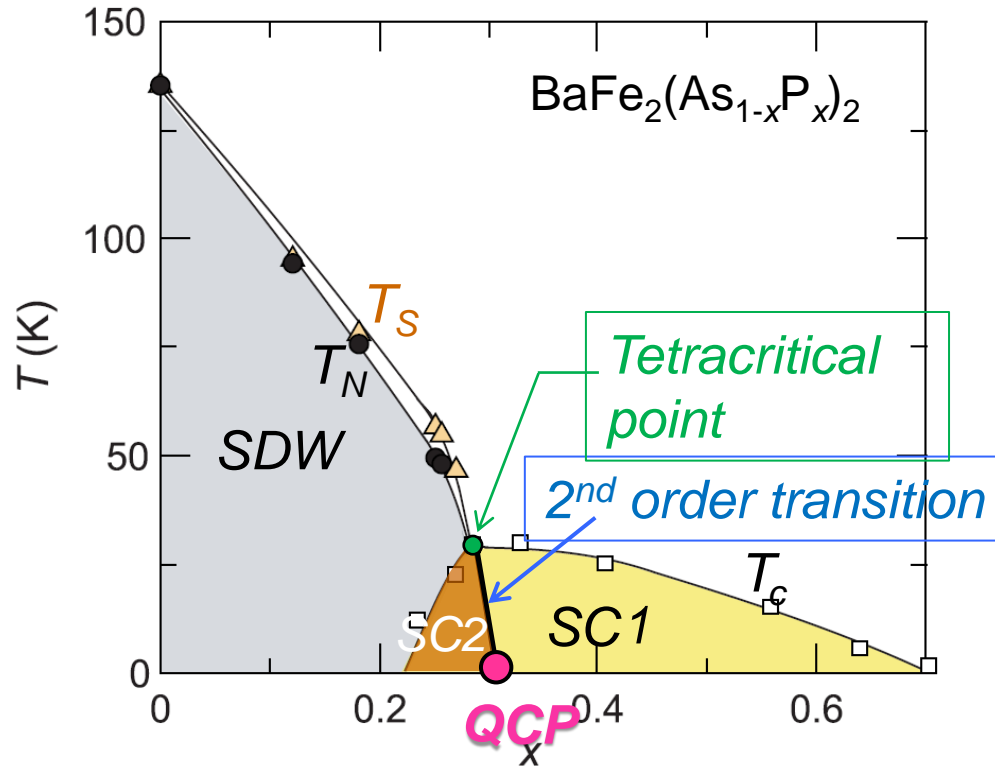
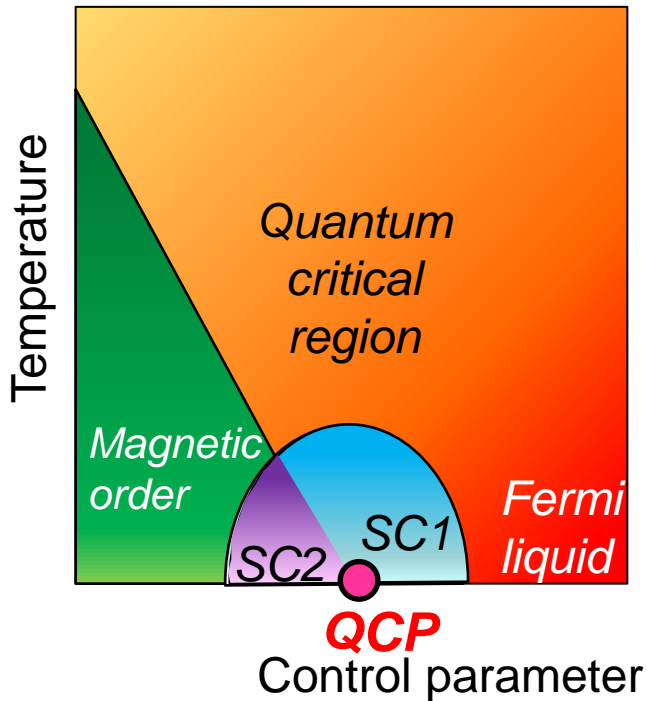
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